

# **State of the Art in Photon Density Estimation: From Photons to Beams**

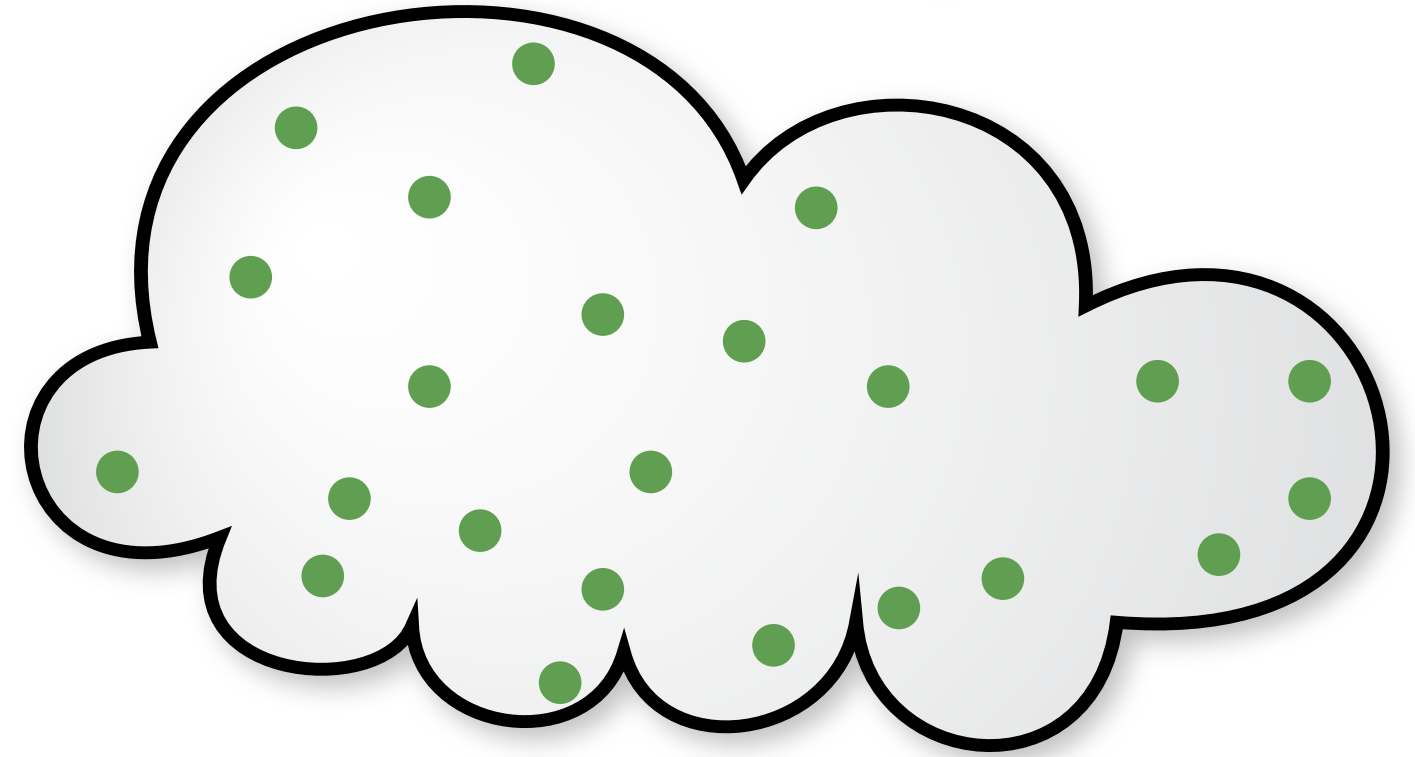
**Wojciech Jarosz**

**THURSDAY, 9 AUGUST 2:00 PM - 5:15 PM | Room 408B**



# So Far...

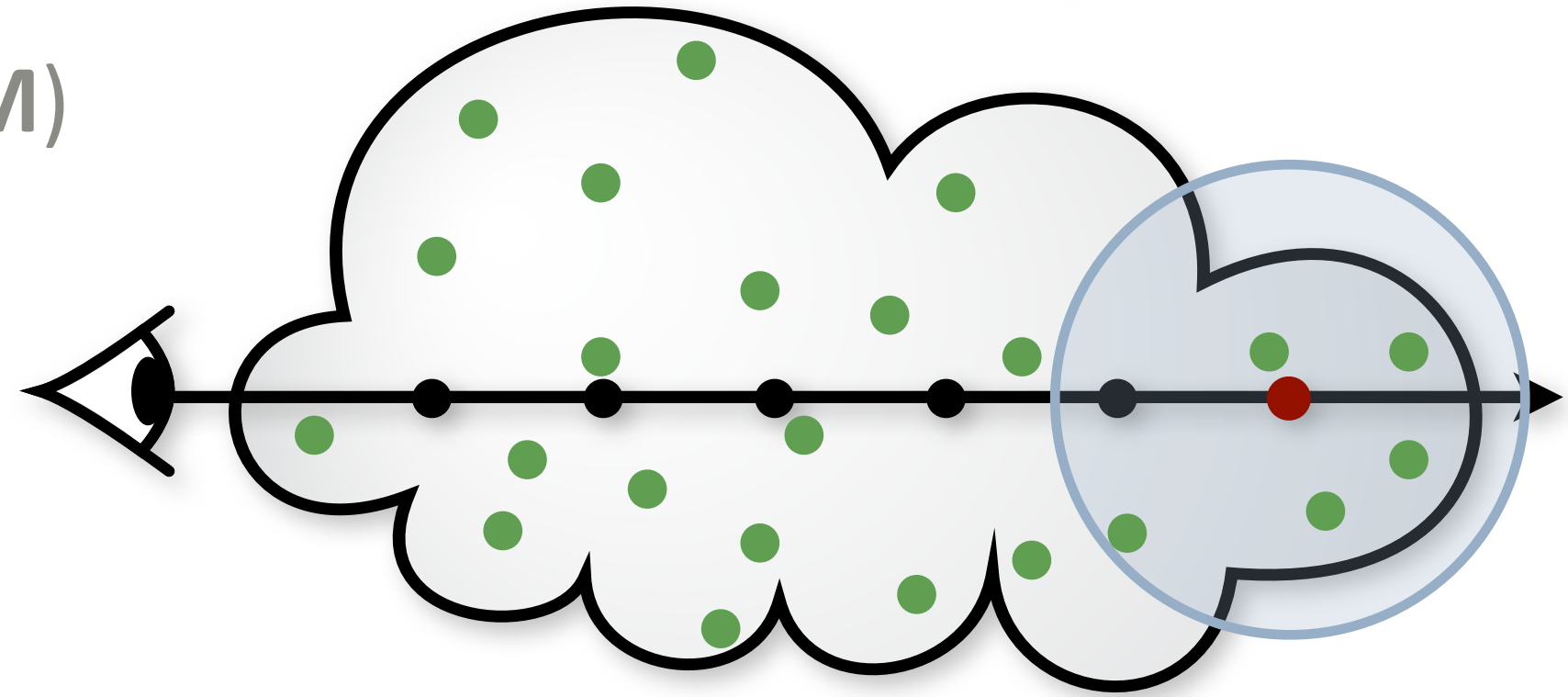
- Volumetric Photon Mapping (**VPM**)  
[Jensen & Christensen 98]
- The Beam Radiance Estimate (**BRE**)  
[Jarosz et al. 08]





# So Far...

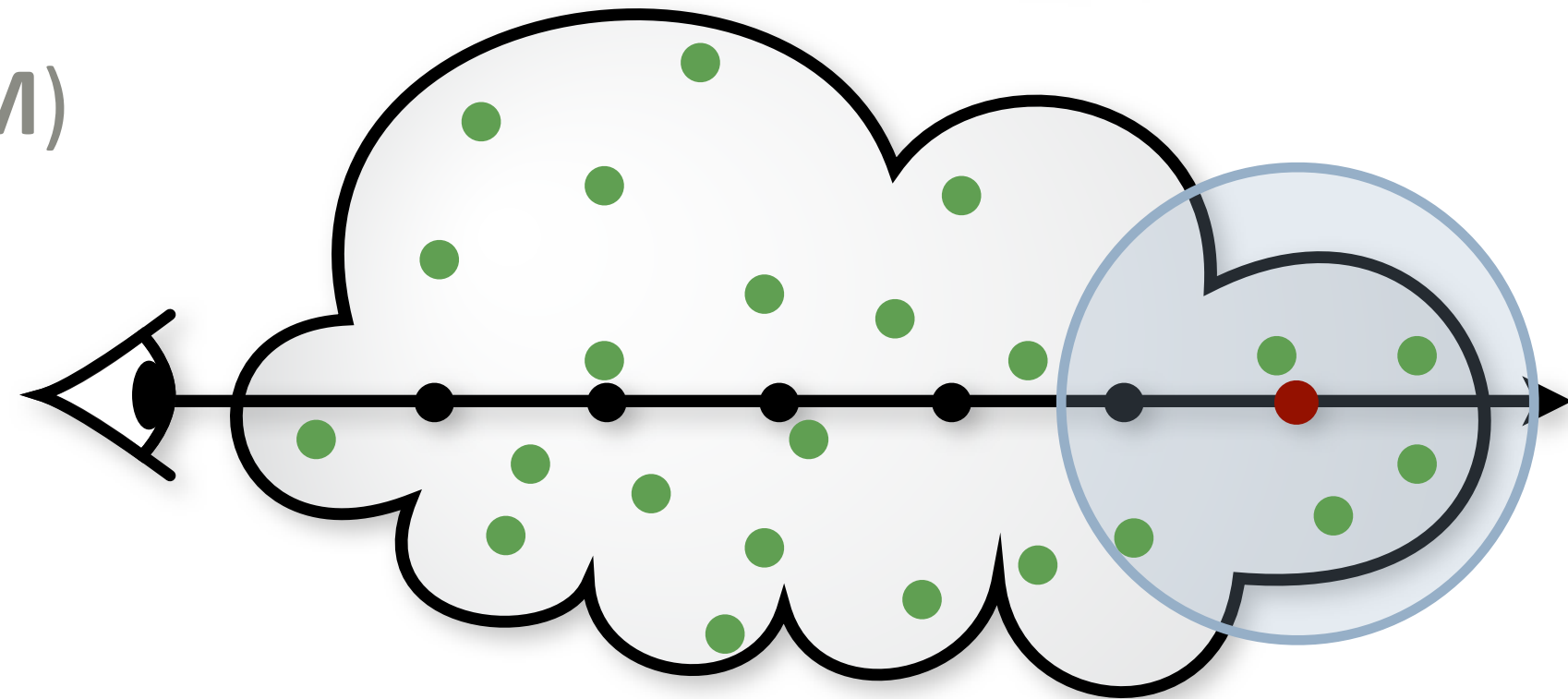
- Volumetric Photon Mapping (VPM)  
[Jensen & Christensen 98]
- The Beam Radiance Estimate (BRE)  
[Jarosz et al. 08]



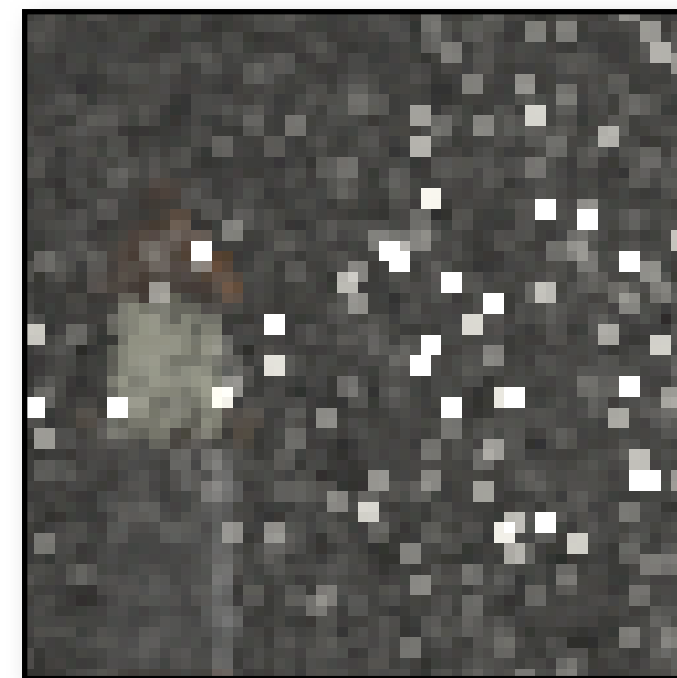


# So Far...

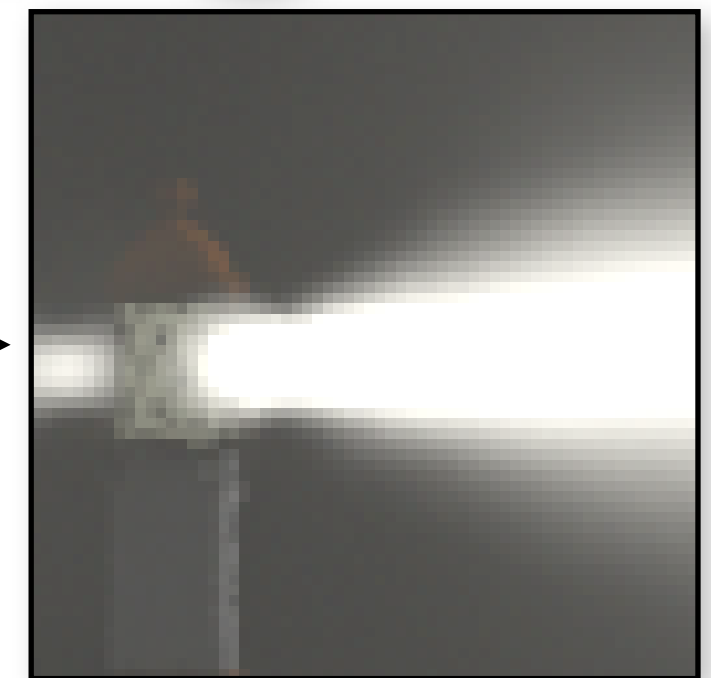
- Volumetric Photon Mapping (VPM)  
[Jensen & Christensen 98]



- The Beam Radiance Estimate (BRE)  
[Jarosz et al. 08]



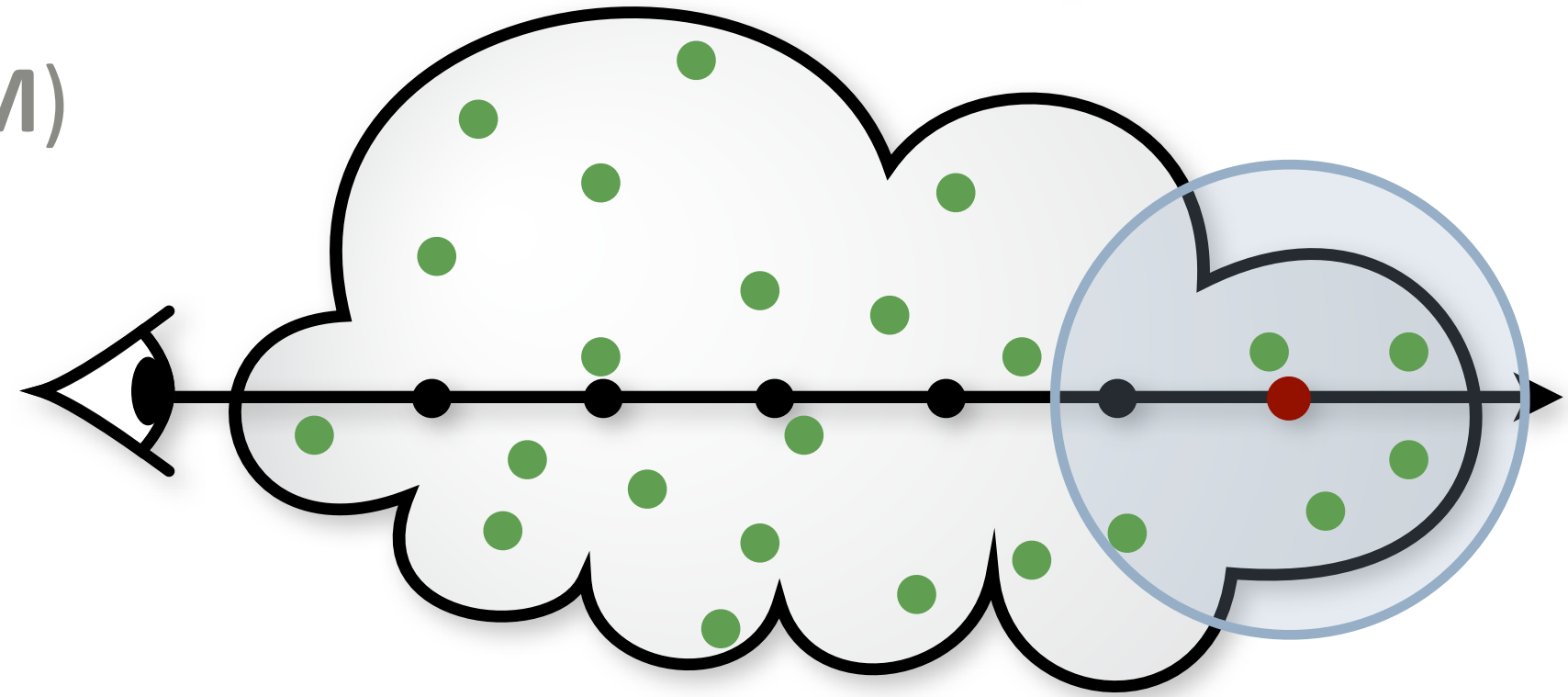
VPM



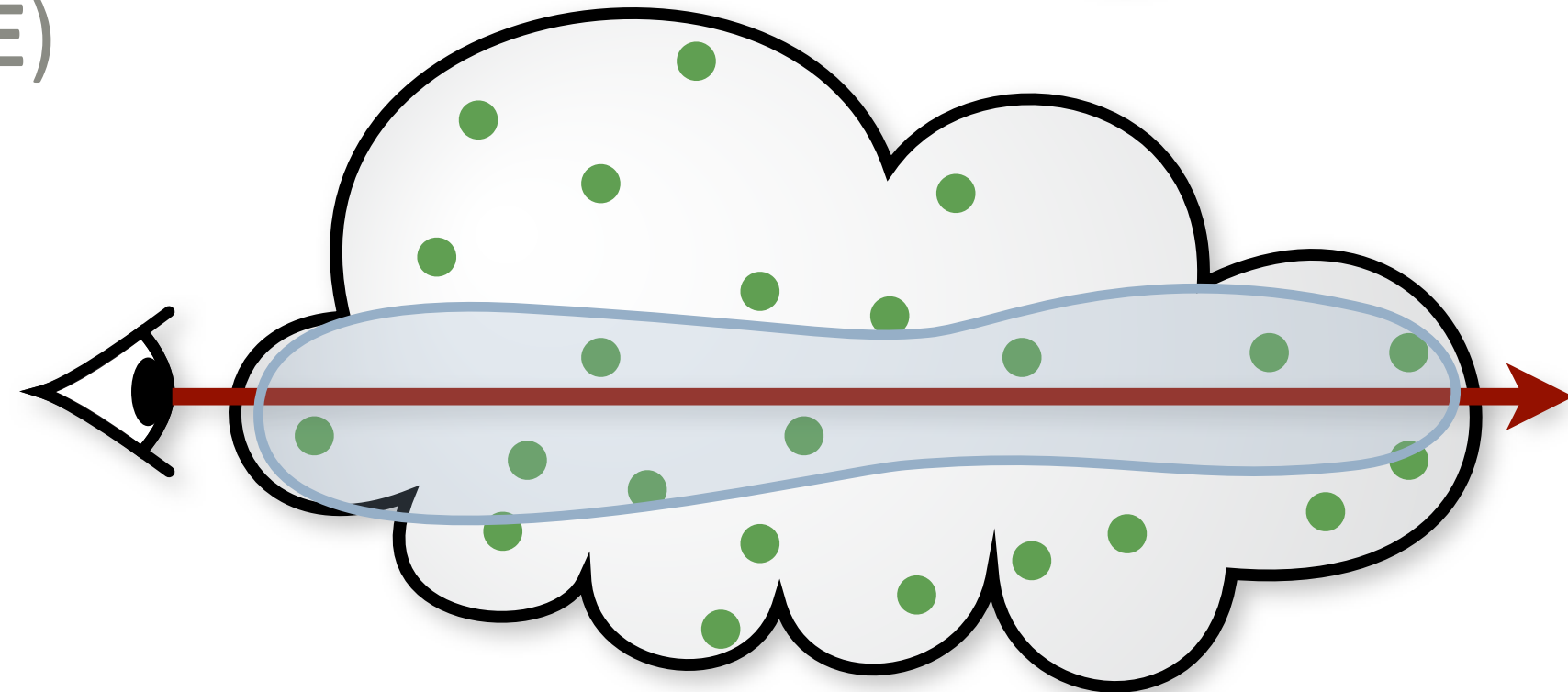
BRE

# So Far...

- Volumetric Photon Mapping (VPM)  
[Jensen & Christensen 98]

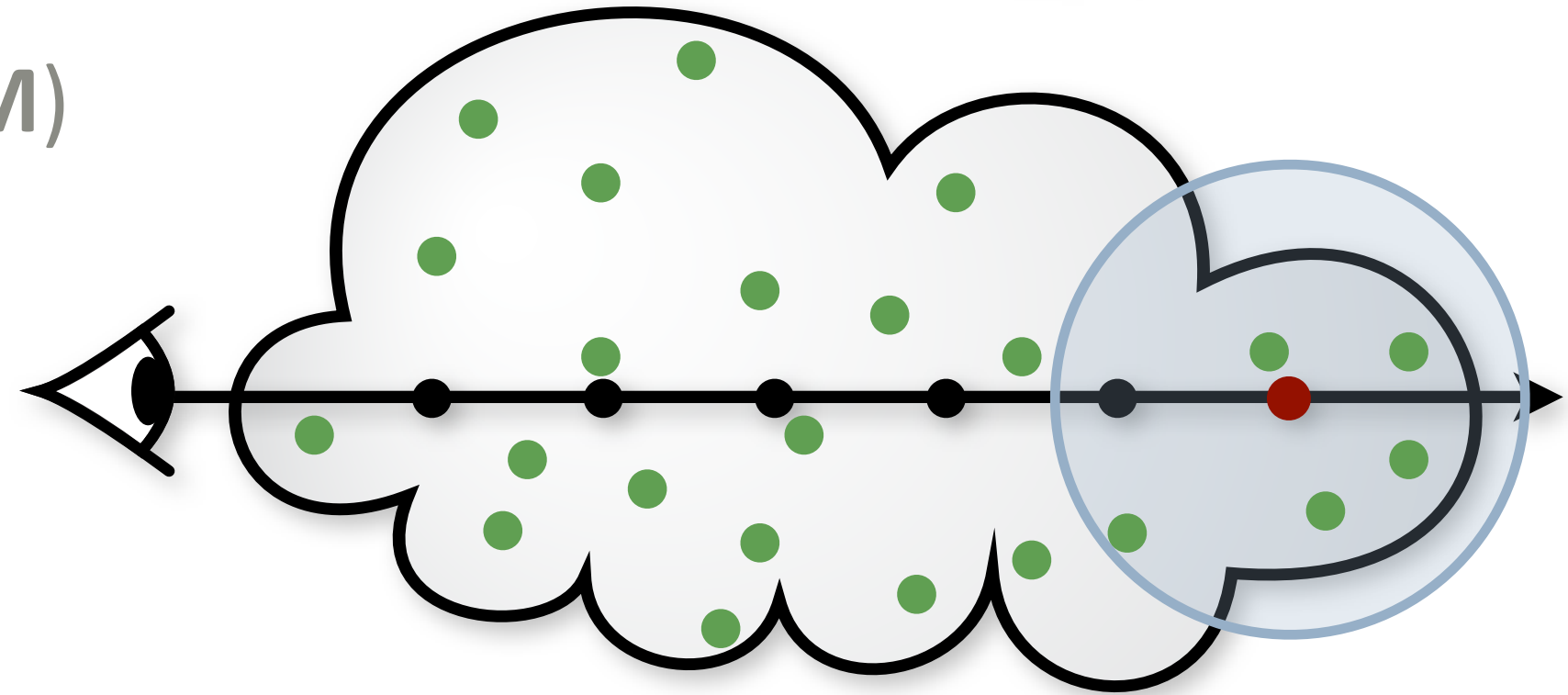
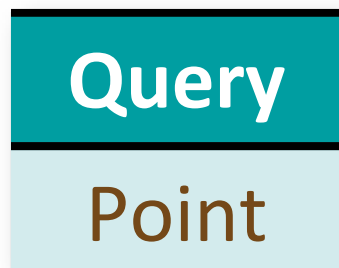


- The Beam Radiance Estimate (BRE)  
[Jarosz et al. 08]

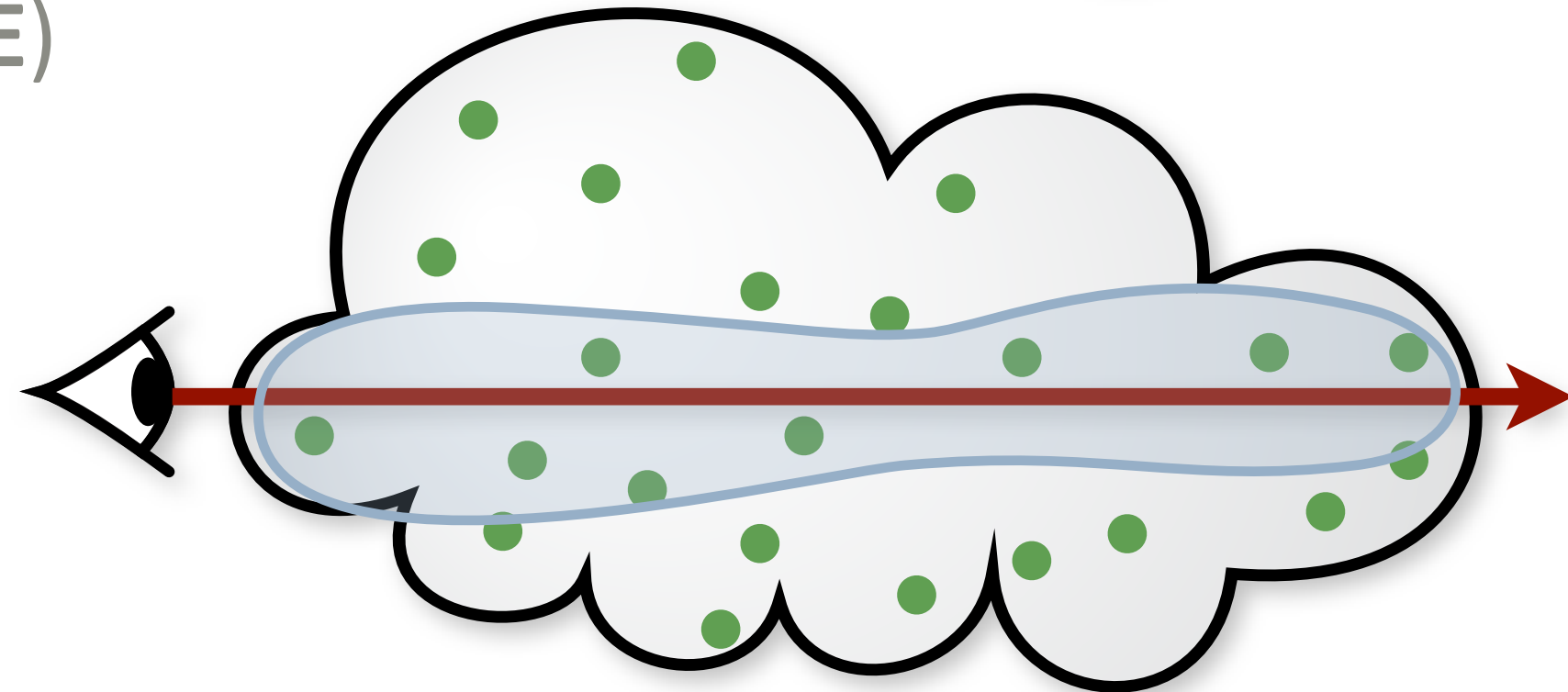


# So Far...

- Volumetric Photon Mapping (VPM)  
[Jensen & Christensen 98]



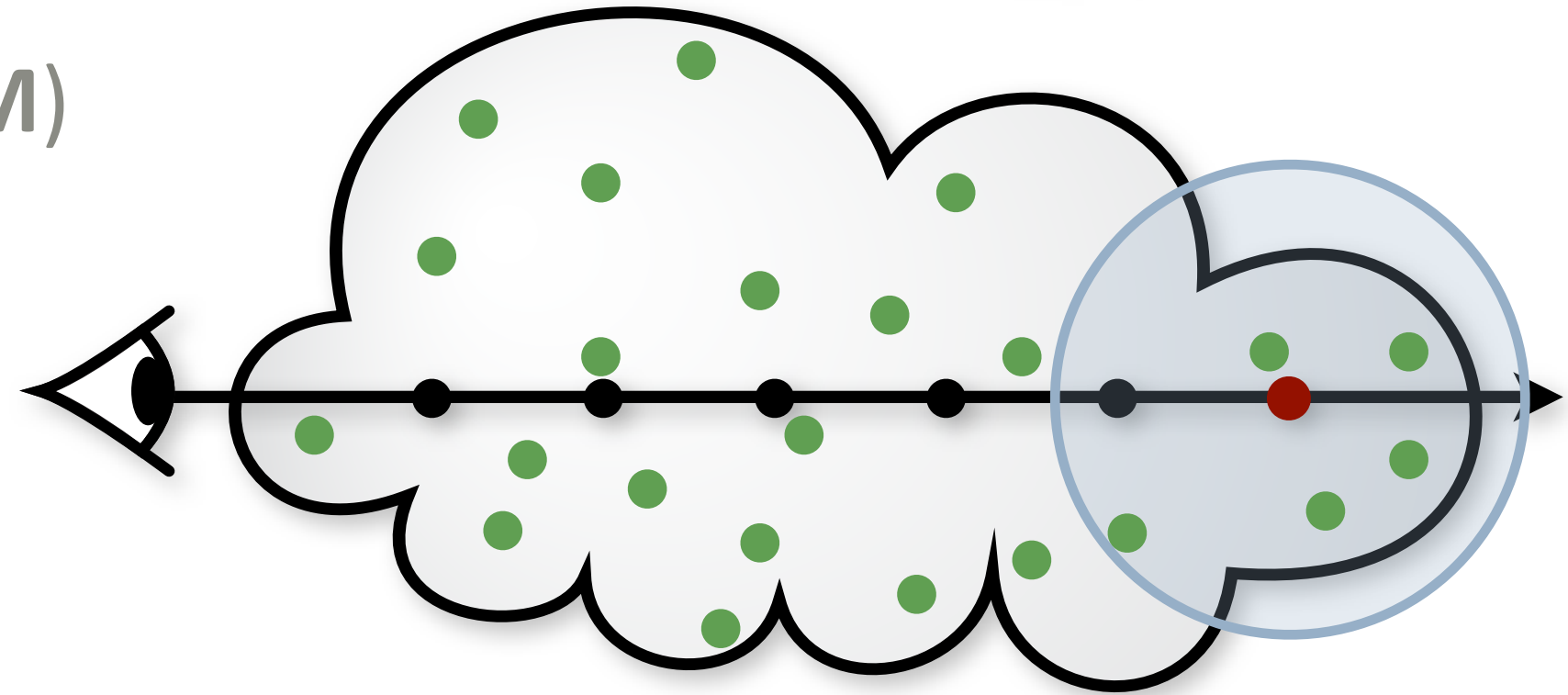
- The Beam Radiance Estimate (BRE)  
[Jarosz et al. 08]



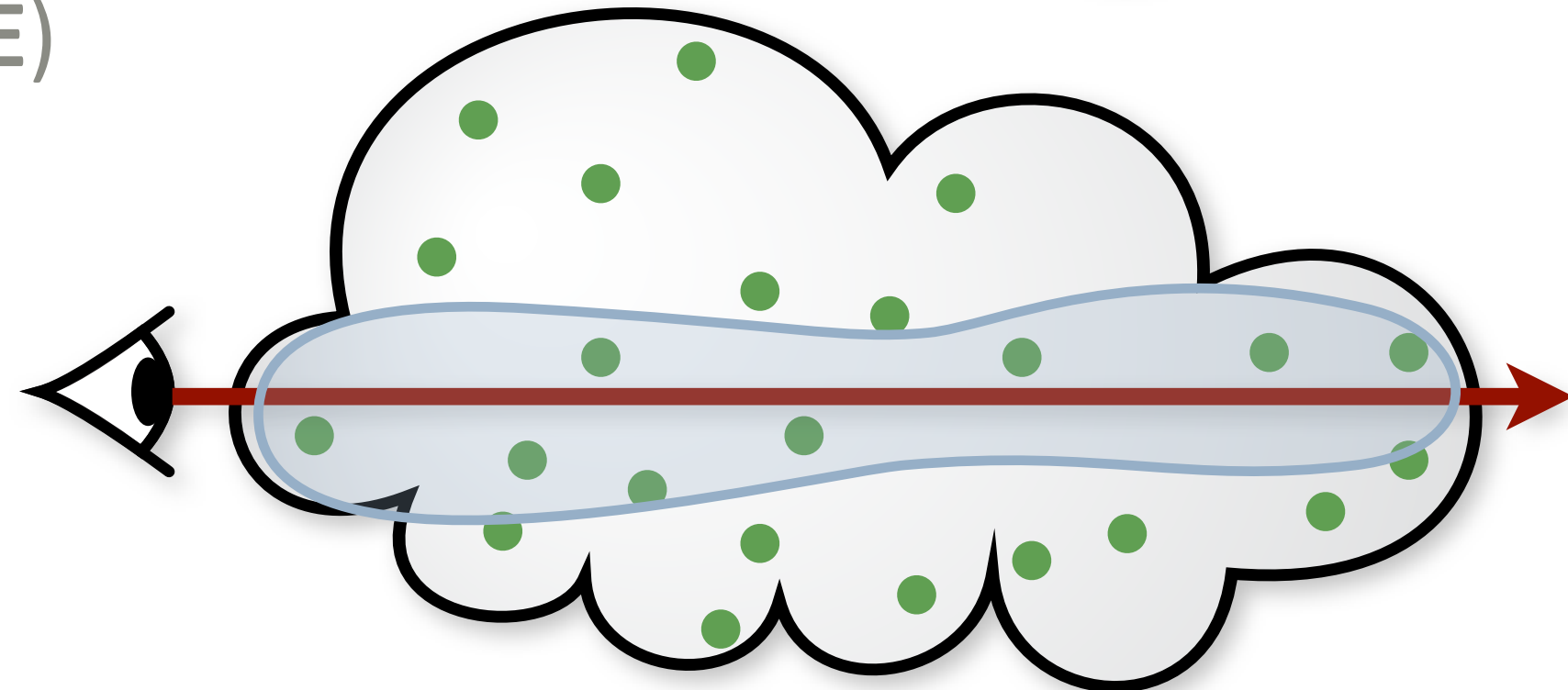
# So Far...

- Volumetric Photon Mapping (VPM)  
[Jensen & Christensen 98]

Query	x	Data
Point	x	Point



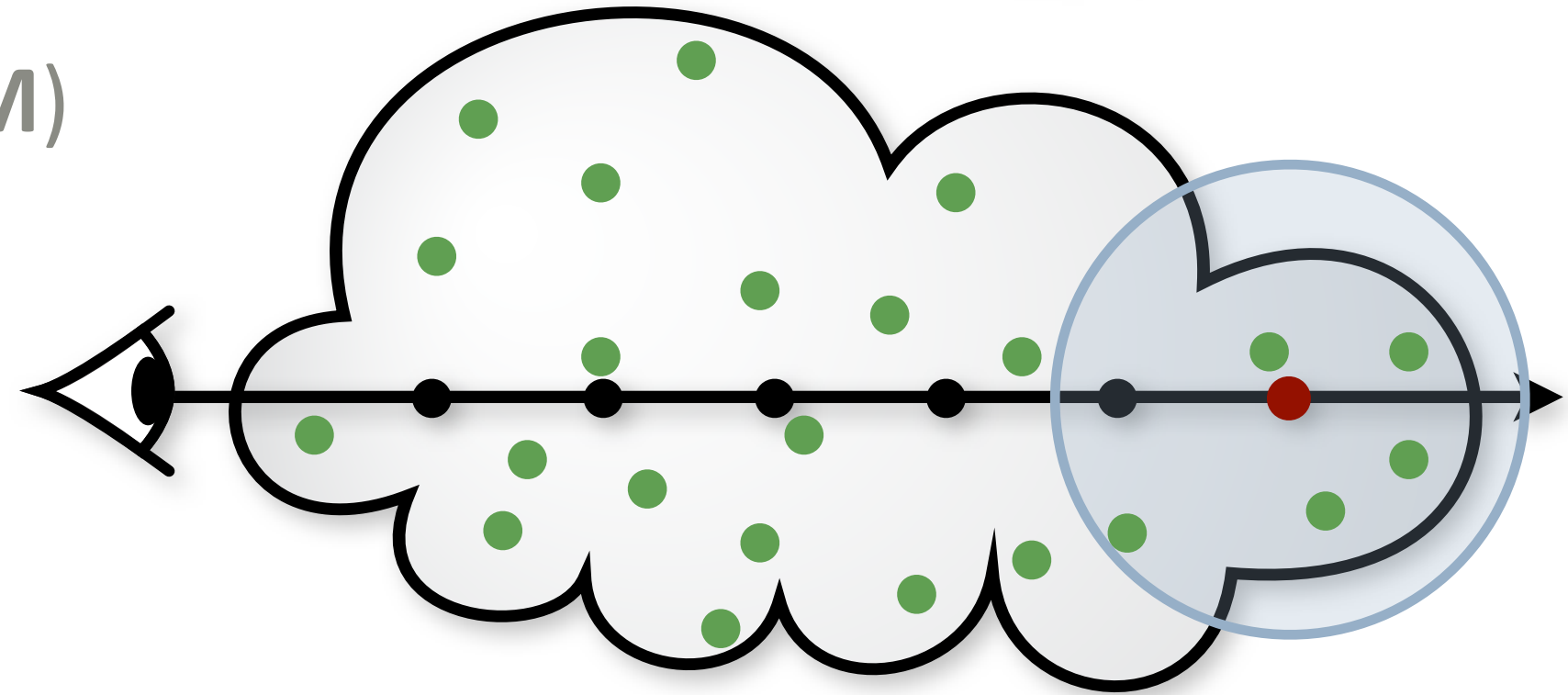
- The Beam Radiance Estimate (BRE)  
[Jarosz et al. 08]



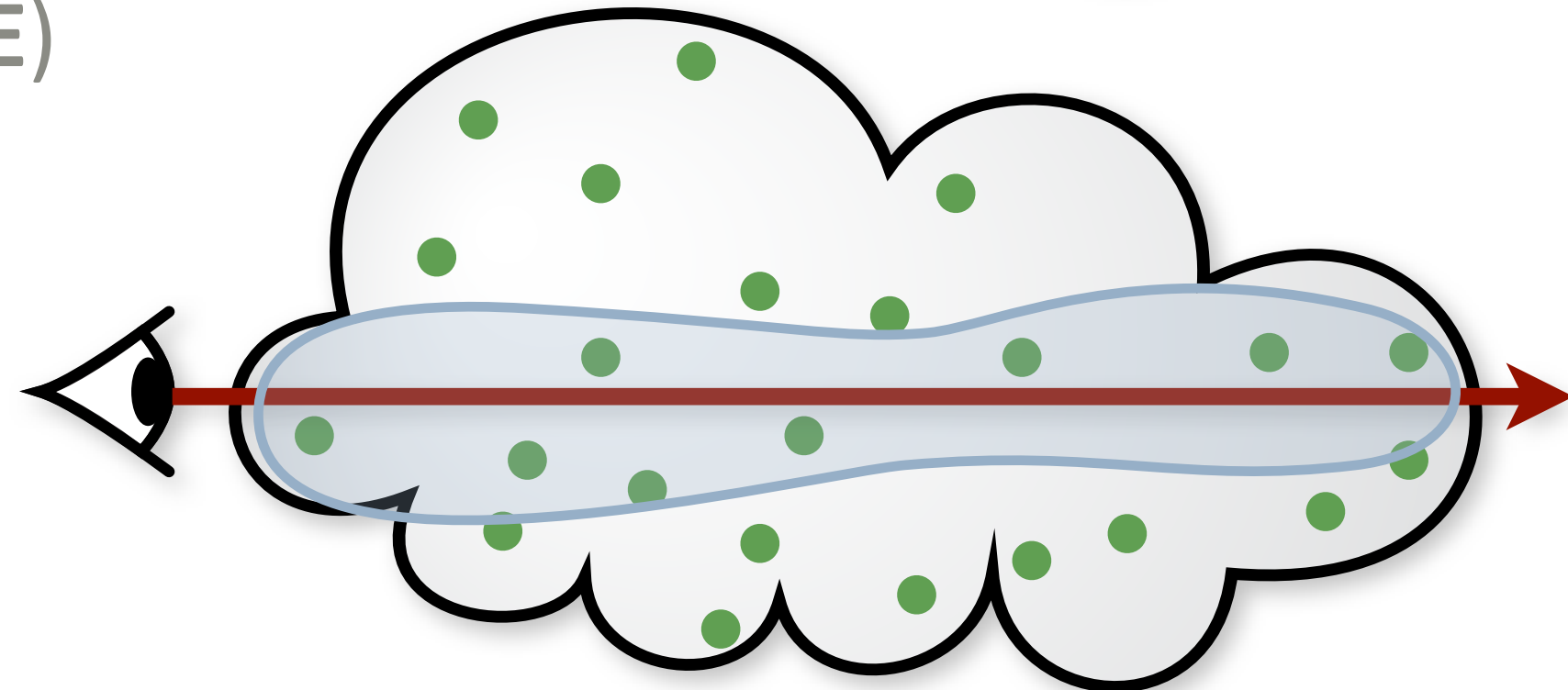
# So Far...

- Volumetric Photon Mapping (VPM)  
[Jensen & Christensen 98]

Query	x	Data	Blur
Point	x	Point	(3D)



- The Beam Radiance Estimate (BRE)  
[Jarosz et al. 08]

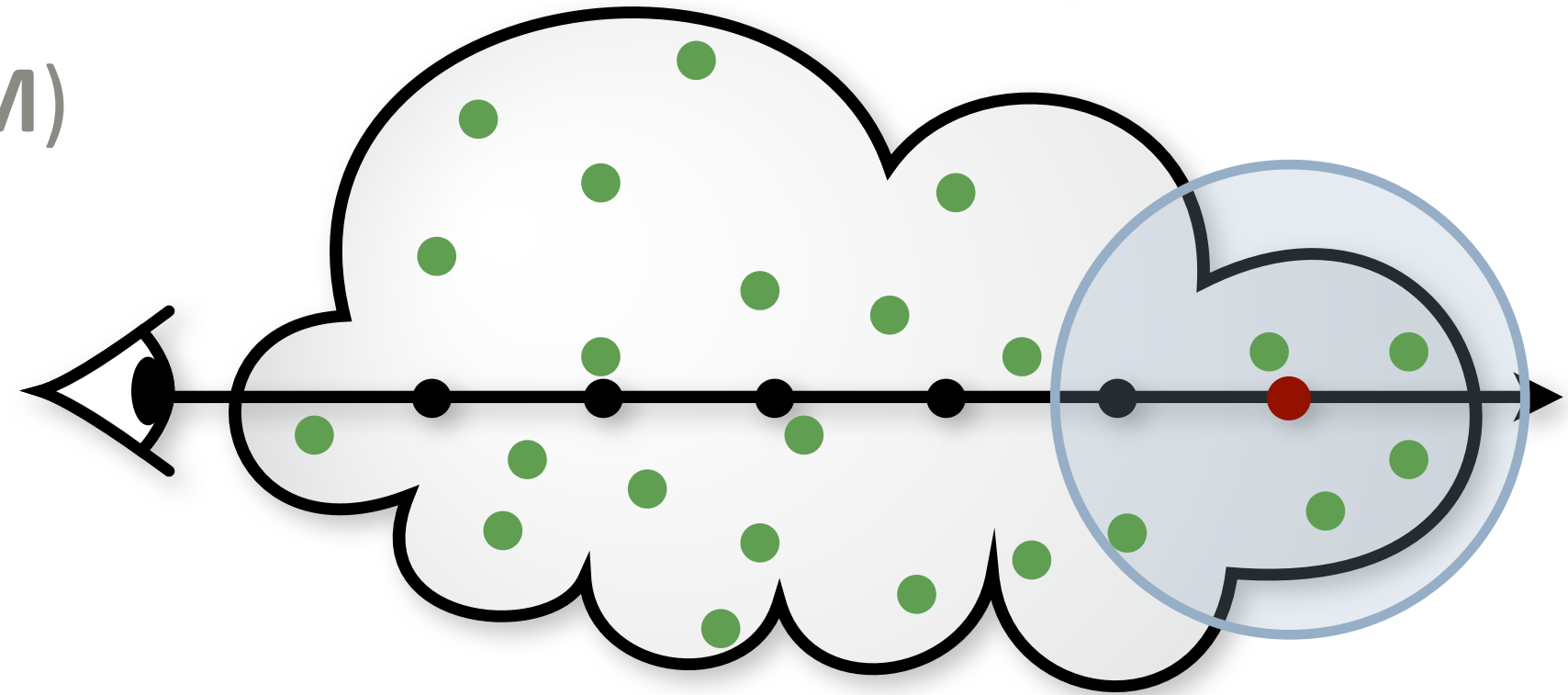




# So Far...

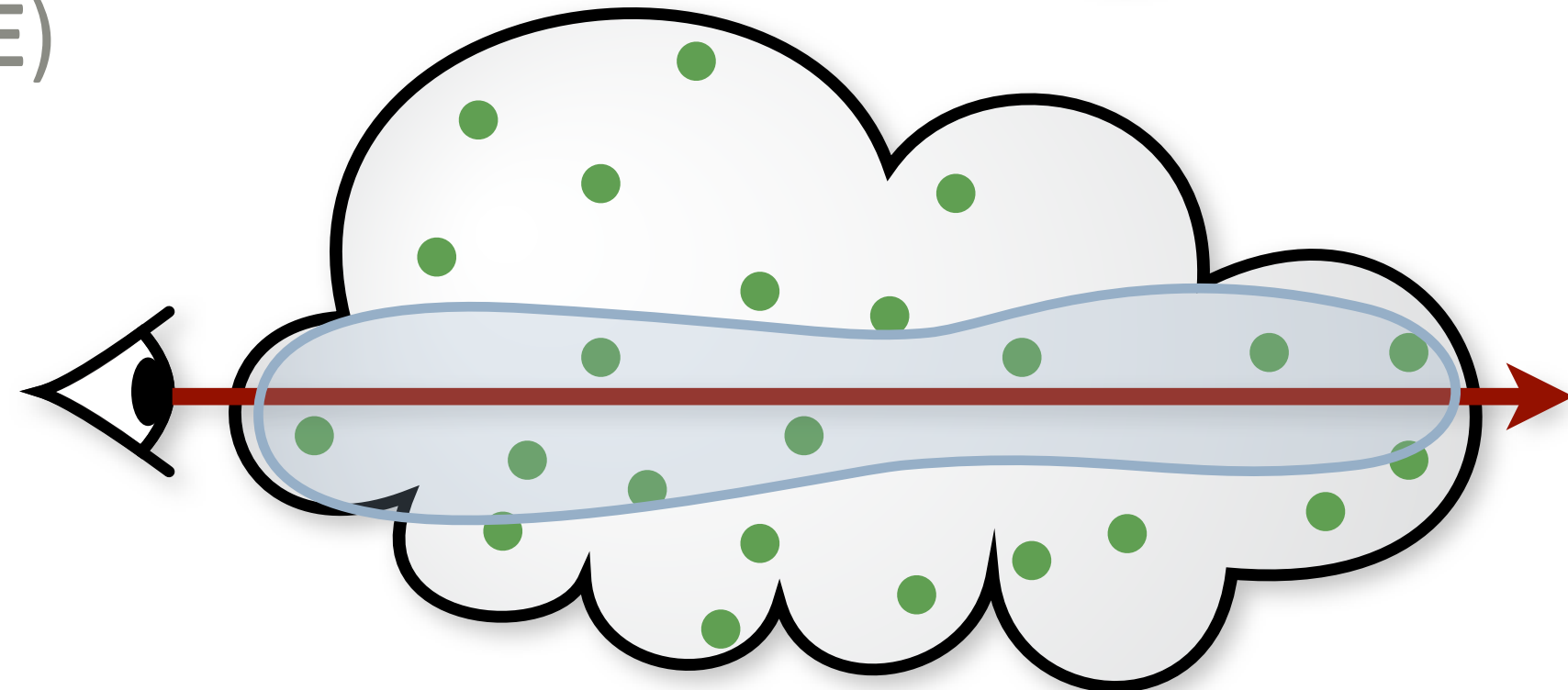
- Volumetric Photon Mapping (VPM)  
[Jensen & Christensen 98]

Query	x	Data	Blur
Point	x	Point	(3D)



- The Beam Radiance Estimate (BRE)  
[Jarosz et al. 08]

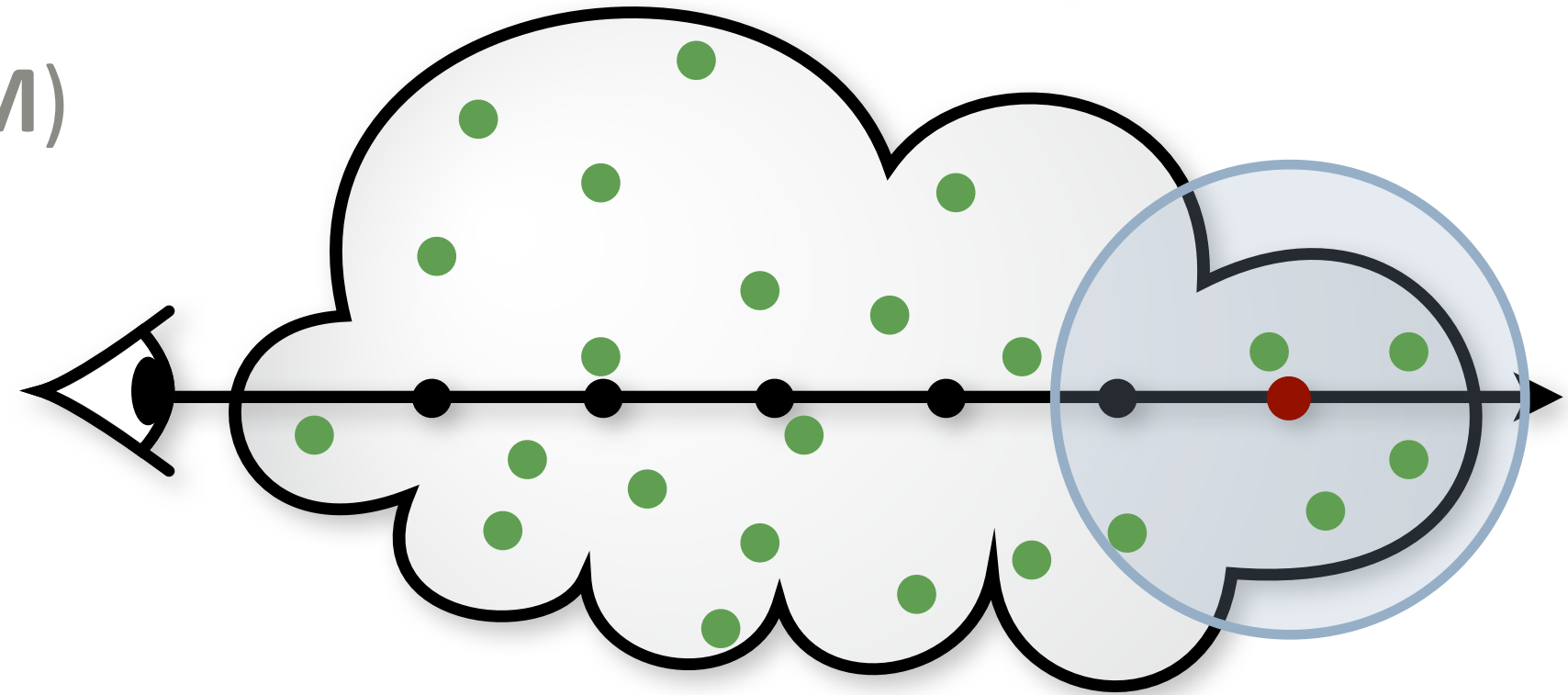
Query
Beam



# So Far...

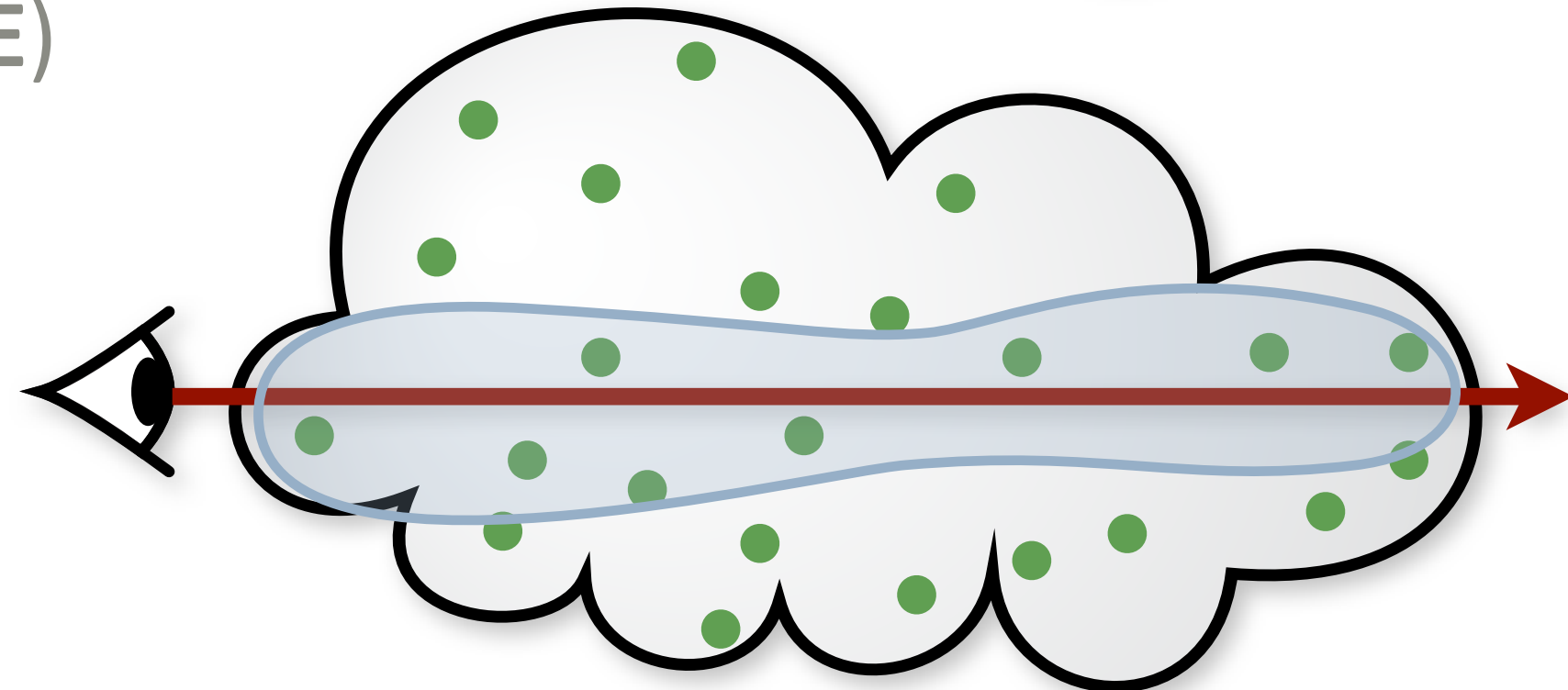
- Volumetric Photon Mapping (VPM)  
[Jensen & Christensen 98]

Query	x	Data	Blur
Point	x	Point	(3D)



- The Beam Radiance Estimate (BRE)  
[Jarosz et al. 08]

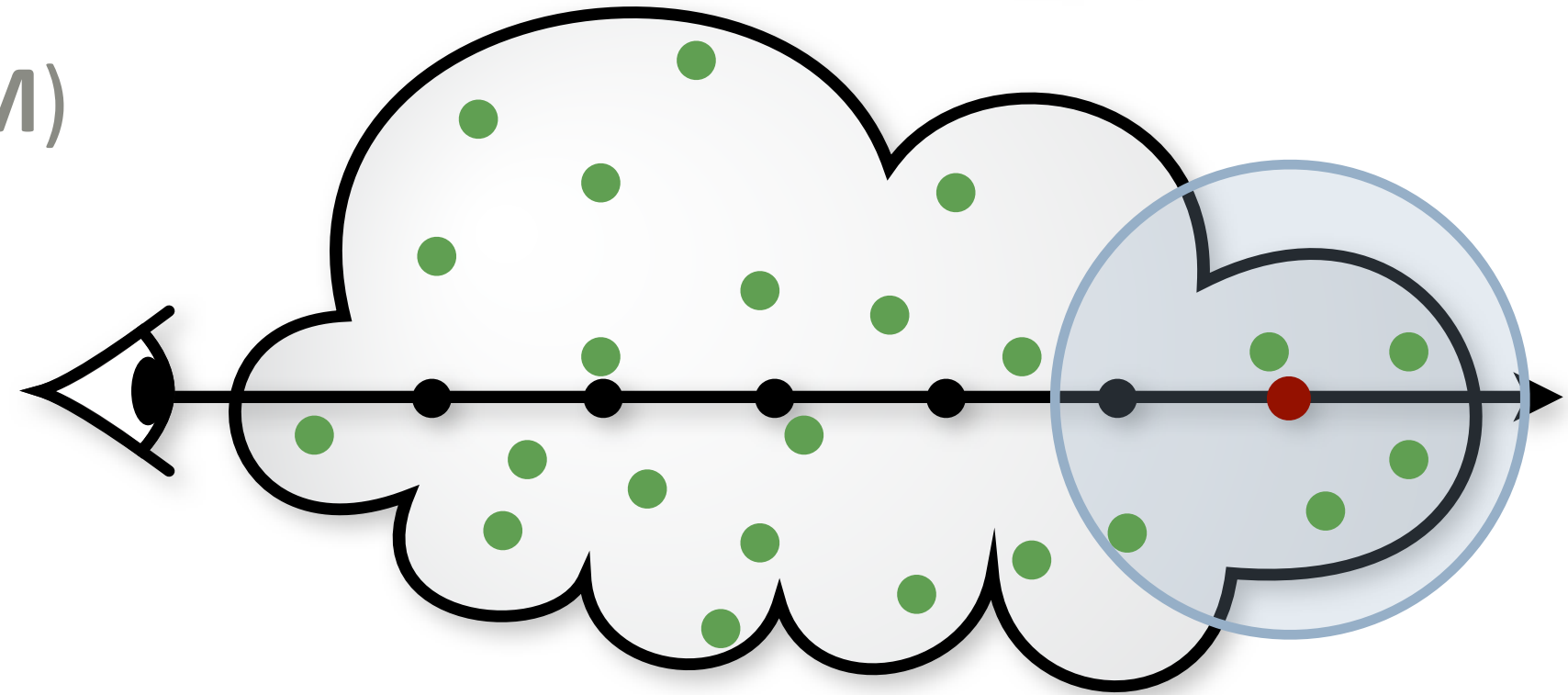
Query	x	Data
Beam	x	Point



# So Far...

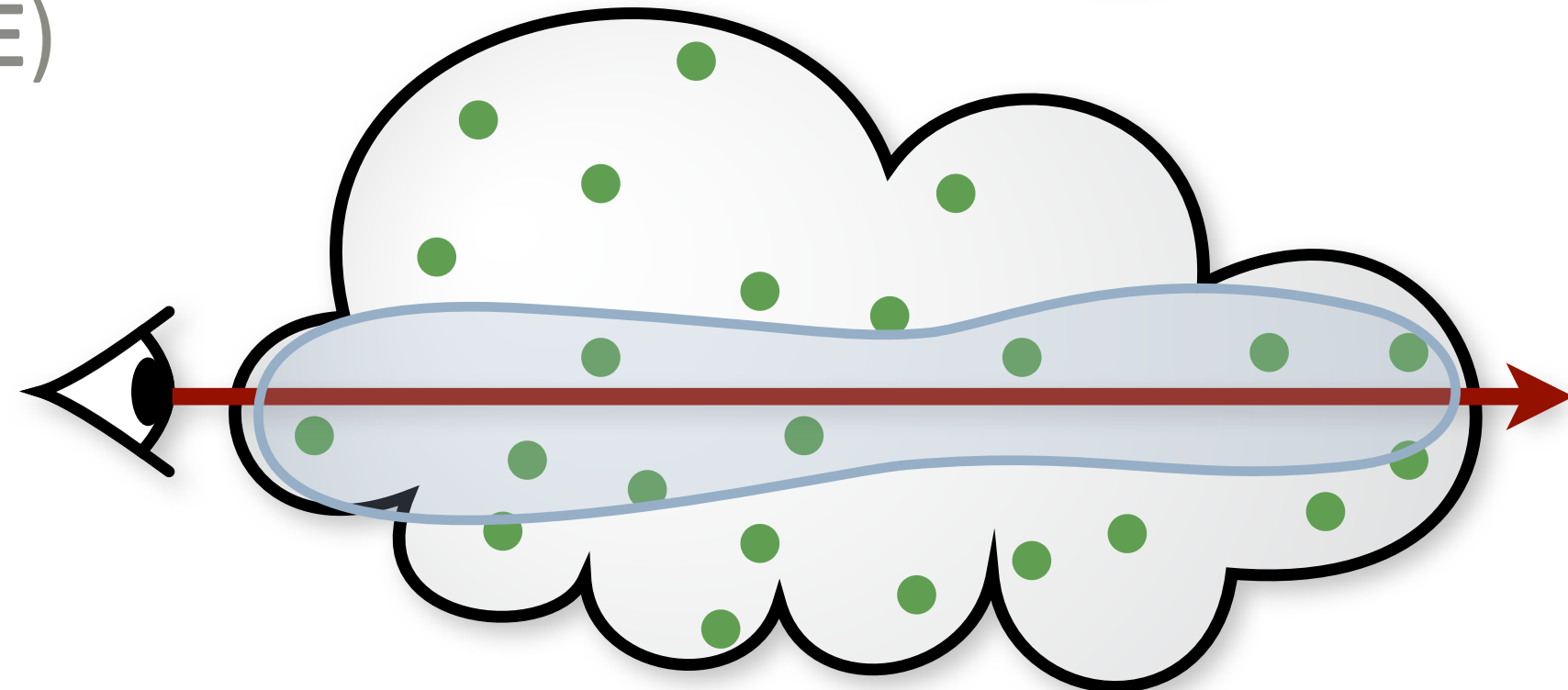
- Volumetric Photon Mapping (VPM)  
[Jensen & Christensen 98]

Query	x	Data	Blur
Point	x	Point	(3D)



- The Beam Radiance Estimate (BRE)  
[Jarosz et al. 08]

Query	x	Data	Blur
Beam	x	Point	(2D)





# So Far...

- Volumetric Photon Mapping (**VPM**)  
[Jensen & Christensen 98]

Query	x	Data	Blur
Point	x	Point	(3D)

- Beyond Photon Points:

- The Beam Radiance Estimate (**BRE**)  
[Jarosz et al. 08]

Query	x	Data	Blur
Beam	x	Point	(2D)



# So Far...

- Volumetric Photon Mapping (**VPM**)  
[Jensen & Christensen 98]

Query	x	Data	Blur
Point	x	Point	(3D)

- Beyond Photon Points:

Query
Point/Beam

- The Beam Radiance Estimate (**BRE**)  
[Jarosz et al. 08]

Query	x	Data	Blur
Beam	x	Point	(2D)



# So Far...

- Volumetric Photon Mapping (**VPM**)  
[Jensen & Christensen 98]

Query	x	Data	Blur
Point	x	Point	(3D)

- Beyond Photon Points:

Query	Data
Point/Beam	Point/Beam

- The Beam Radiance Estimate (**BRE**)  
[Jarosz et al. 08]

Query	x	Data	Blur
Beam	x	Point	(2D)



# So Far...

- Volumetric Photon Mapping (**VPM**)  
[Jensen & Christensen 98]

Query	x	Data	Blur
Point	x	Point	(3D)

- Beyond Photon Points:

Query	Data	Blur
Point/Beam	Point/Beam	1D/2D/3D

- The Beam Radiance Estimate (**BRE**)  
[Jarosz et al. 08]

Query	x	Data	Blur
Beam	x	Point	(2D)



# Density Estimator Options

Query	x	Data	Blur
Point	x	Point	(3D)
Beam	x	Point	(2D)



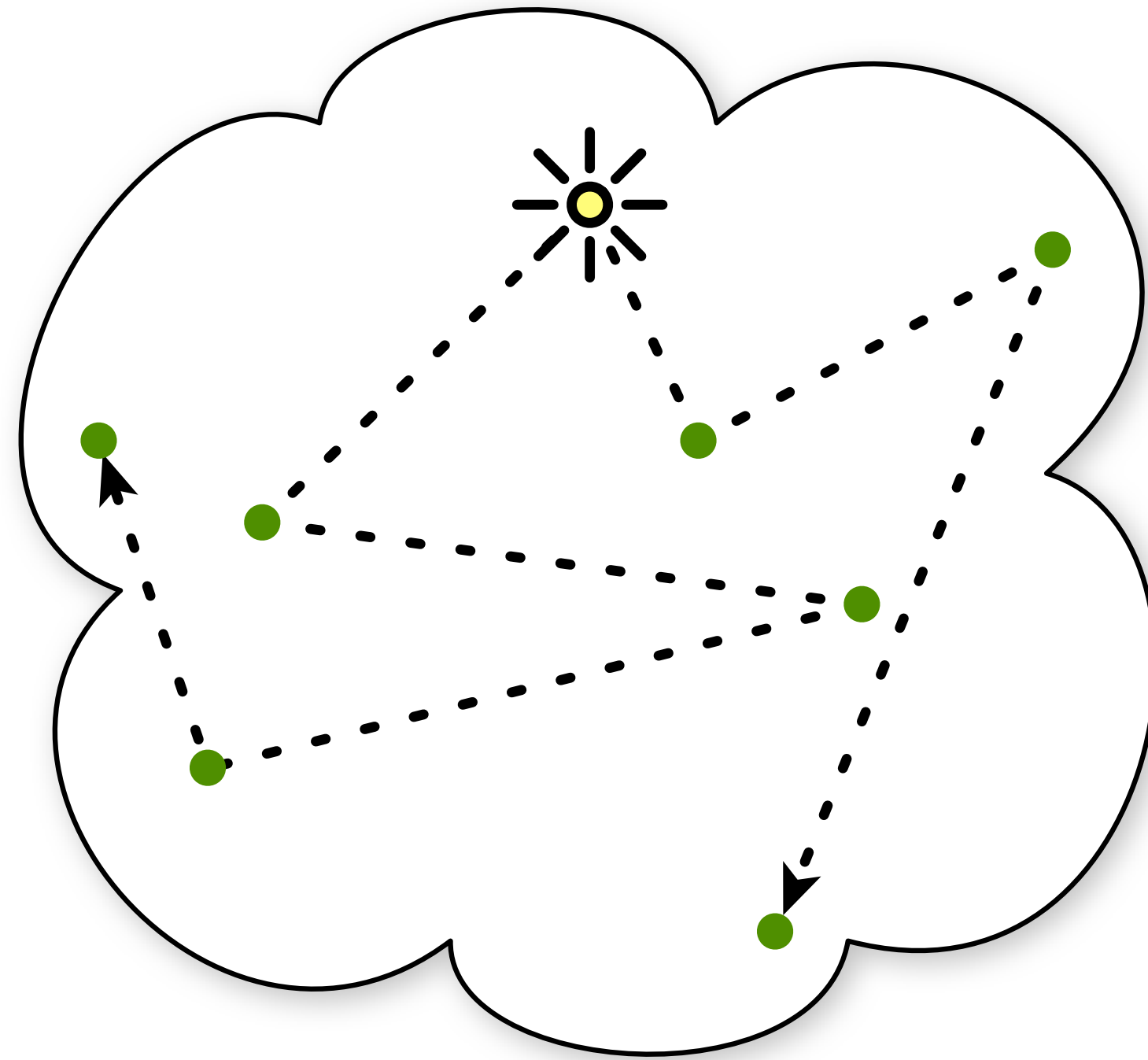


# Density Estimator Options

Query	x	Data	Blur
Point	x	Point	(3D)
Beam	x	Point	(2D)
<b>Beam</b>	<b>x</b>	<b>Point</b>	<b>(3D)</b>
<b>Point</b>	<b>x</b>	<b>Beam</b>	<b>(3D)</b>
<b>Point</b>	<b>x</b>	<b>Beam</b>	<b>(2D)</b>
<b>Beam</b>	<b>x</b>	<b>Beam</b>	<b>(3D)</b>
<b>Beam</b>	<b>x</b>	<b>Beam</b>	<b>(2D)<sub>1</sub></b>
<b>Beam</b>	<b>x</b>	<b>Beam</b>	<b>(2D)<sub>2</sub></b>
<b>Beam</b>	<b>x</b>	<b>Beam</b>	<b>(1D)</b>



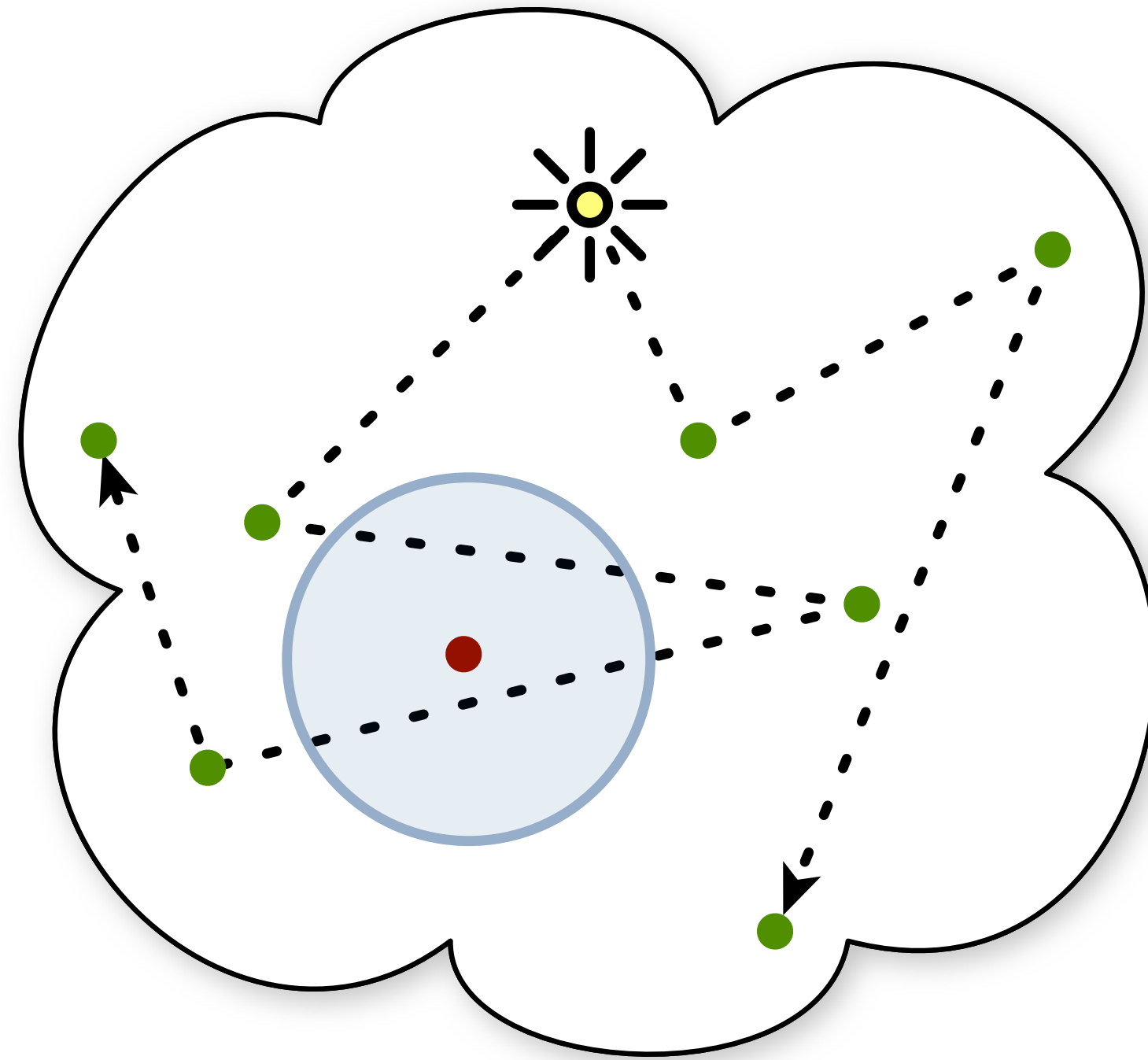
# Volumetric Photon Mapping



Photon Points



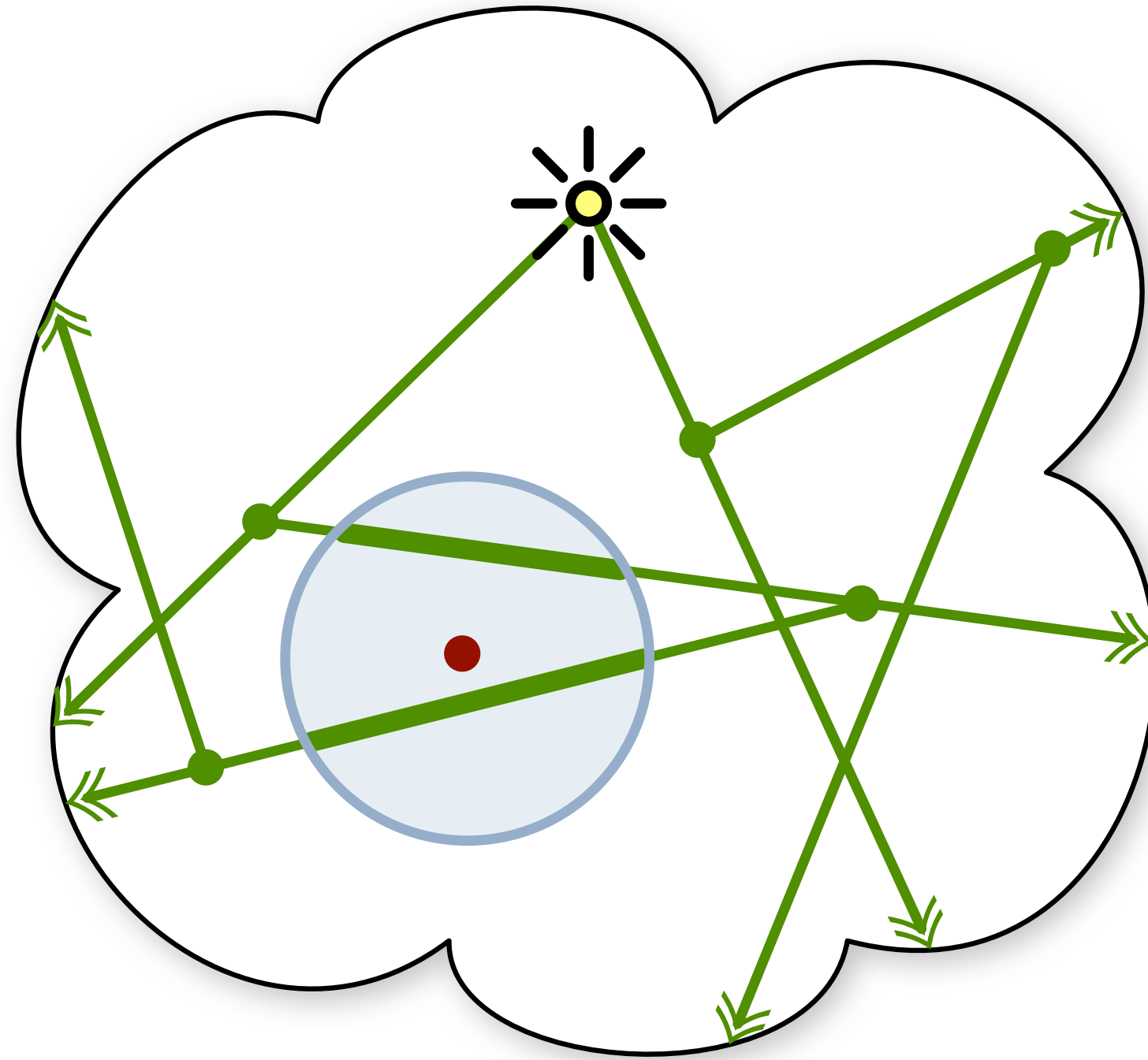
# Volumetric Photon Mapping



Photon Points

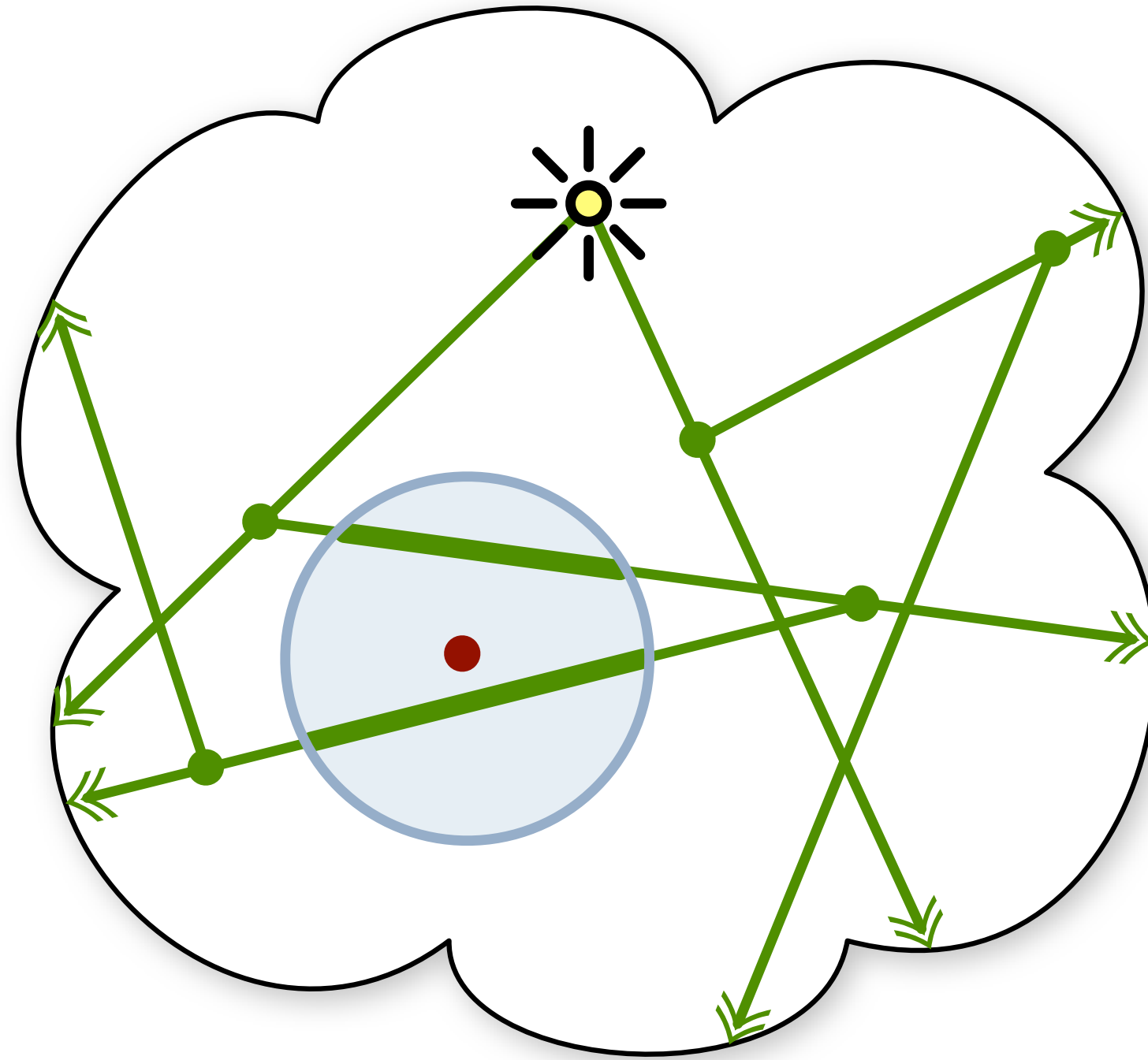


# Volumetric Photon Mapping





# Volumetric Photon Mapping



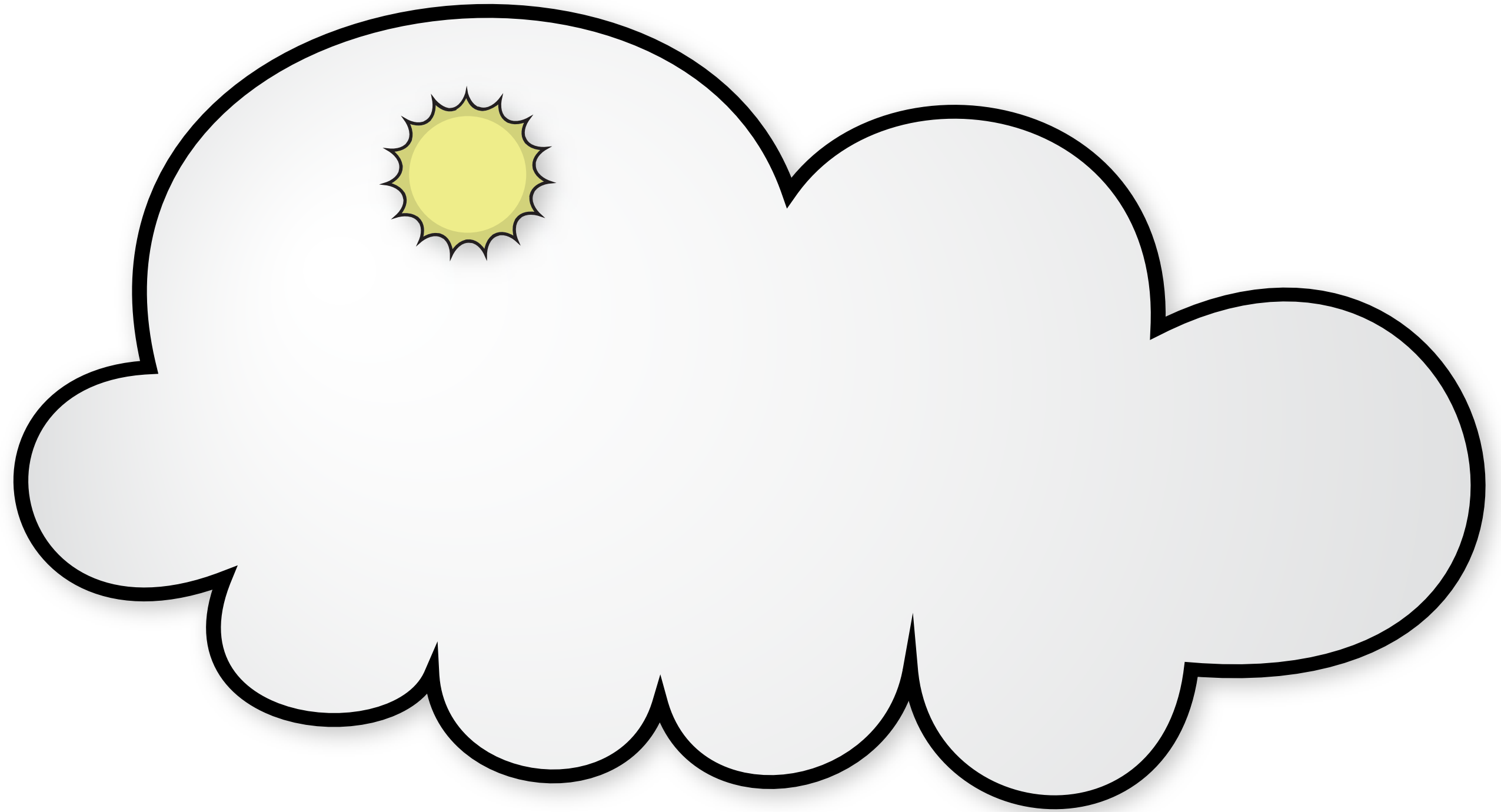
Photon Beams



# Photon Beams



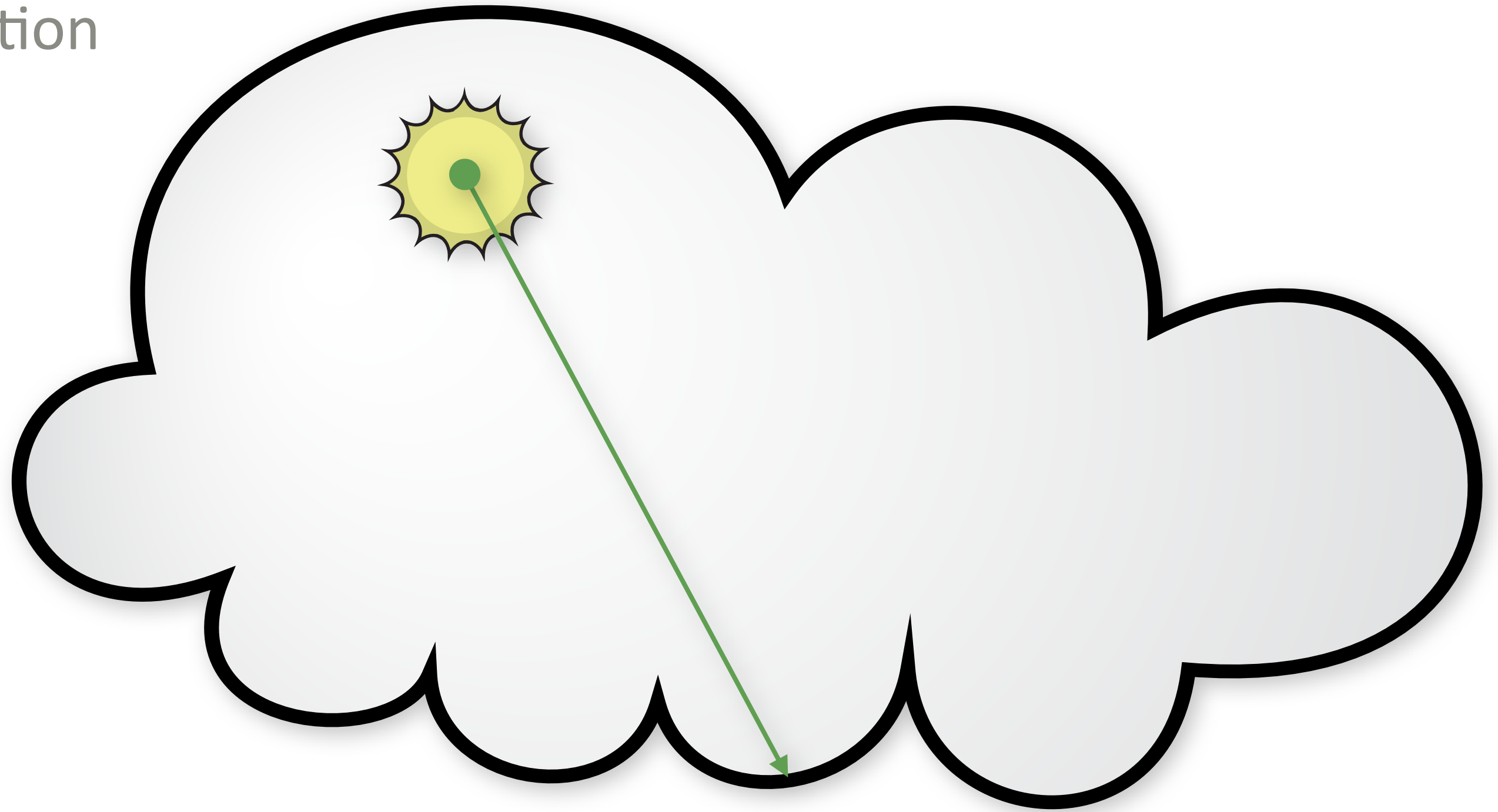
# Traditional Photon Tracing





# Traditional Photon Tracing

1) choose direction

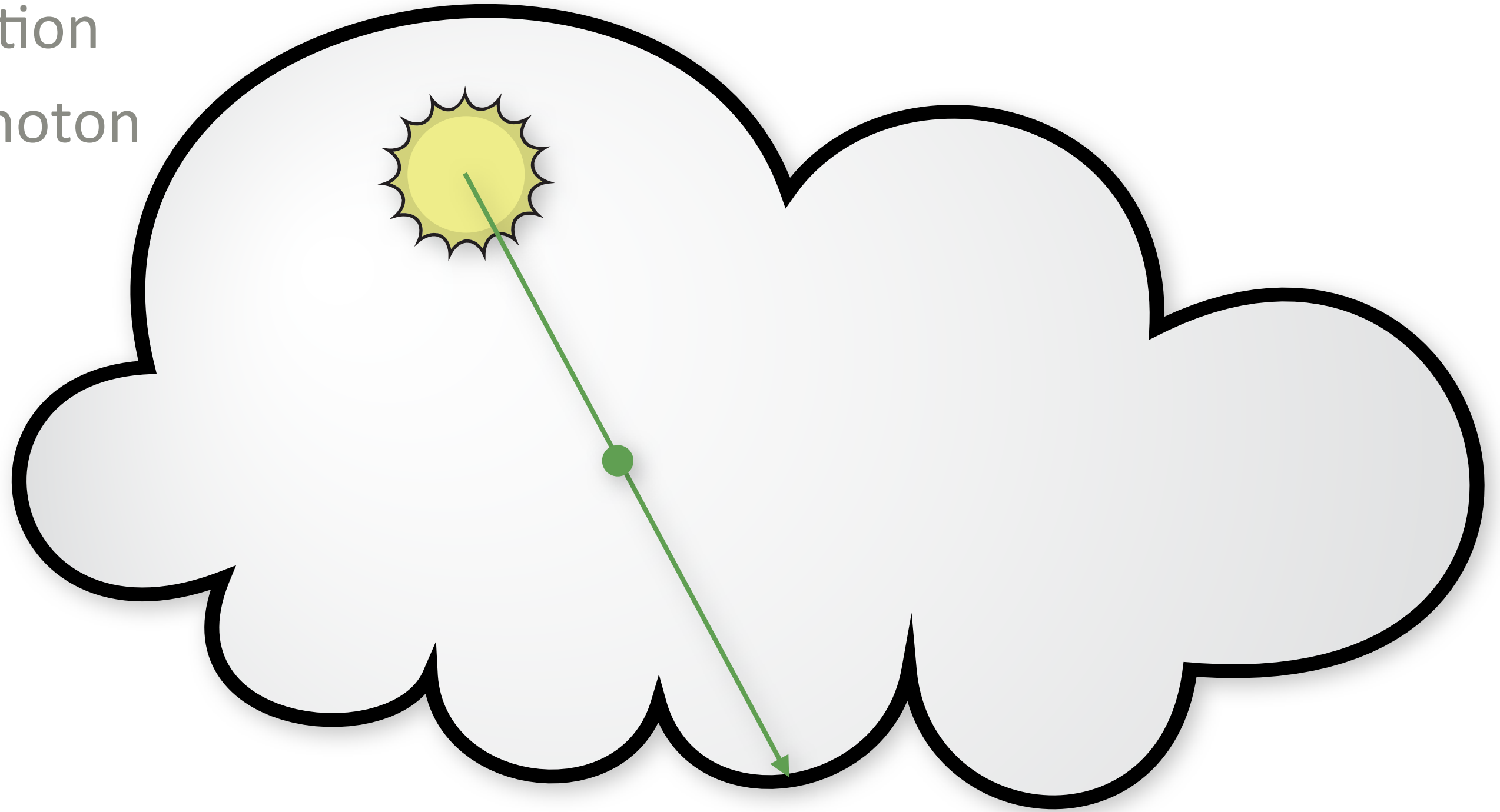






# Traditional Photon Tracing

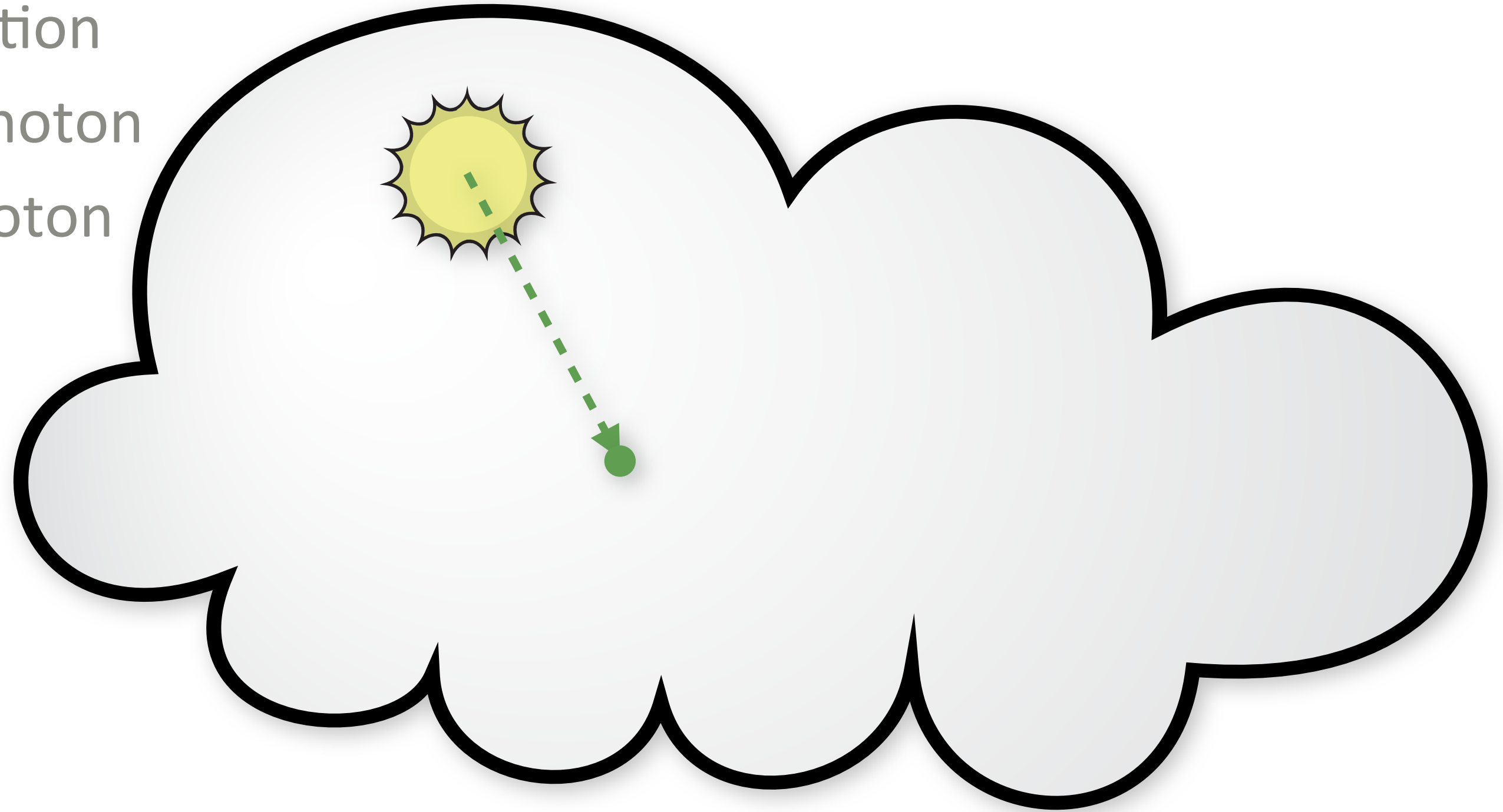
- 1) choose direction
- 2) propagate photon





# Traditional Photon Tracing

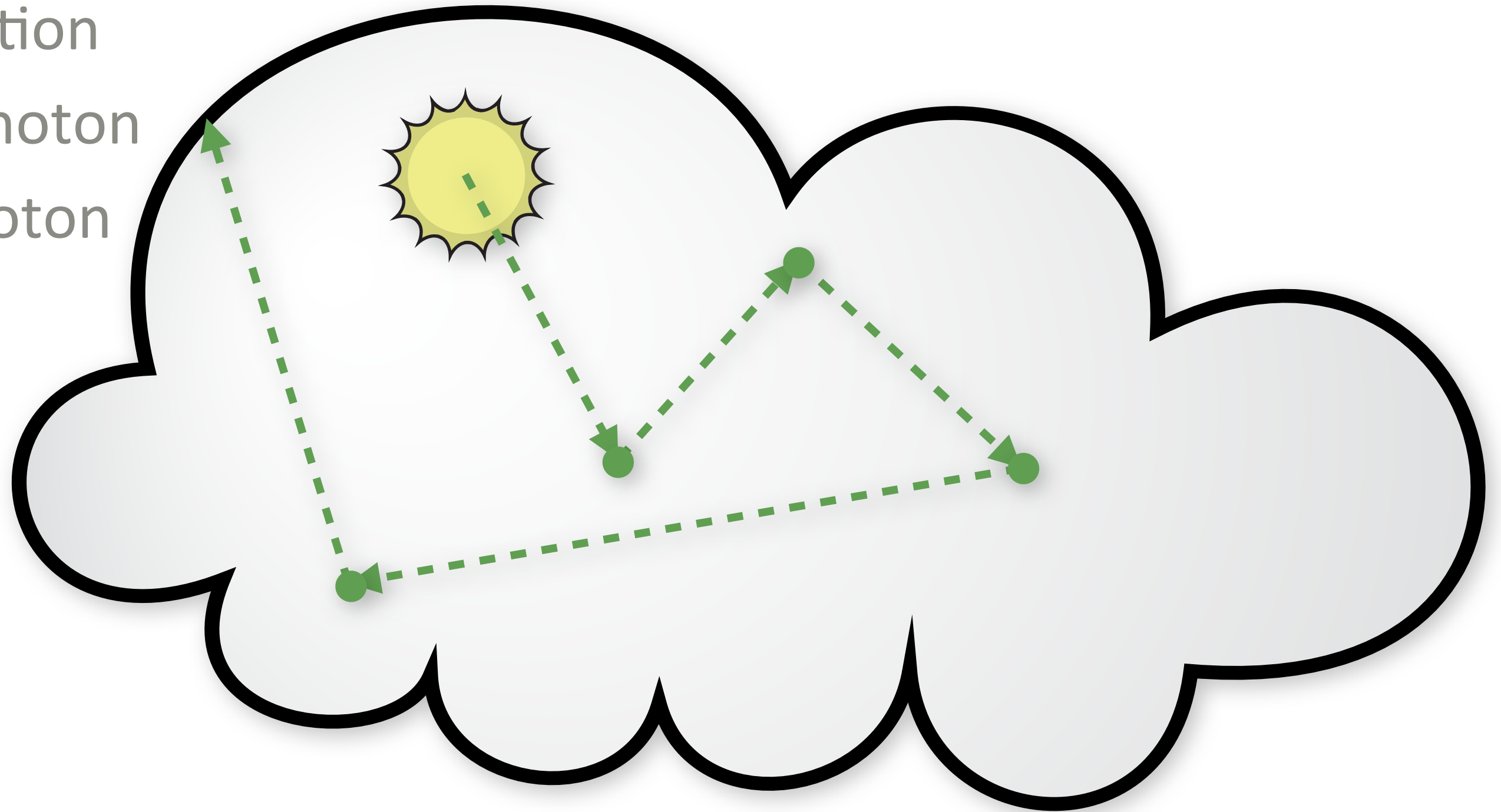
- 1) choose direction
- 2) propagate photon
- 3) deposit a photon





# Traditional Photon Tracing

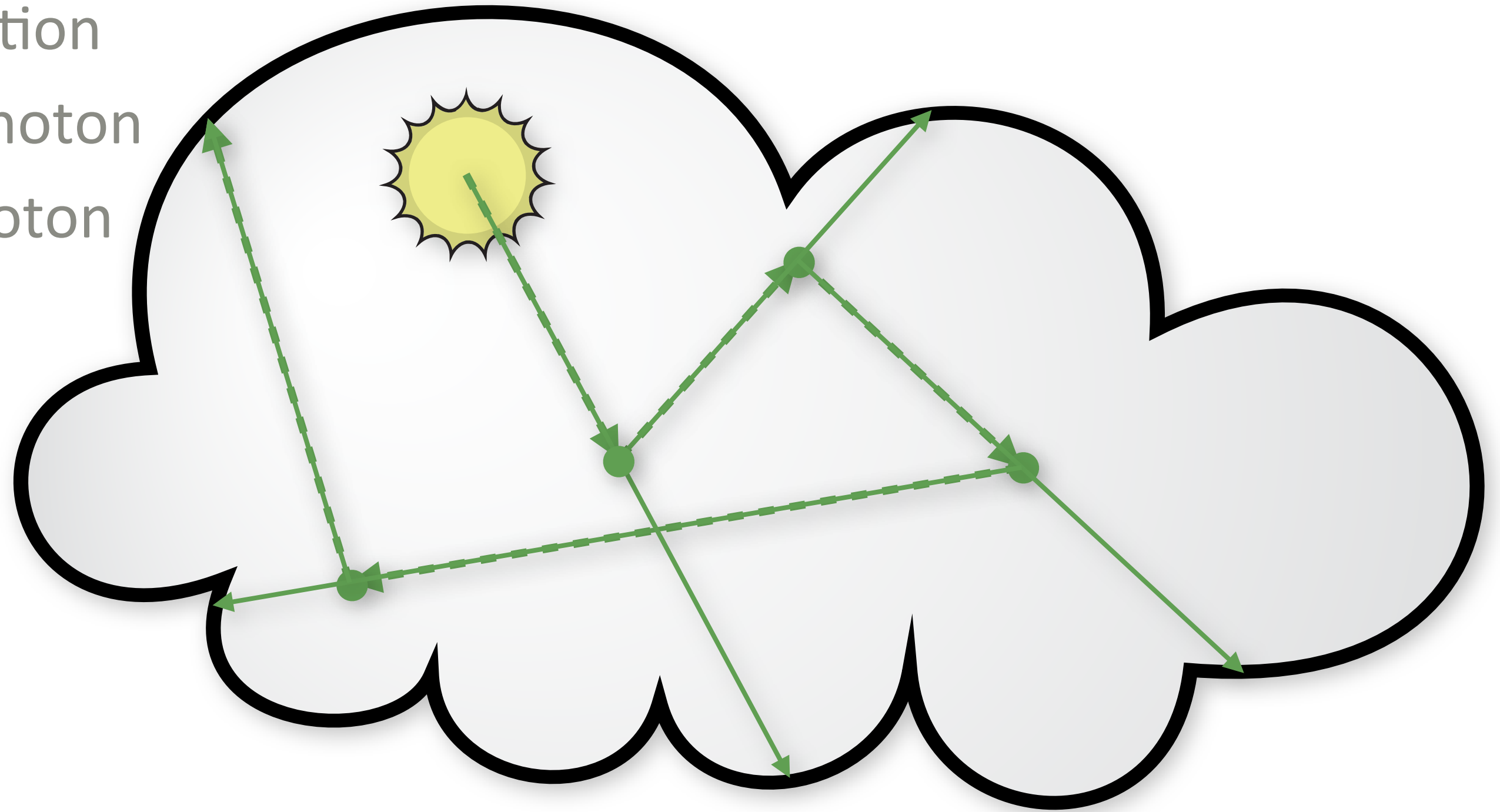
- 1) choose direction
- 2) propagate photon
- 3) deposit a photon
- 4) repeat





# Traditional Photon Tracing

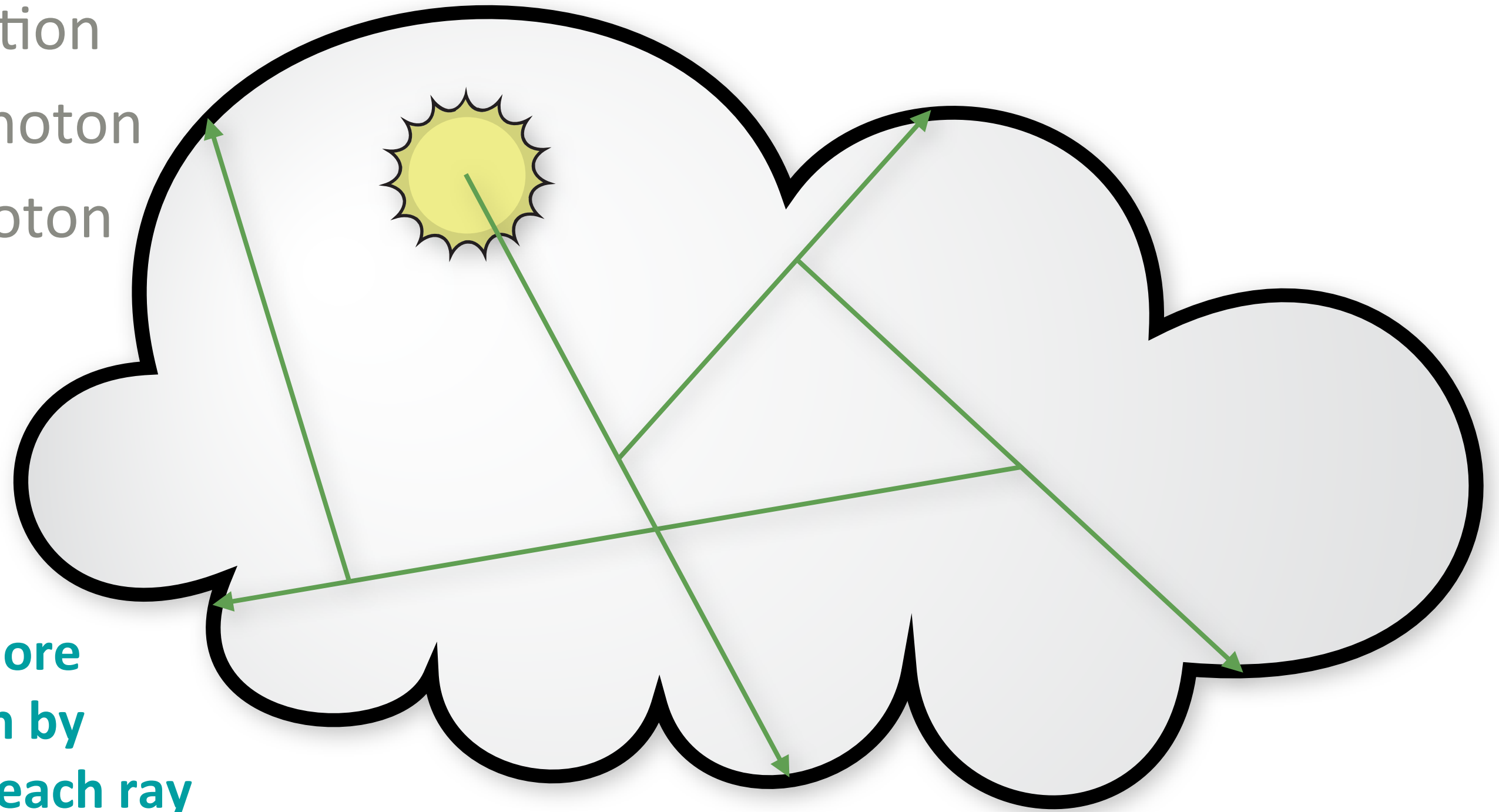
- 1) choose direction
- 2) propagate photon
- 3) deposit a photon
- 4) repeat





# “Photon Marching”

- 1) choose direction
- 2) propagate photon
- 3) deposit a photon
- 4) repeat

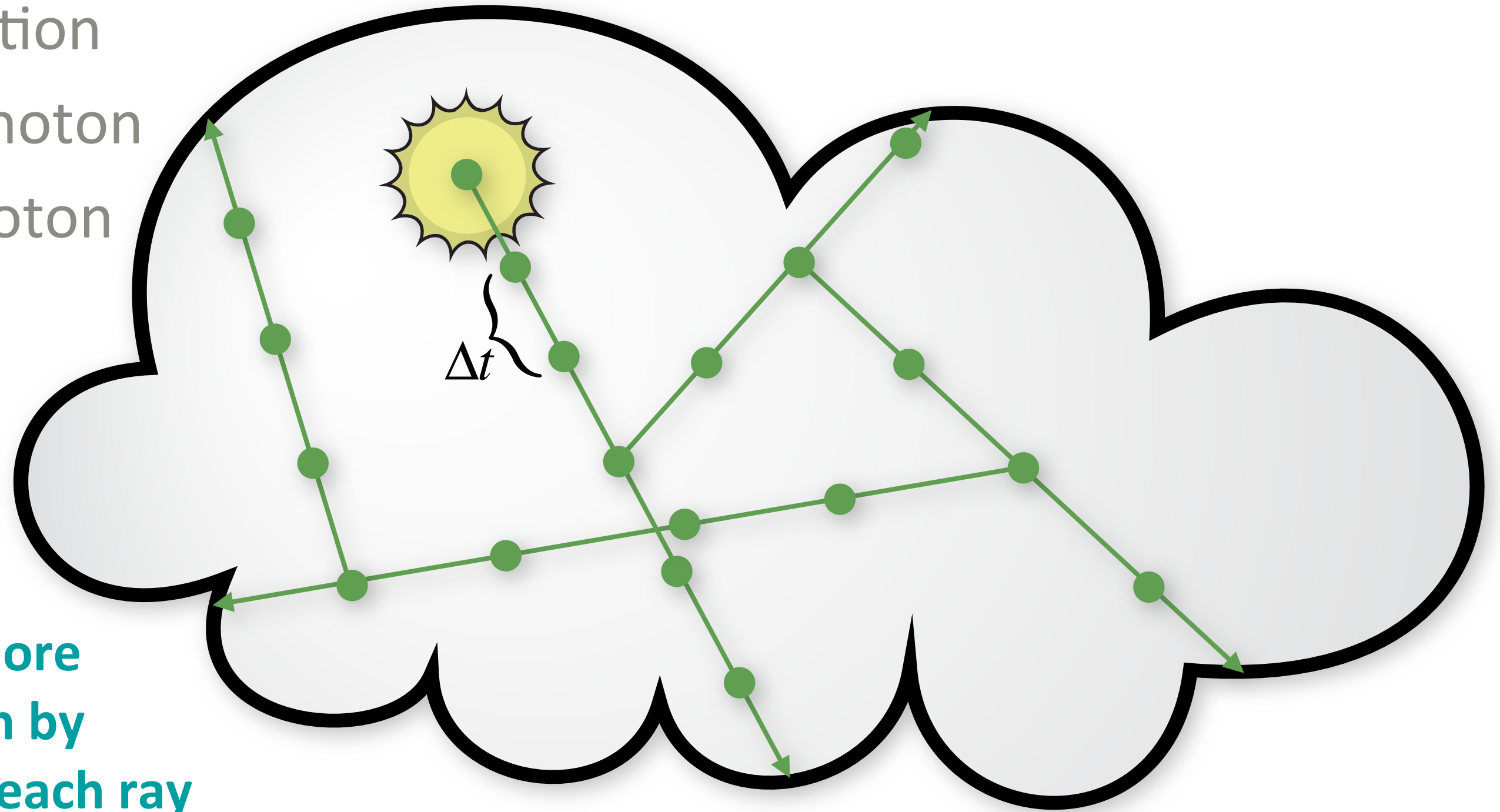


**Could deposit more than one photon by marching along each ray**



# “Photon Marching”

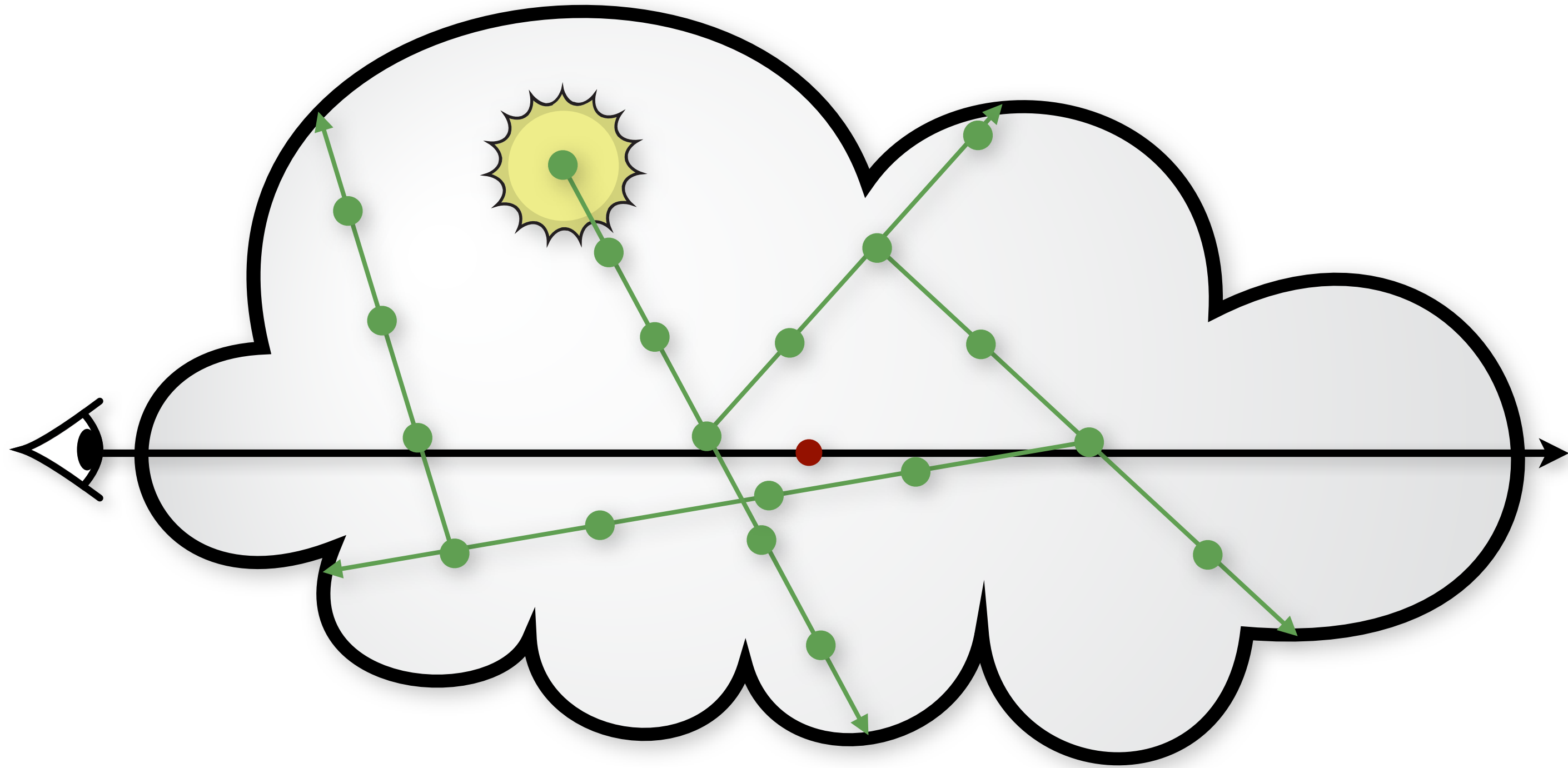
- 1) choose direction
- 2) propagate photon
- 3) deposit a photon
- 4) repeat



Could deposit more than one photon by marching along each ray



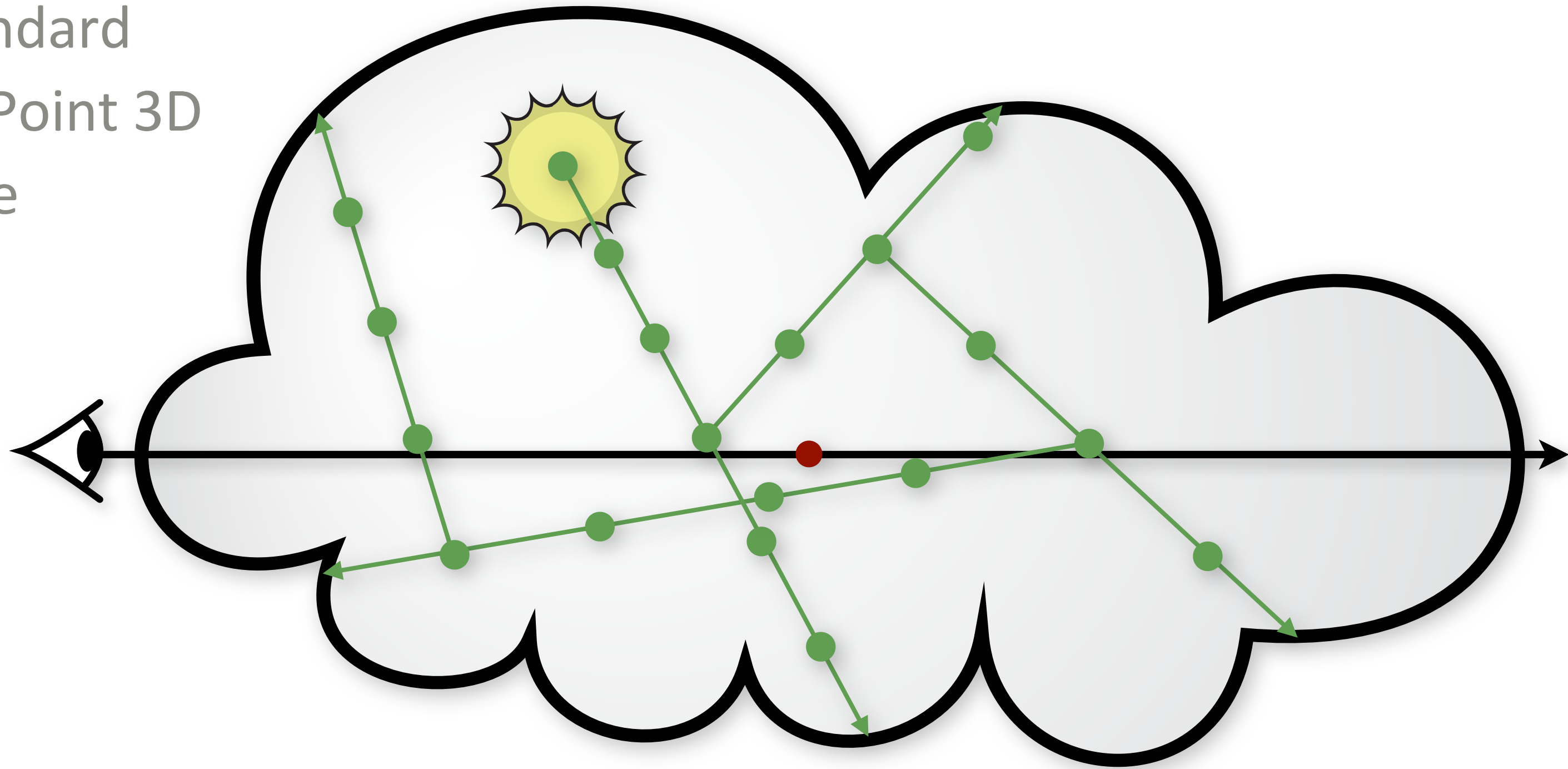
# Radiance Estimation using “Discrete Photon Beams”





# Radiance Estimation using “Discrete Photon Beams”

- Use standard Point x Point 3D estimate

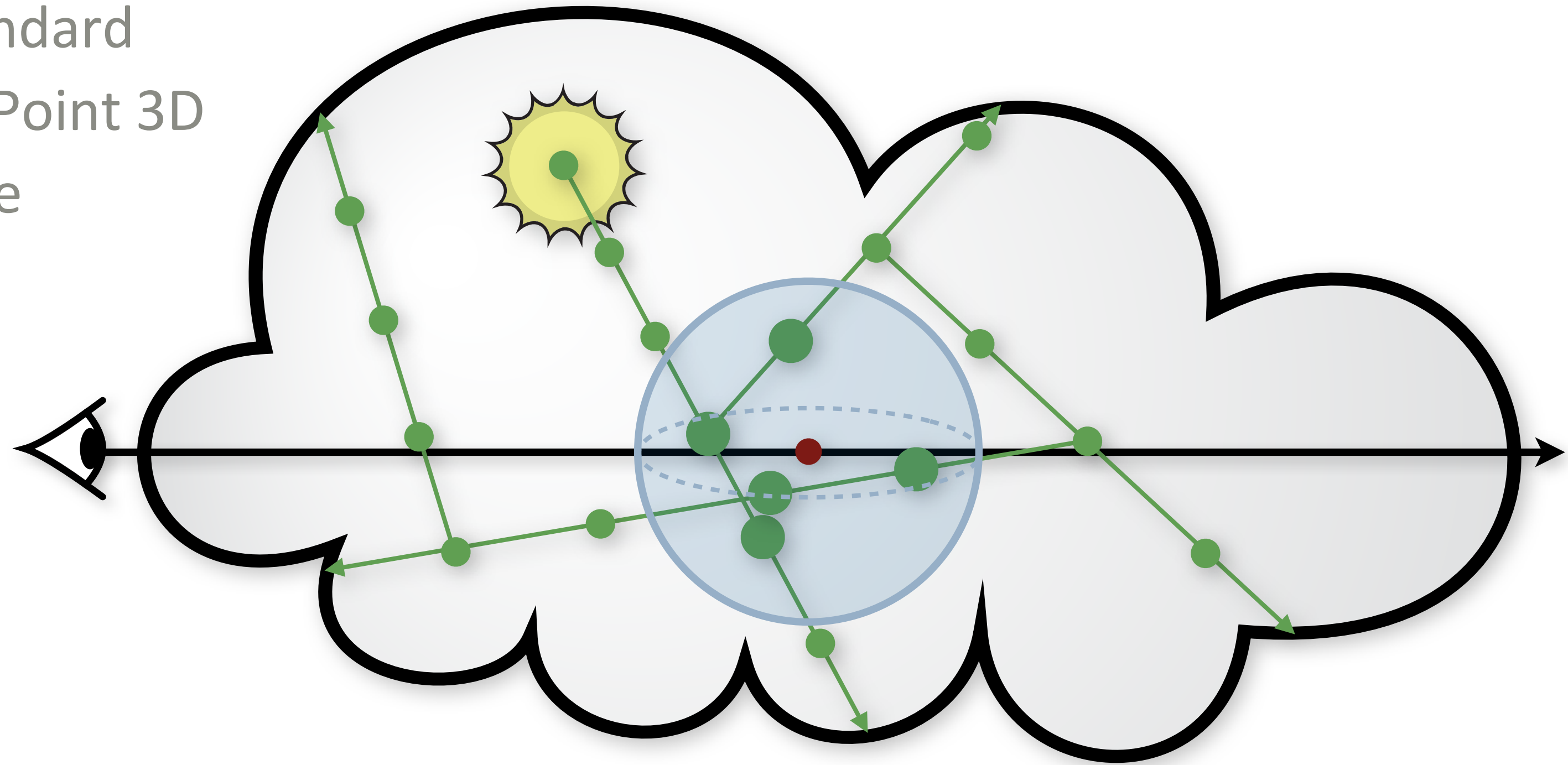






# Radiance Estimation using “Discrete Photon Beams”

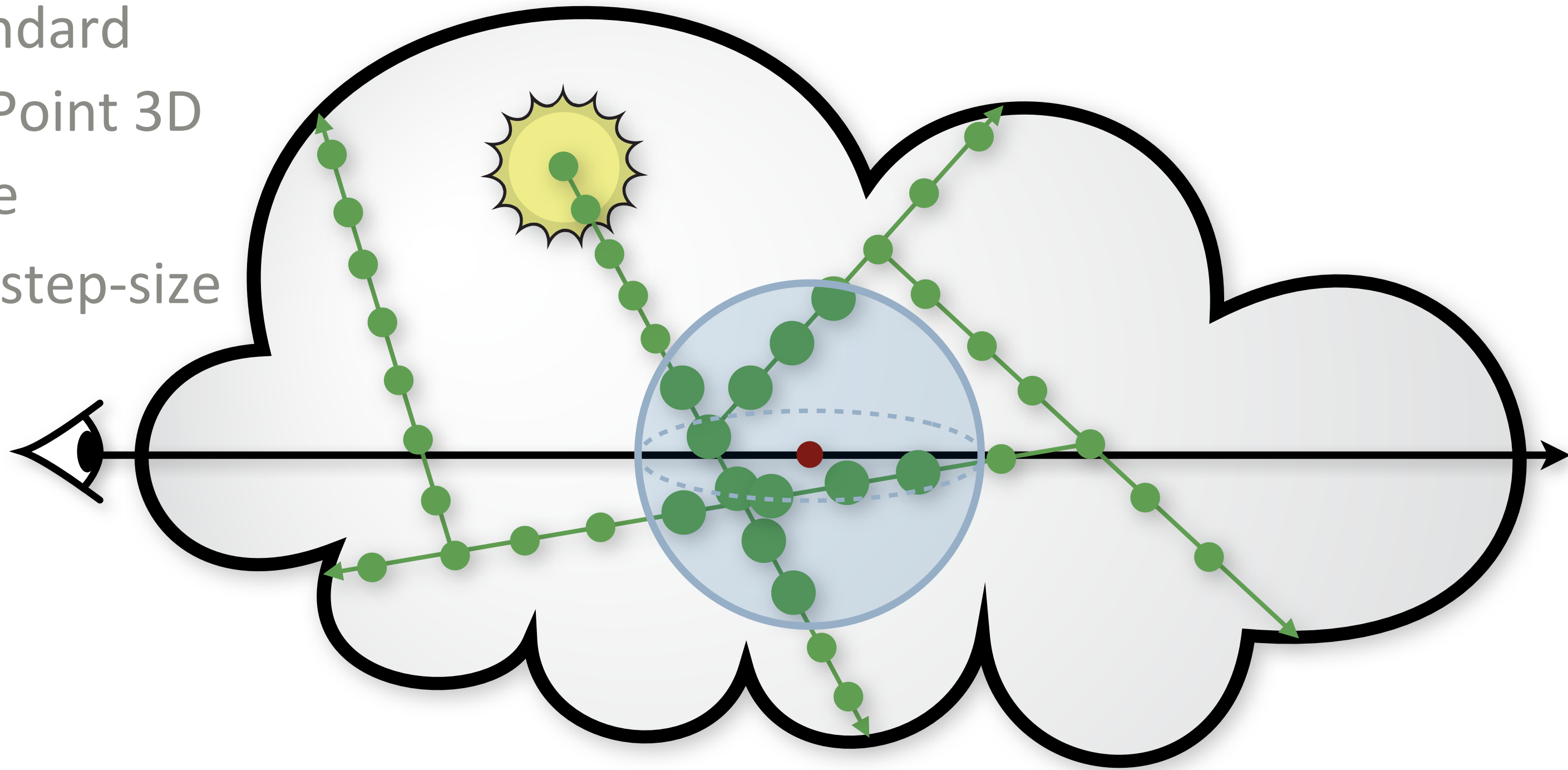
- Use standard Point x Point 3D estimate





# Radiance Estimation using “Discrete Photon Beams”

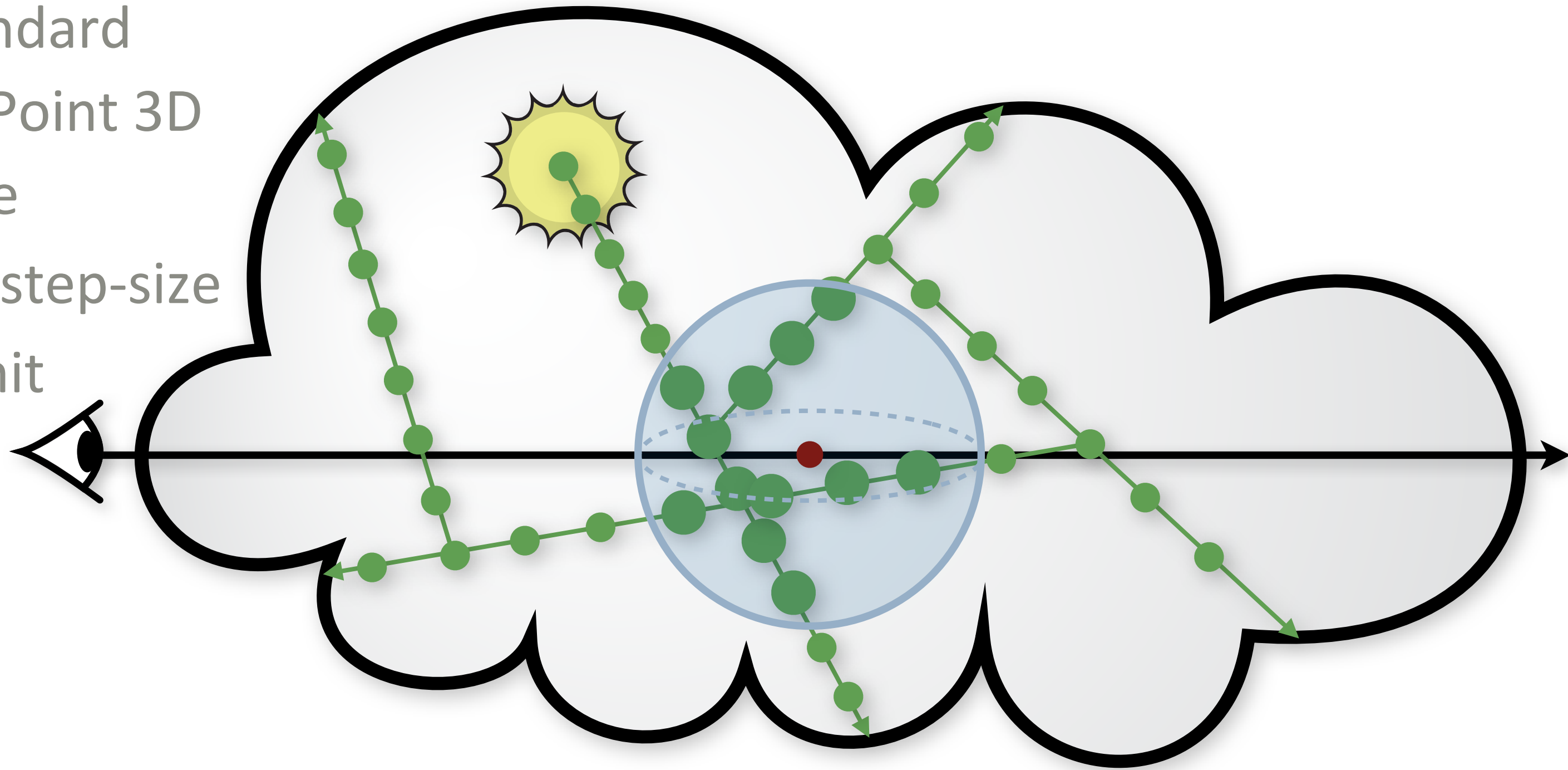
- Use standard Point x Point 3D estimate
- Reduce step-size





# Radiance Estimation using “Discrete Photon Beams”

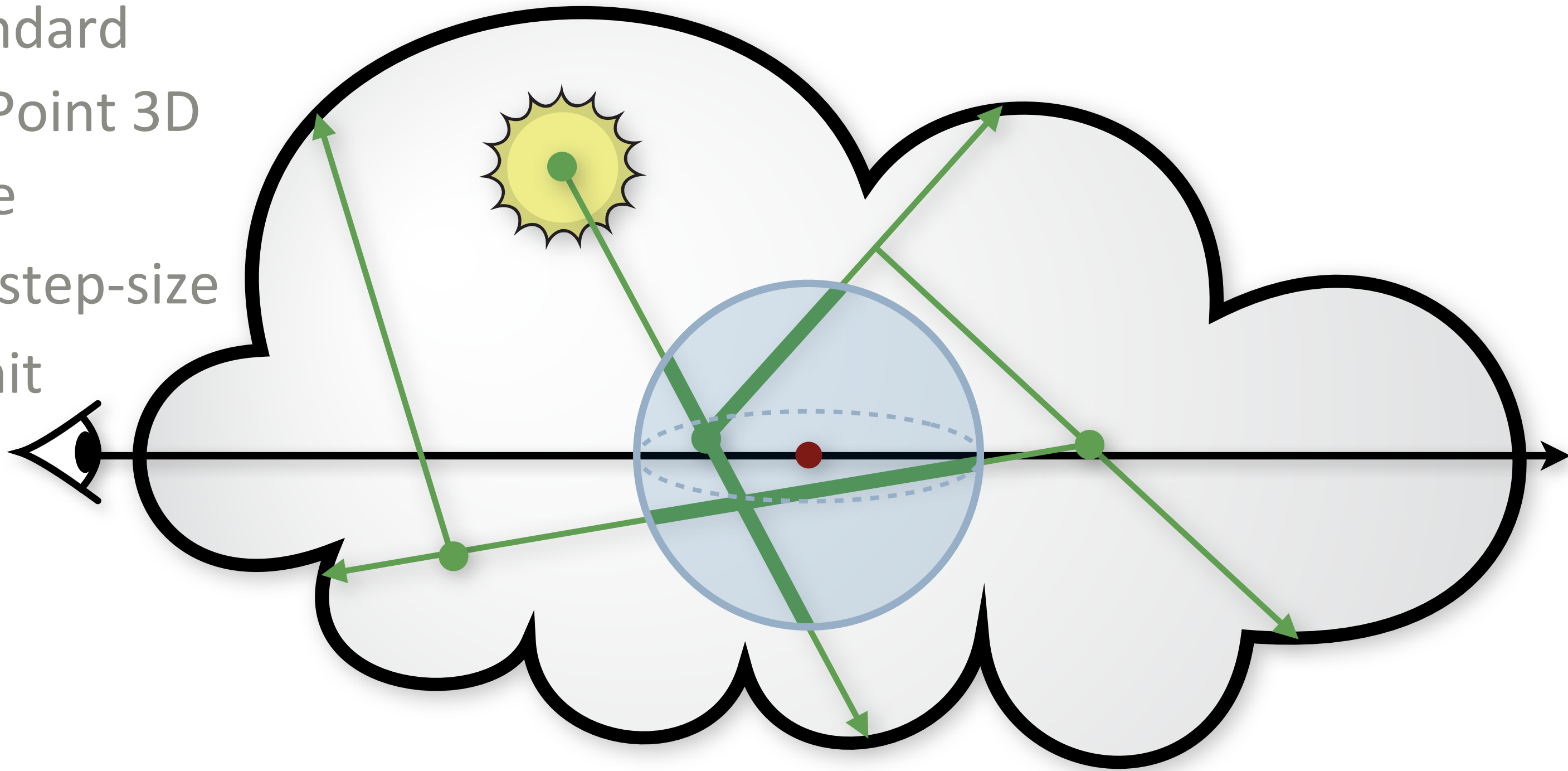
- Use standard Point x Point 3D estimate
- Reduce step-size
- Take limit



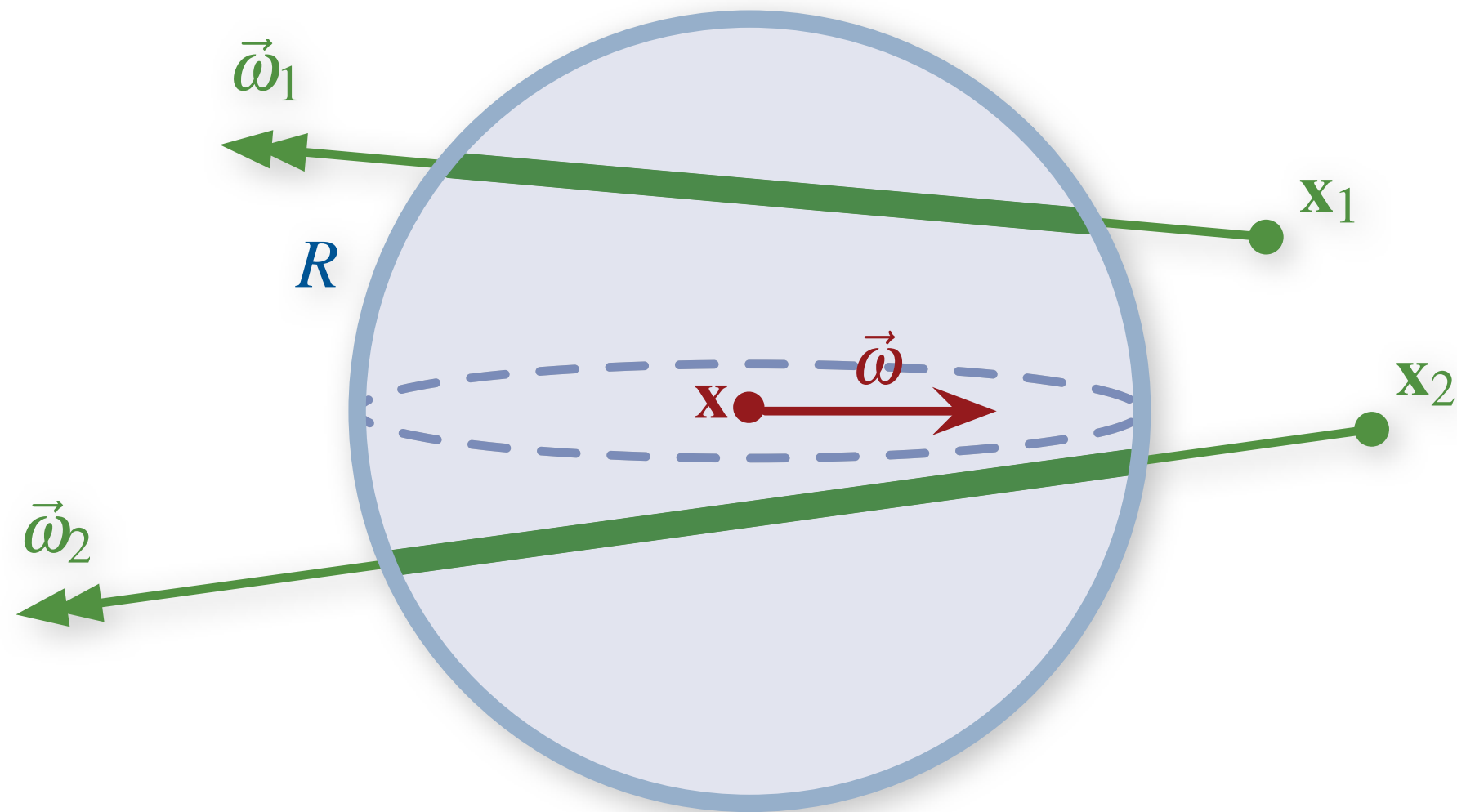


# Radiance Estimation using “Discrete Photon Beams”

- Use standard Point x Point 3D estimate
- Reduce step-size
- Take limit

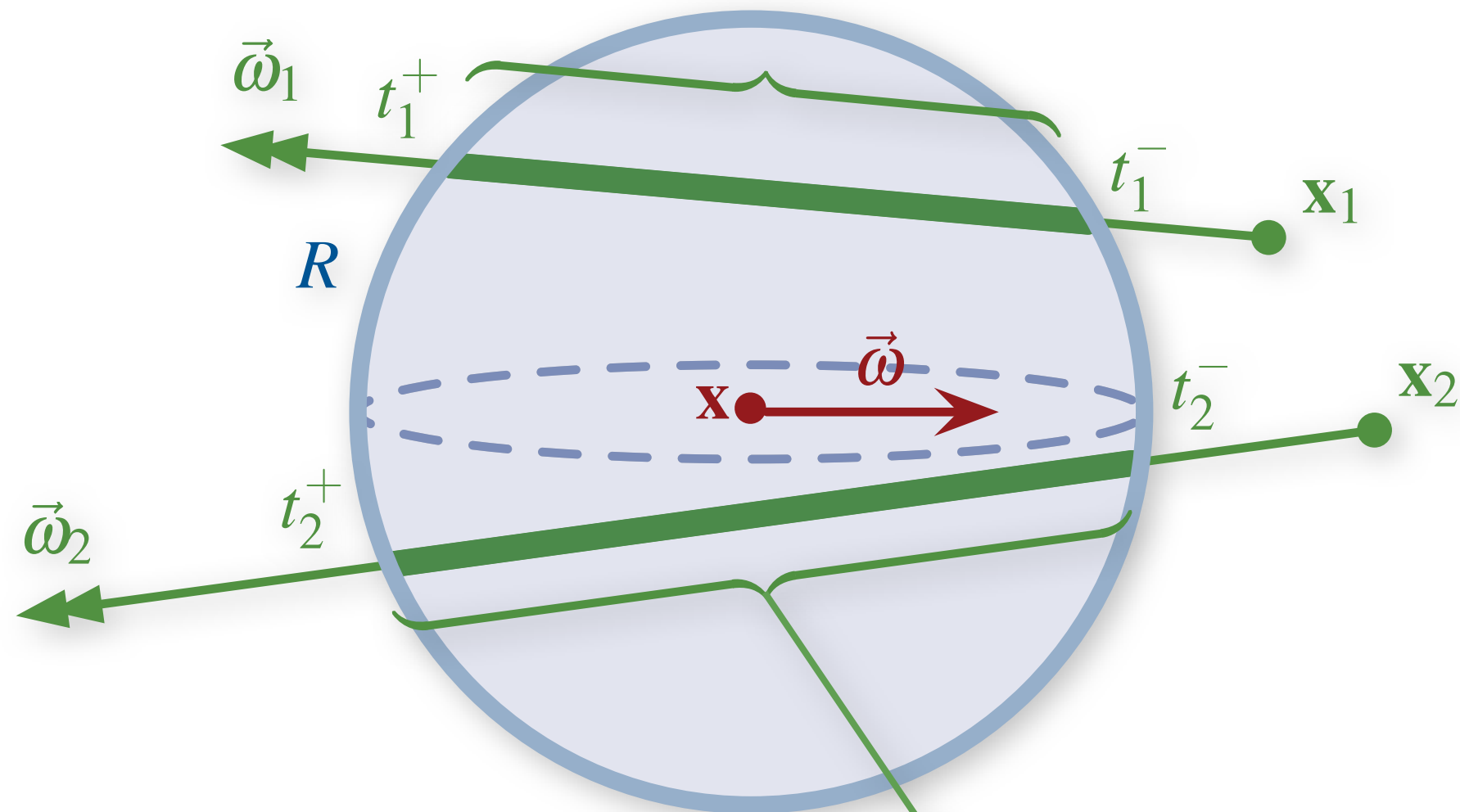


# Point Query × Beam Data (3D blur)



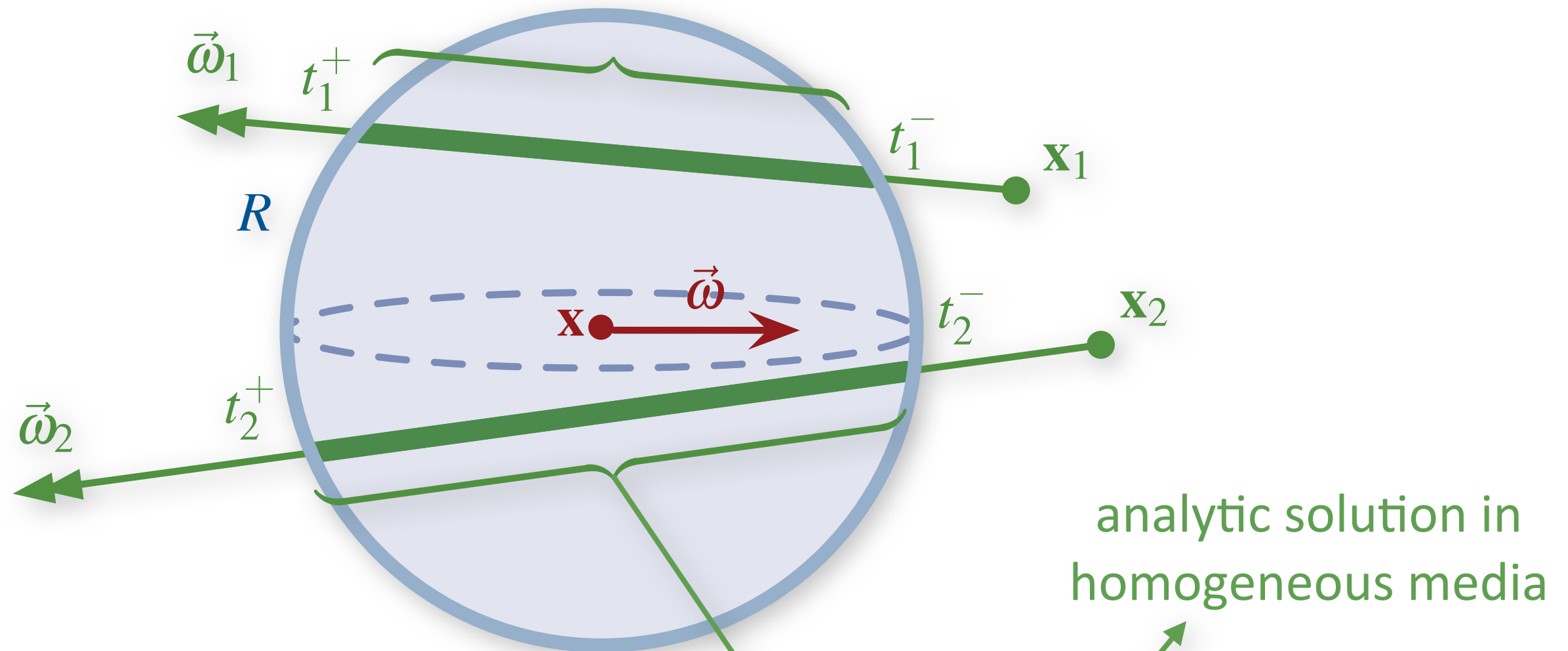
$$L \approx \frac{1}{\mu_R(r^3)} \sum_i f(\theta_i) \Phi_i \int_{t_i^-}^{t_i^+} e^{-\sigma_t t} dt$$

# Point Query × Beam Data (3D blur)



$$L \approx \frac{1}{\mu_R(r^3)} \sum_i f(\theta_i) \Phi_i \int_{t_i^-}^{t_i^+} e^{-\sigma_t t} dt$$

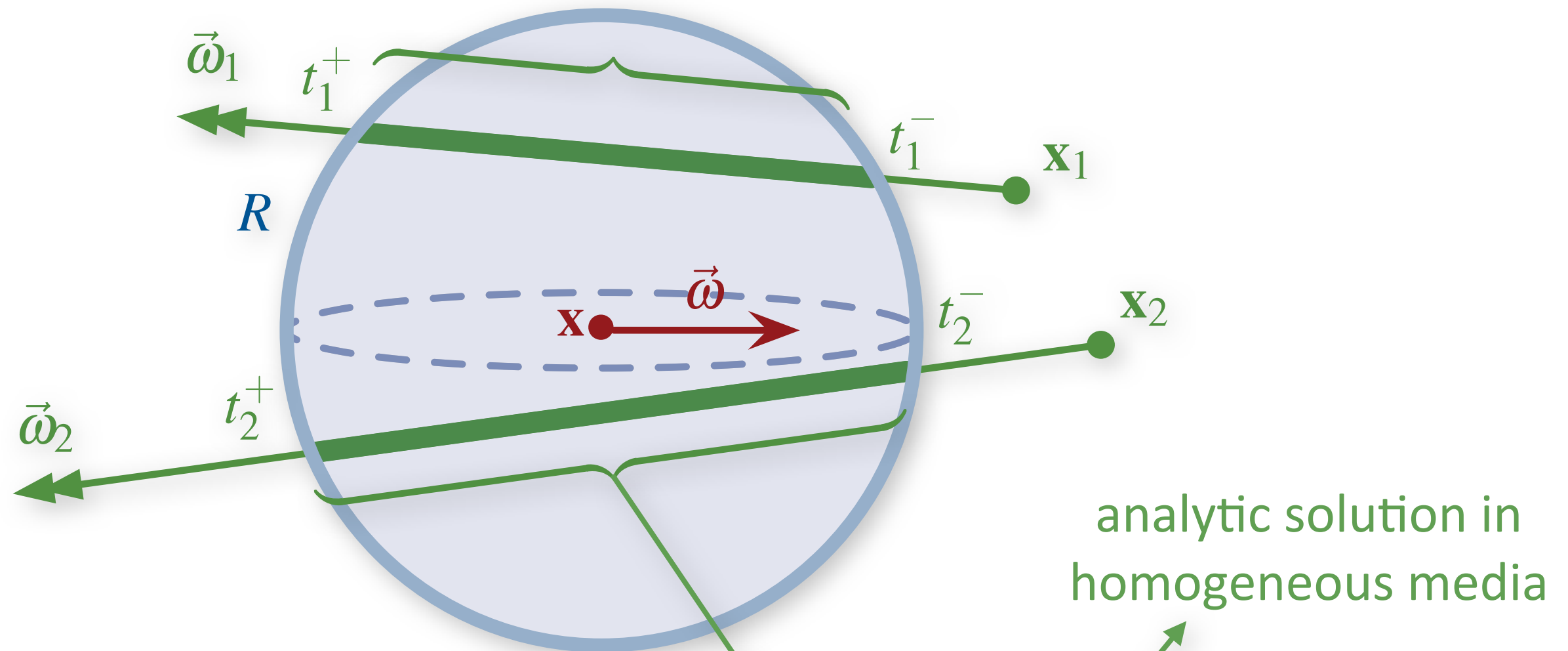
# Point Query × Beam Data (3D blur)



$$L \approx \frac{1}{\mu_R(r^3)} \sum_i f(\theta_i) \Phi_i \int_{t_i^-}^{t_i^+} e^{-\sigma_t t} dt$$

analytic solution in homogeneous media

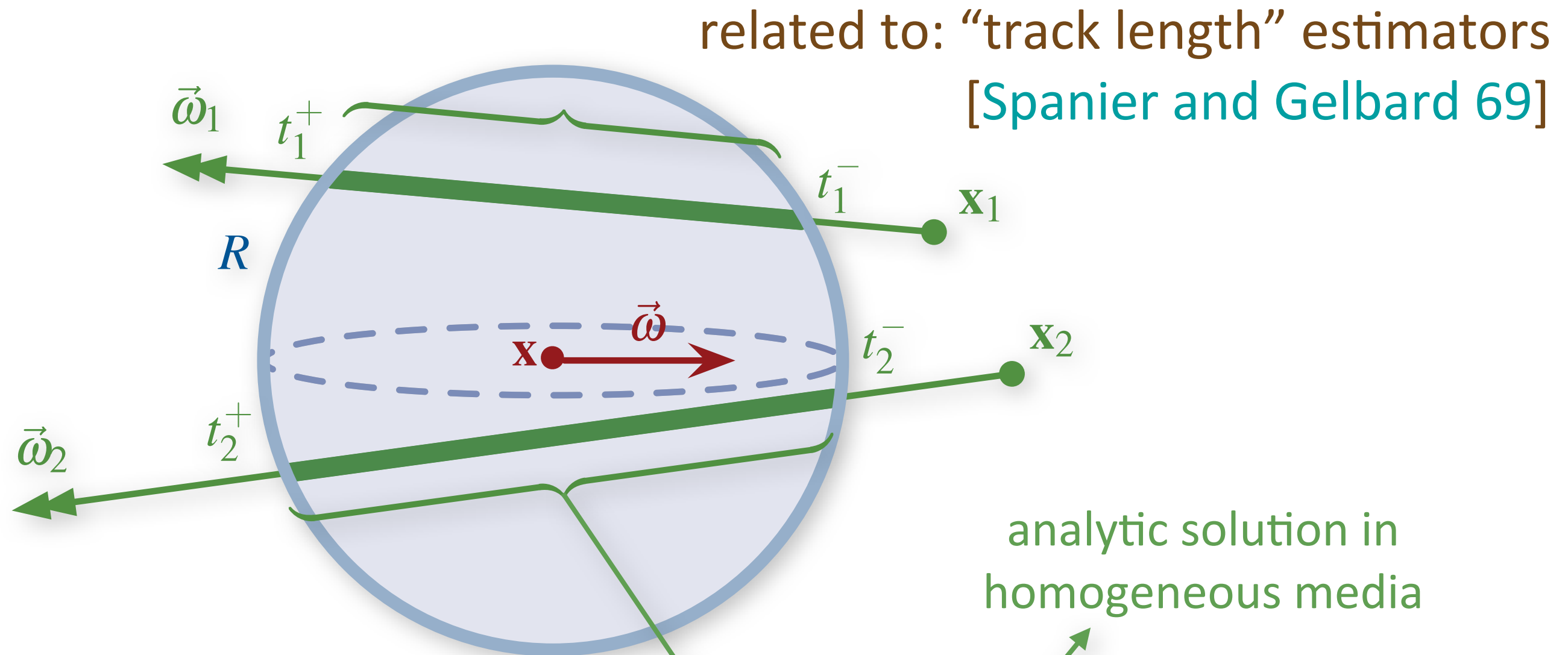
# Point Query × Beam Data (3D blur)



$$L \approx \frac{1}{\mu_R(r^3)} \sum_i f(\theta_i) \Phi_i \int_{t_i^-}^{t_i^+} e^{-\sigma_t t} dt$$



# Point Query × Beam Data (3D blur)

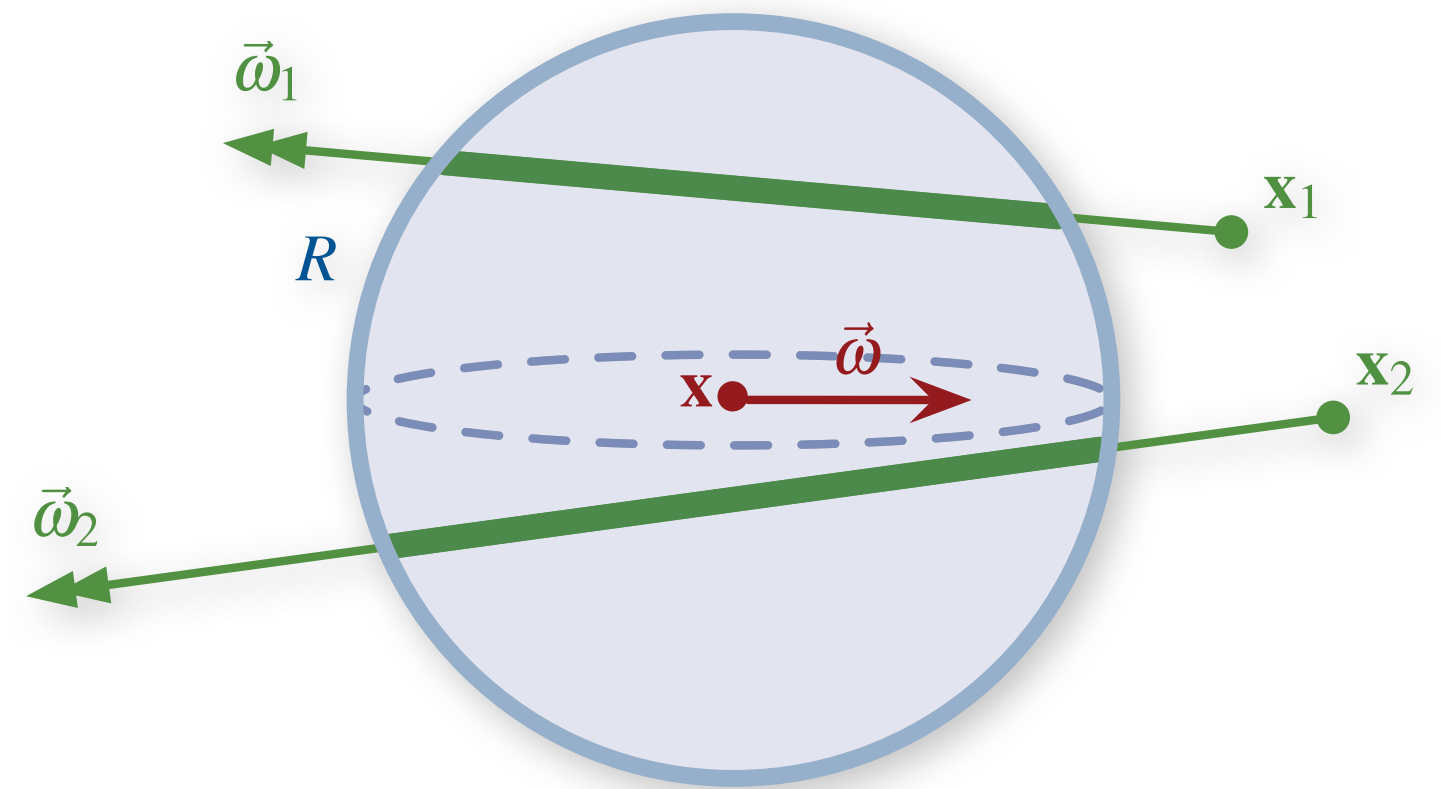


$$L \approx \frac{1}{\mu_R(r^3)} \sum_i f(\theta_i) \Phi_i \int_{t_i^-}^{t_i^+} e^{-\sigma_t t} dt$$



# Reducing Blur Dimensionality

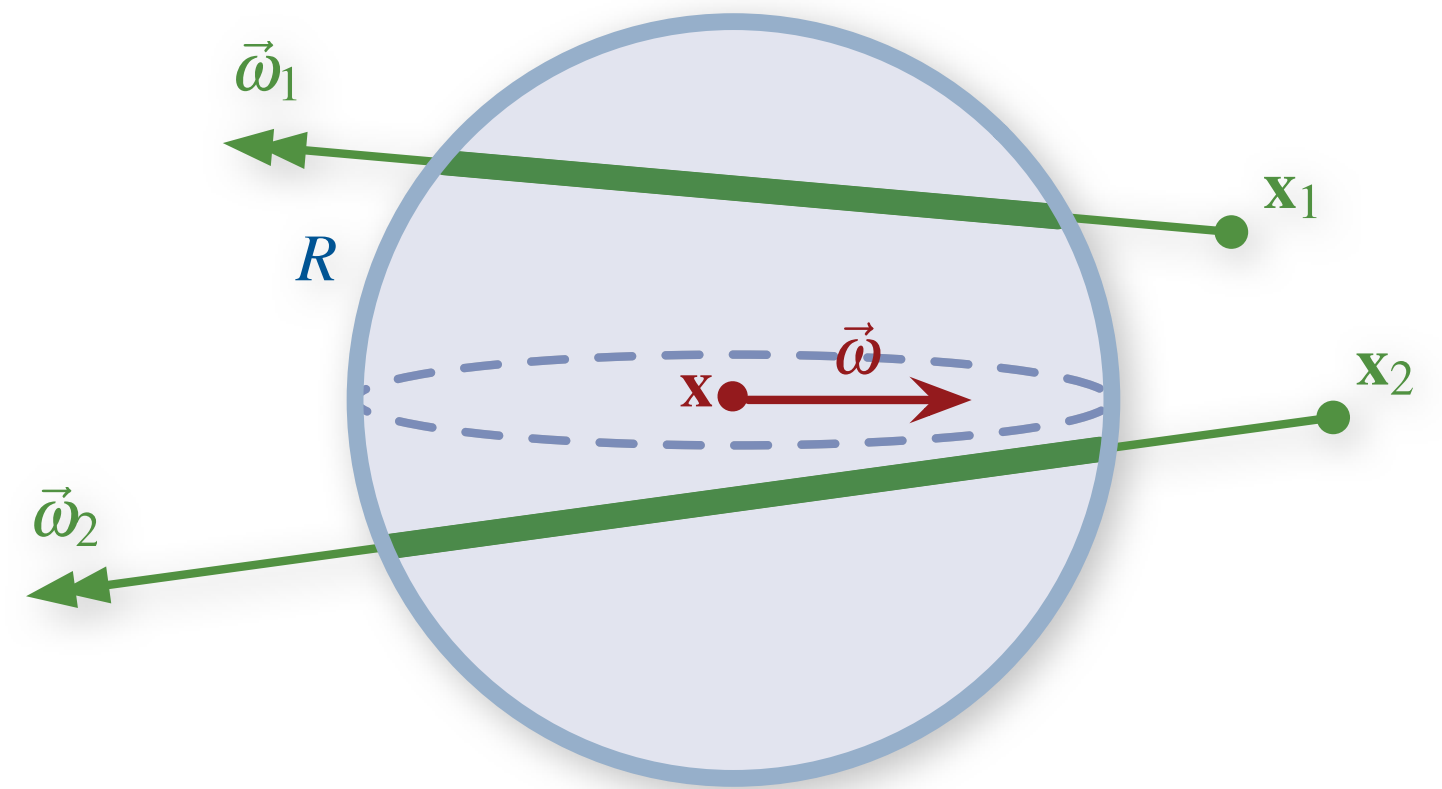
## Point Query x Beam Data (3D blur)



$$L \approx \frac{1}{\mu_R(r^3)} \sum_i f(\theta_i) \Phi_i \int_{t_i^-}^{t_i^+} e^{-\sigma t} dt$$

# Reducing Blur Dimensionality

## Point Query x Beam Data (3D blur)

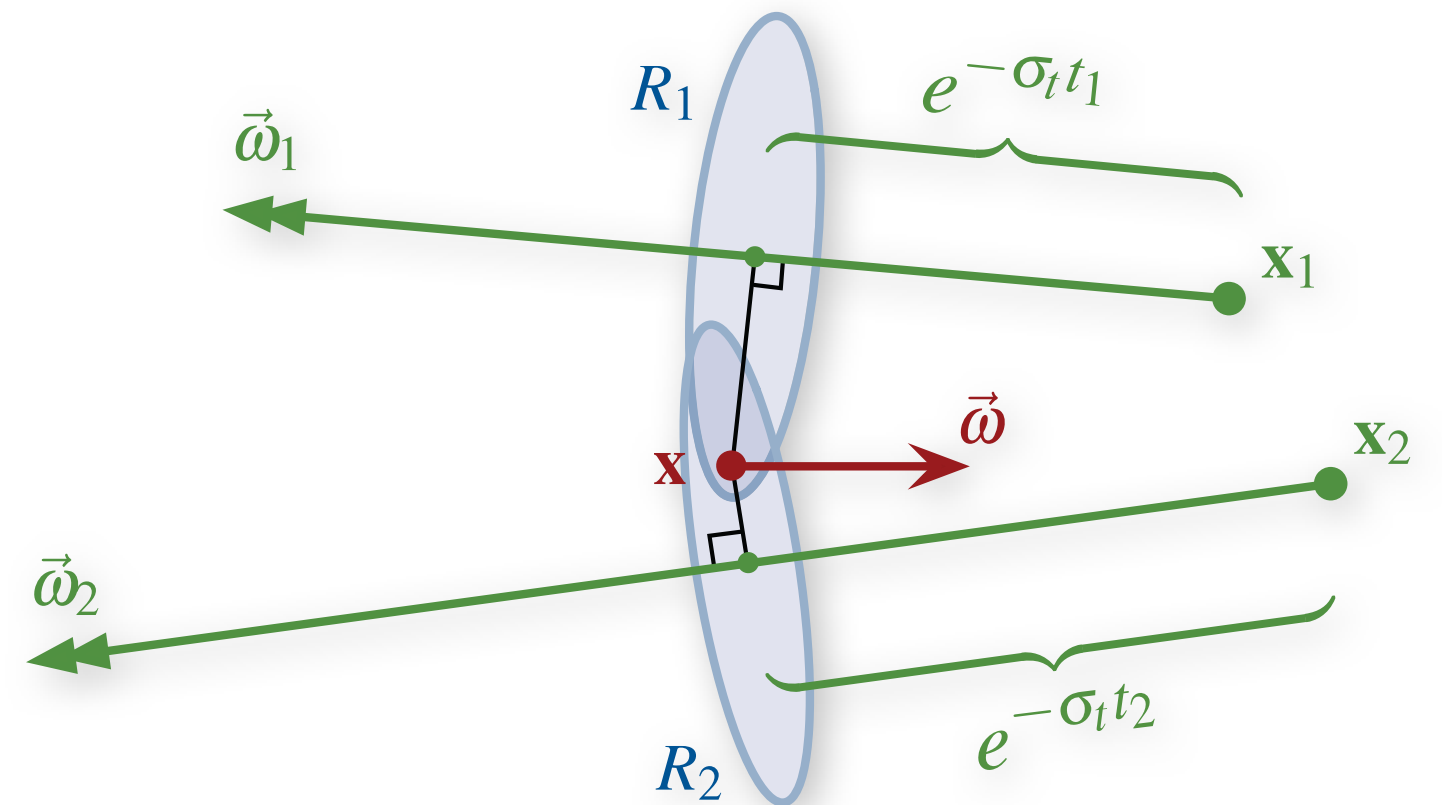


$$L \approx \frac{1}{\mu_R(r^3)} \sum_i f(\theta_i) \Phi_i \int_{t_i^-}^{t_i^+} e^{-\sigma t} dt$$



# Reducing Blur Dimensionality

## Point Query x Beam Data (2D blur)

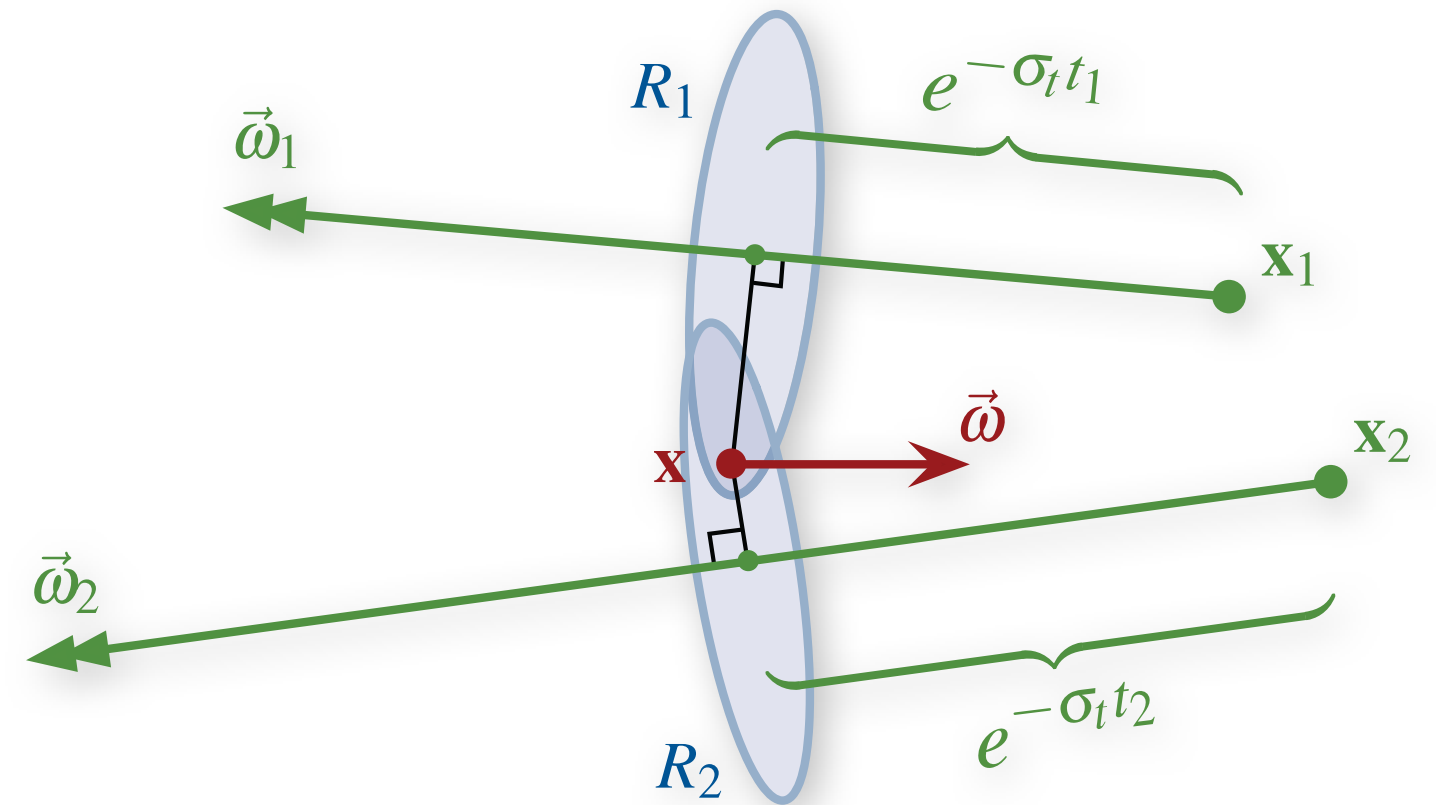


$$L \approx \frac{1}{\mu_R(r^2)} \sum_i f(\theta_i) \Phi_i e^{-\sigma_t t_i}$$



# Reducing Blur Dimensionality

## Point Query x Beam Data (2D blur)

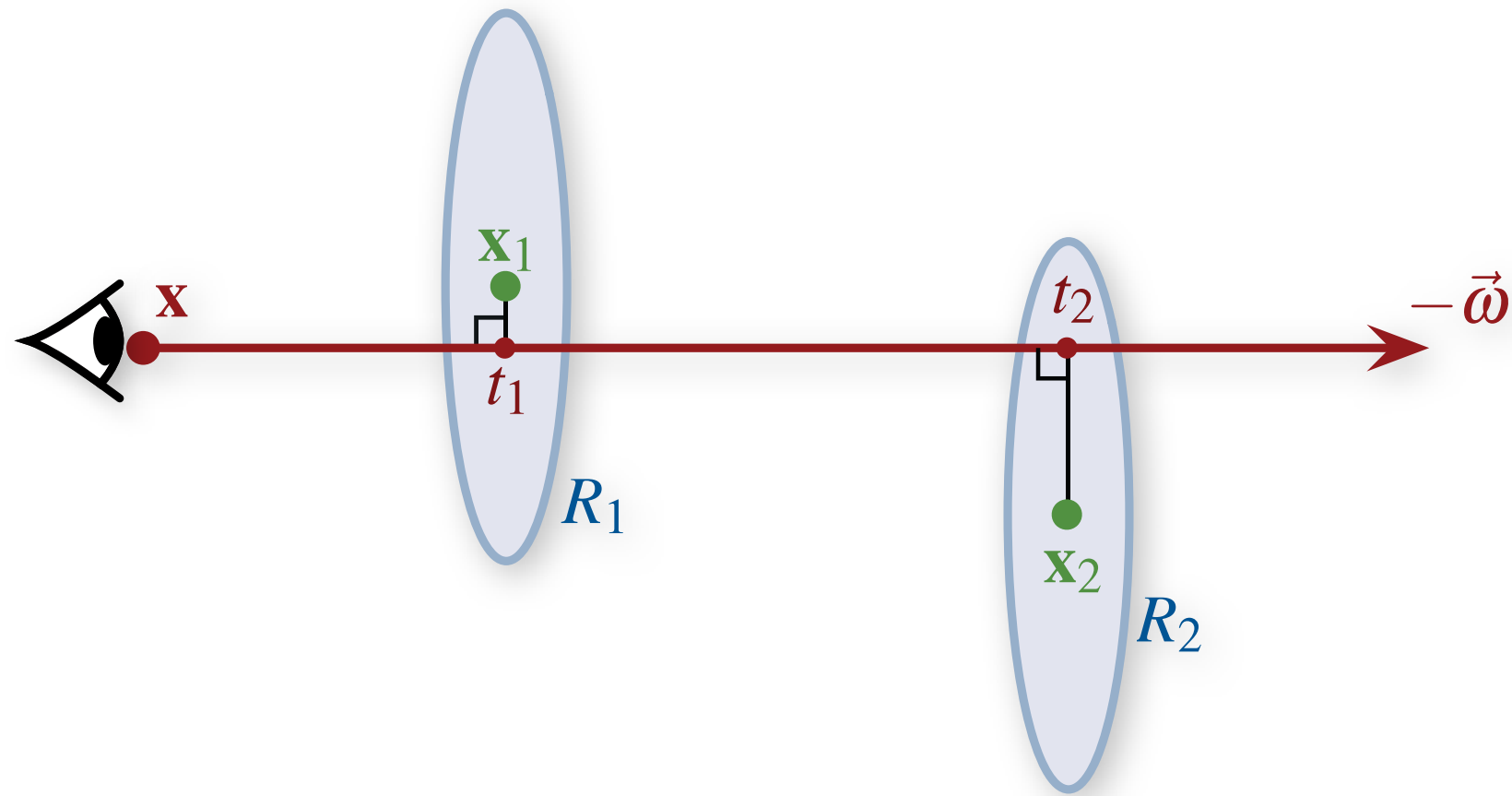


$$L \approx \frac{1}{\mu_R(r^2)} \sum_i f(\theta_i) \Phi_i e^{-\sigma_t t_i}$$



# Radiometric Duality

## Beam Query x Point Data (2D blur)

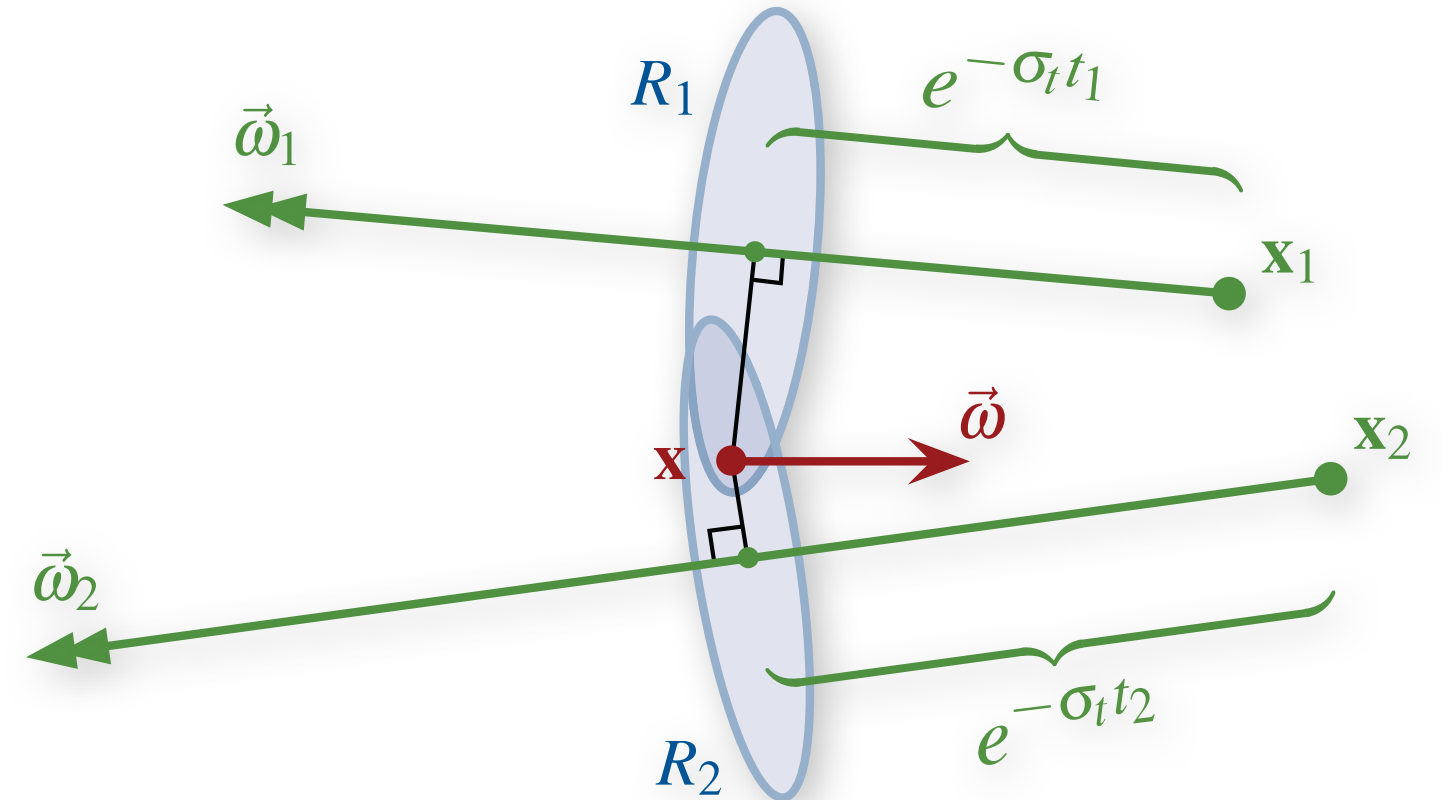


$$L \approx \frac{1}{\mu_R(r^2)} \sum_i f(\theta_i) \Phi_i e^{-\sigma_t t_i}$$

“Beam Radiance Estimate”

[Jarosz et al. 08]

## Point Query x Beam Data (2D blur)

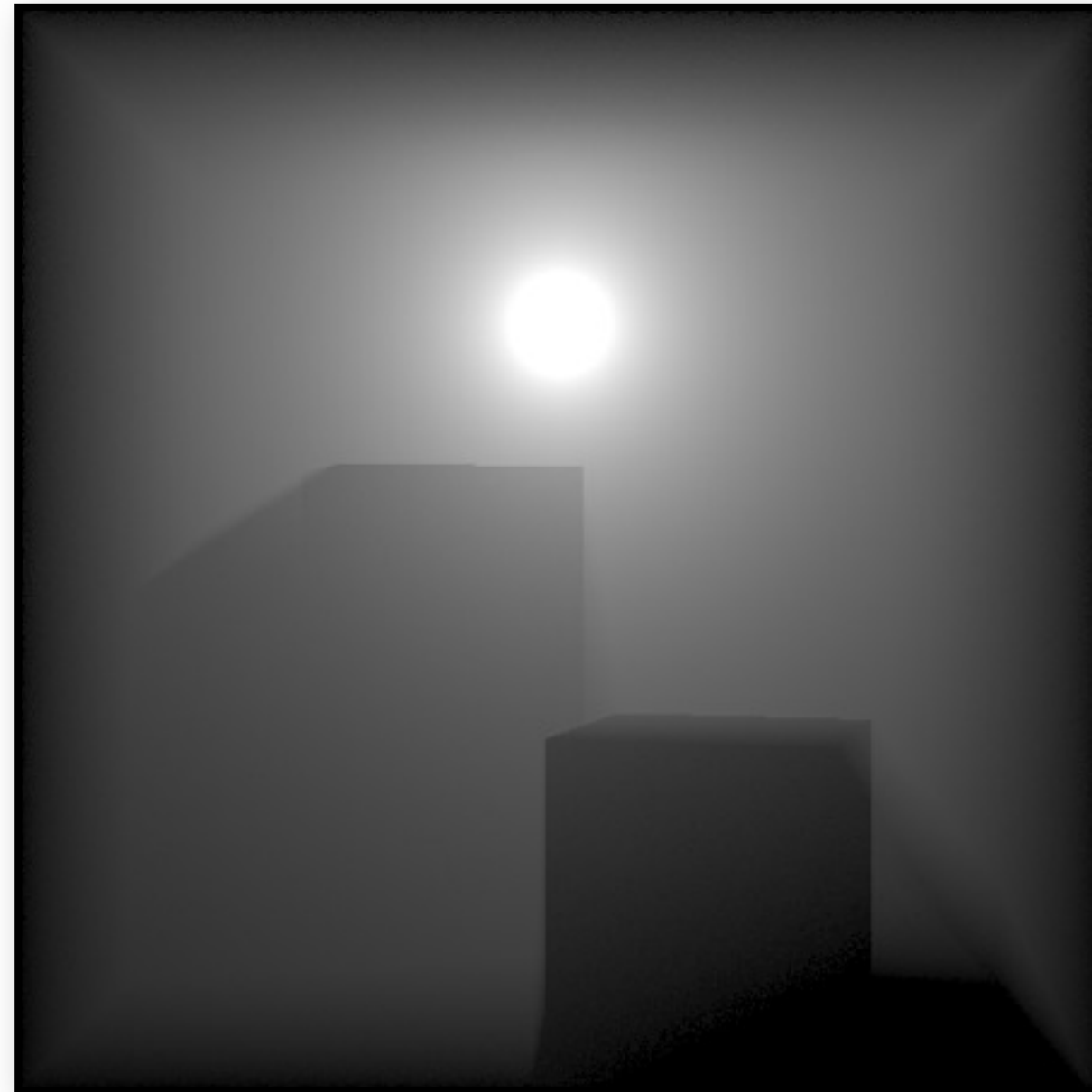


$$L \approx \frac{1}{\mu_R(r^2)} \sum_i f(\theta_i) \Phi_i e^{-\sigma_t t_i}$$



# Photon Points vs. Photon Beams

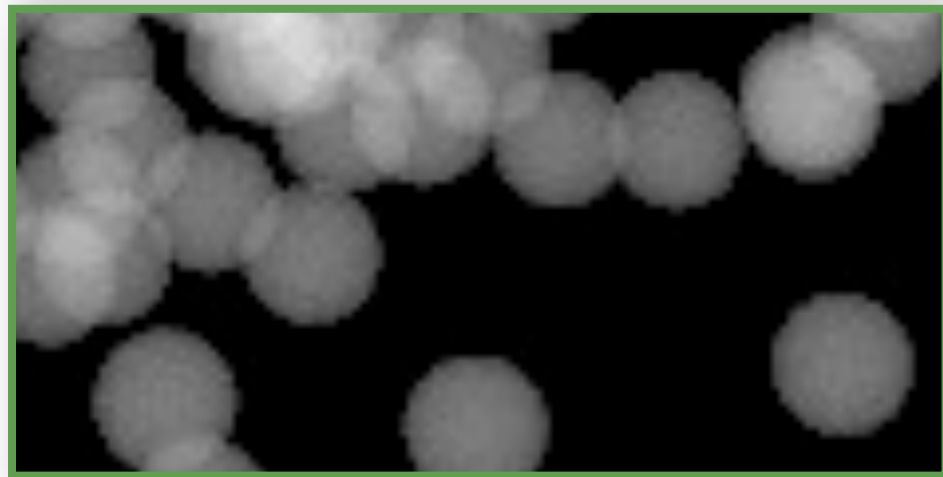
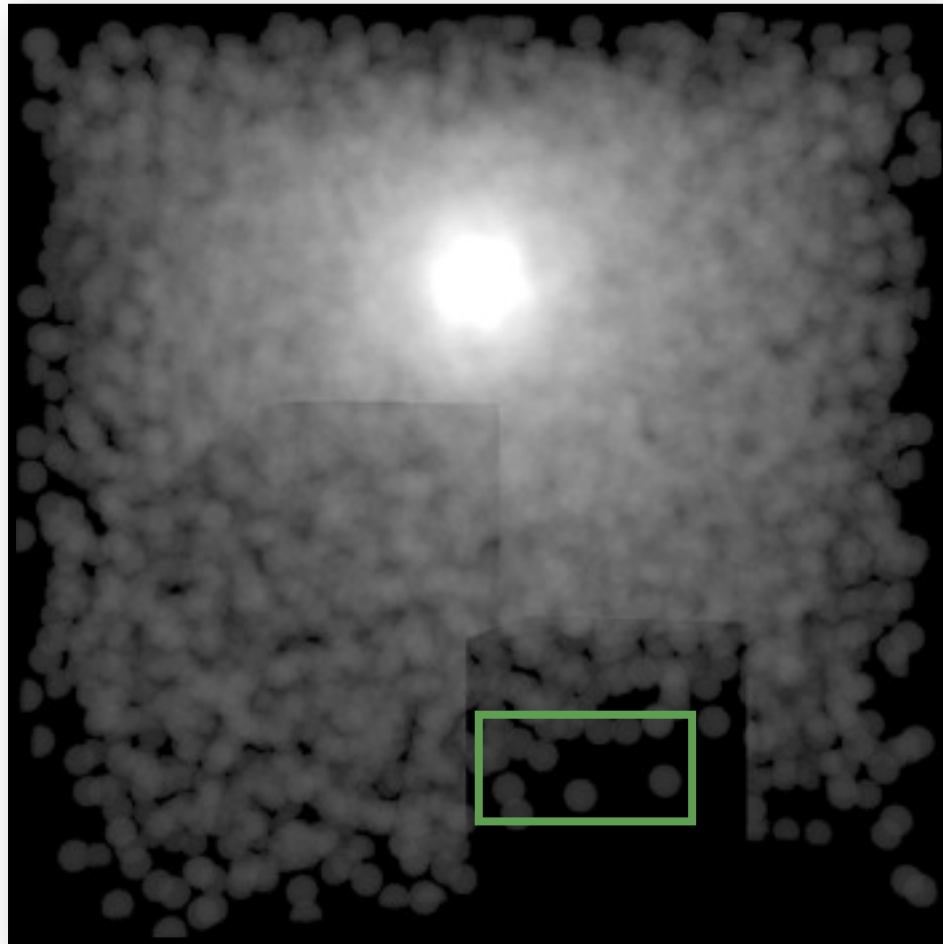
Ground Truth



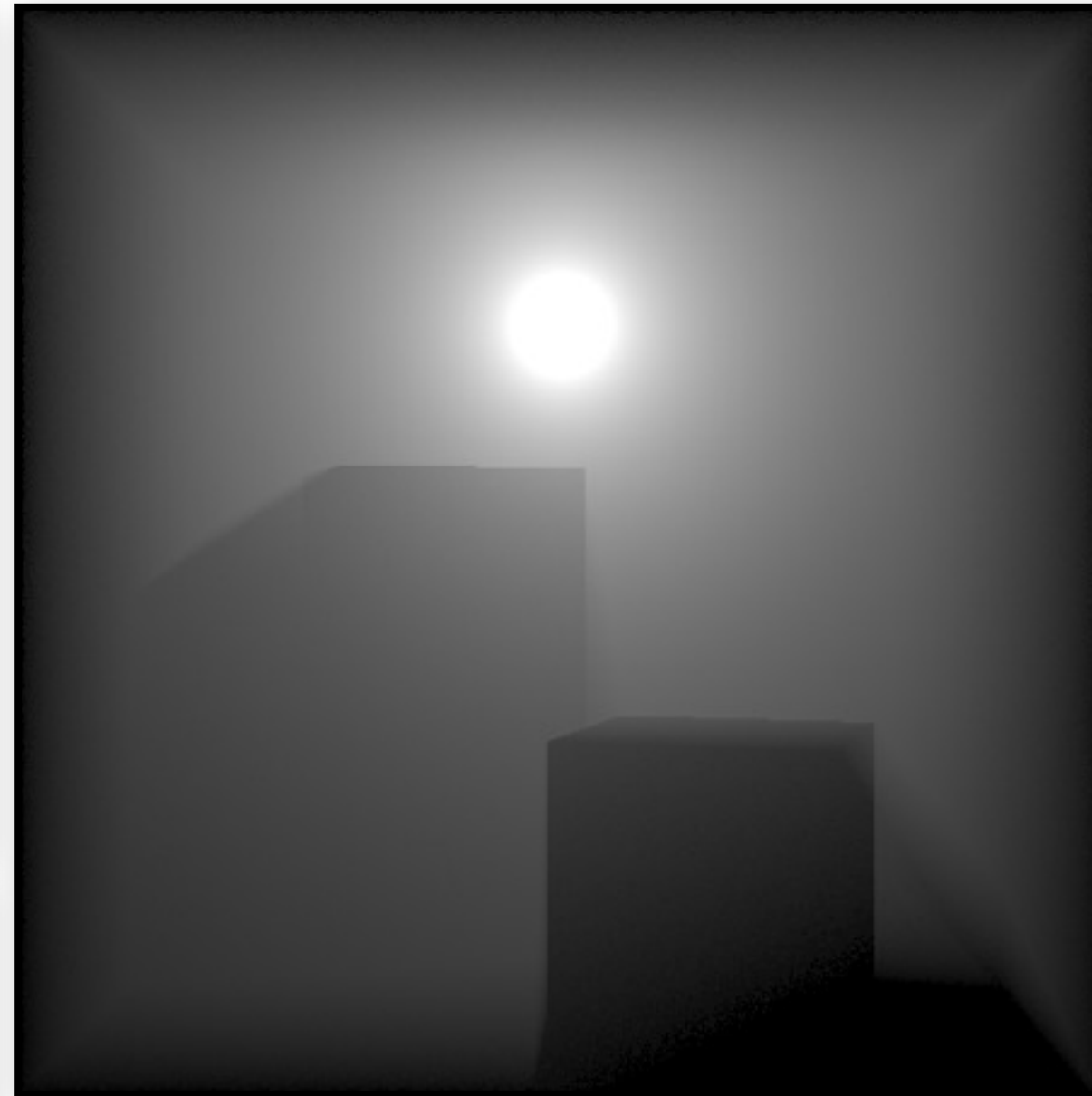


# Photon Points vs. Photon Beams

100k Photon Points



Ground Truth

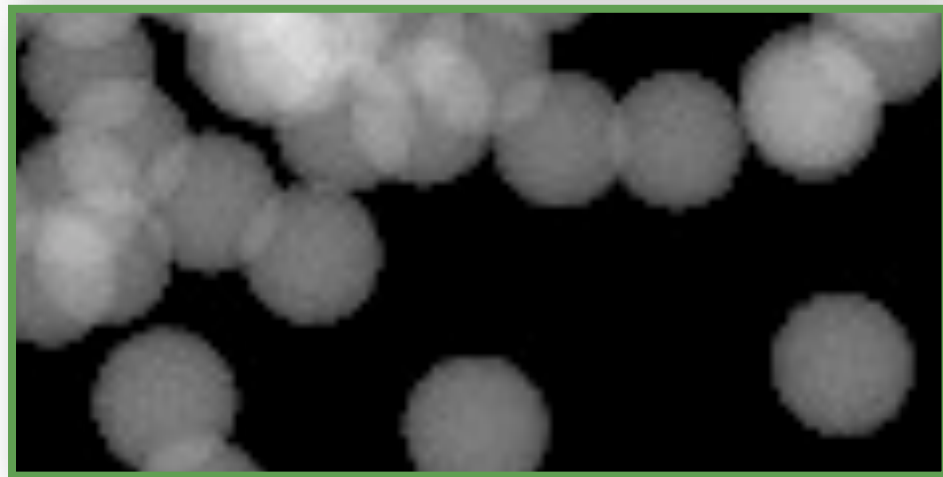
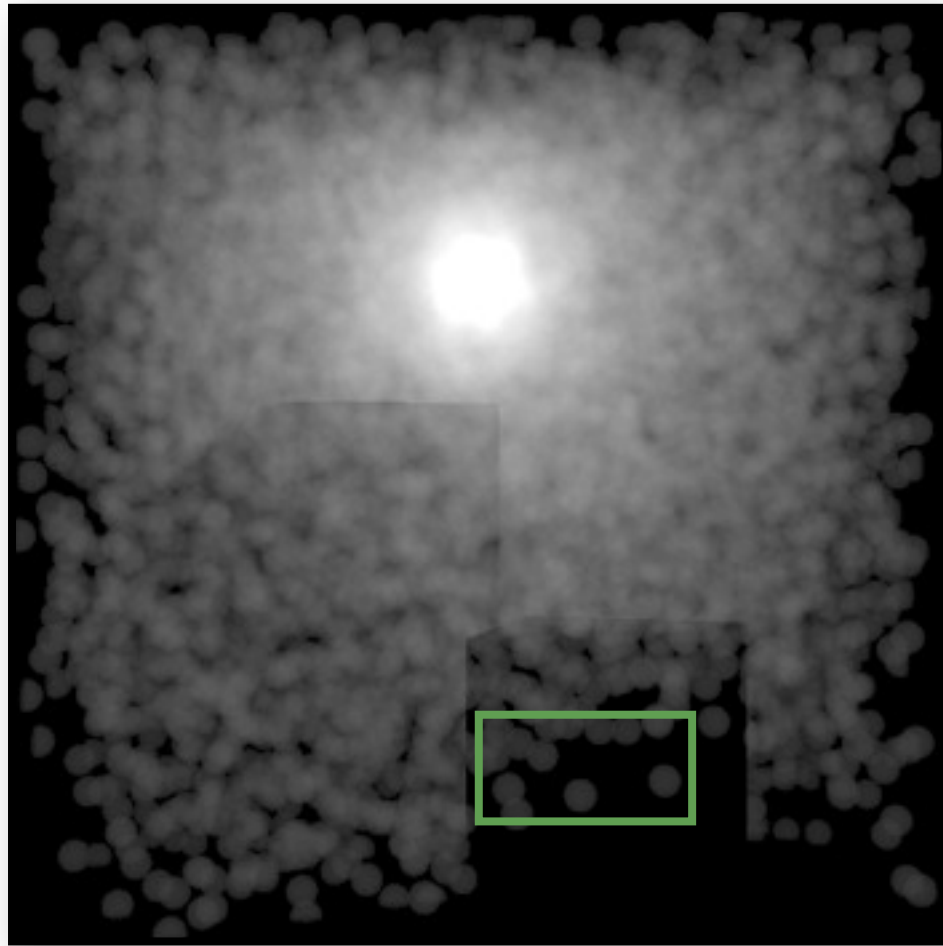




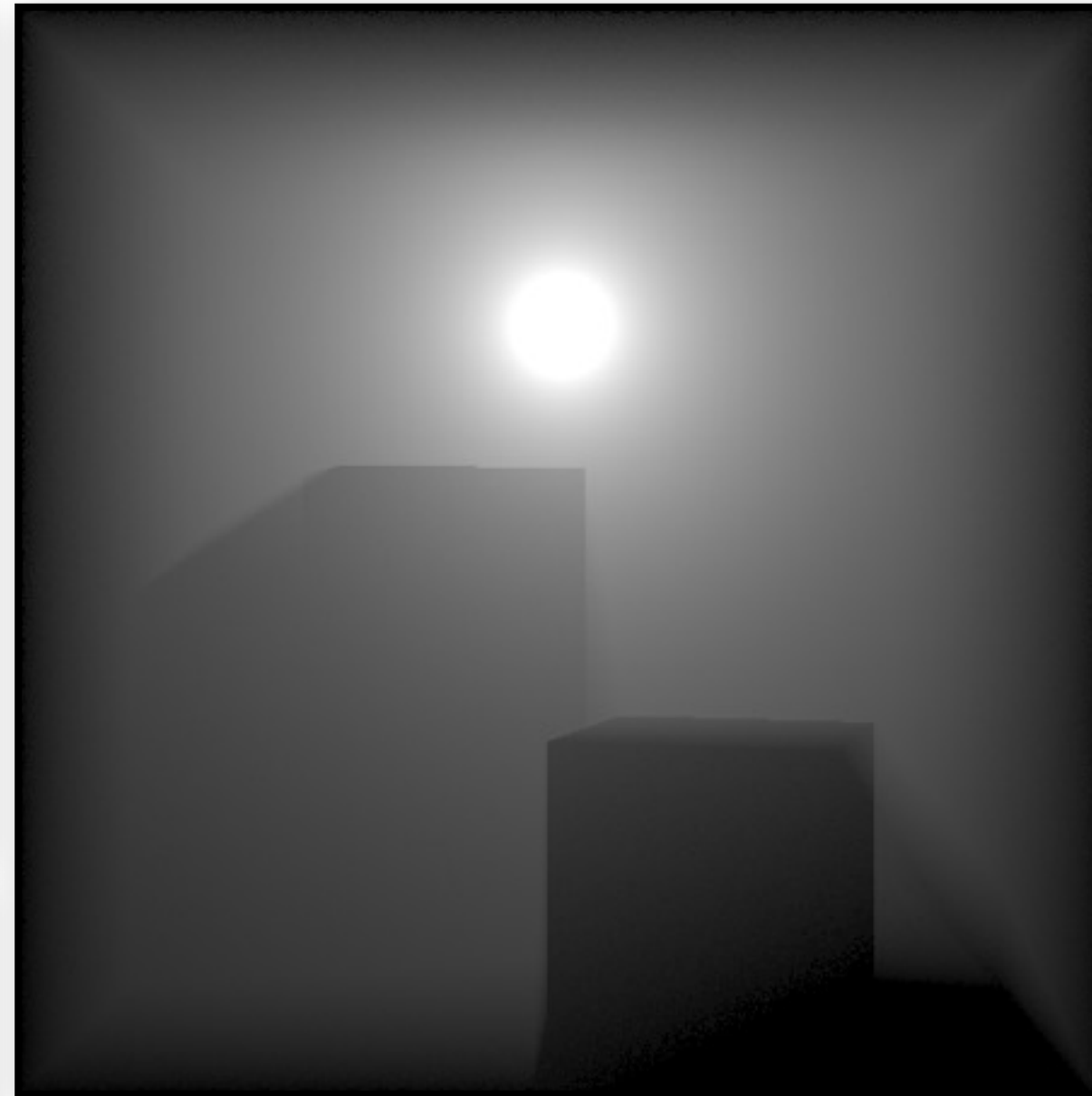


# Photon Points vs. Photon Beams

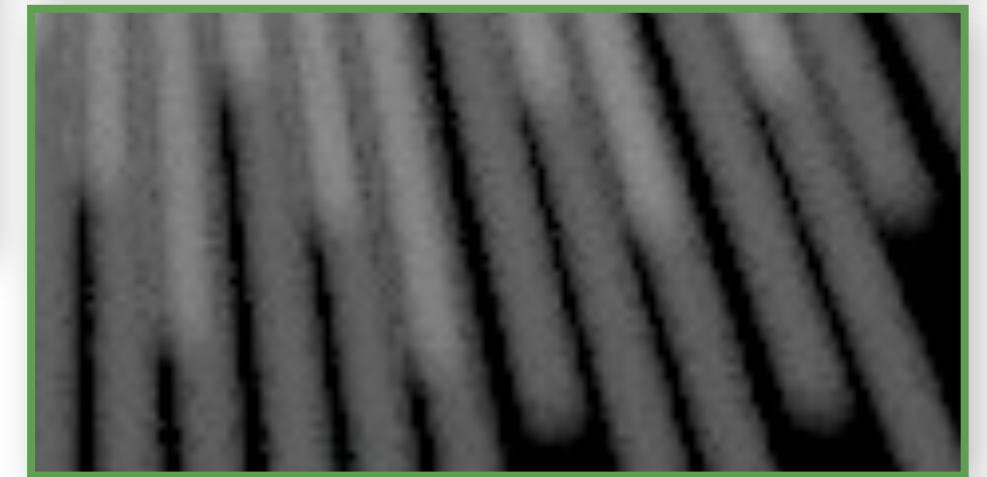
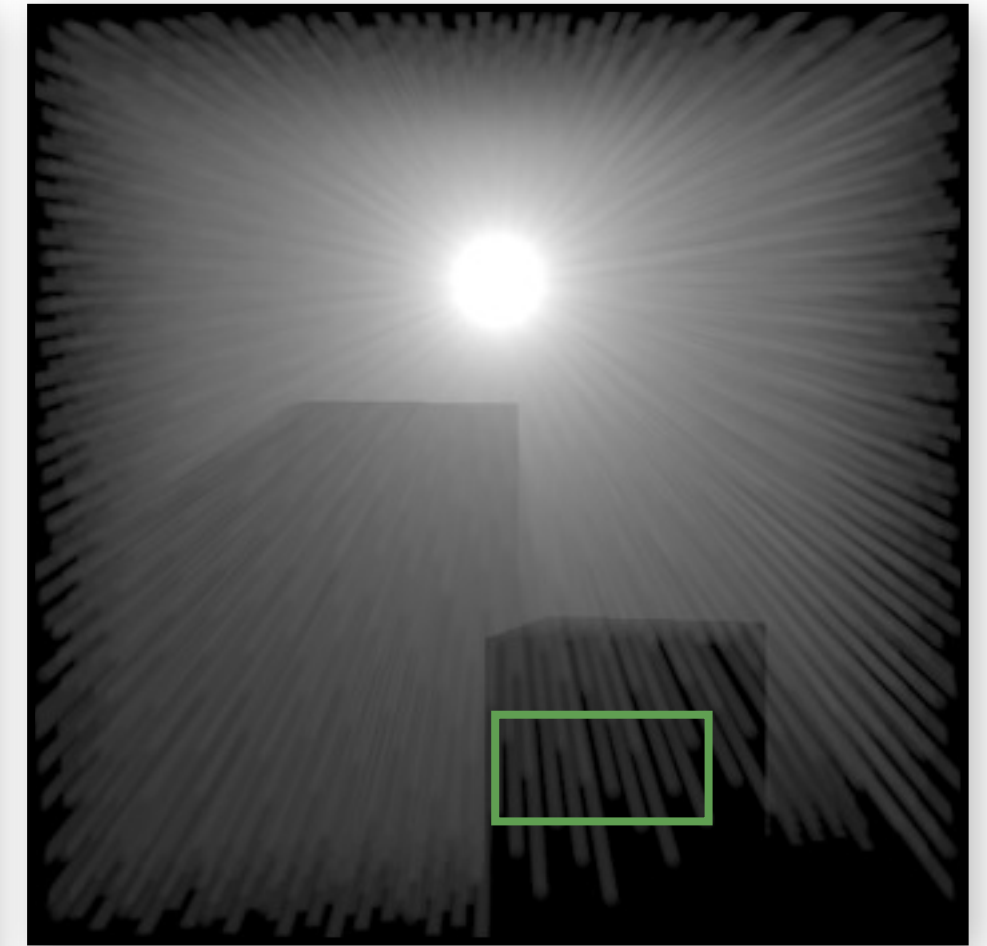
100k Photon Points



Ground Truth



5k Photon Beams





# Beam Queries with Photon Beams

- Beam Query x Beam Data (3D)
- Beam Query x Beam Data (2D)<sub>1</sub>
- Beam Query x Beam Data (2D)<sub>2</sub>
- Beam Query x Beam Data (1D)

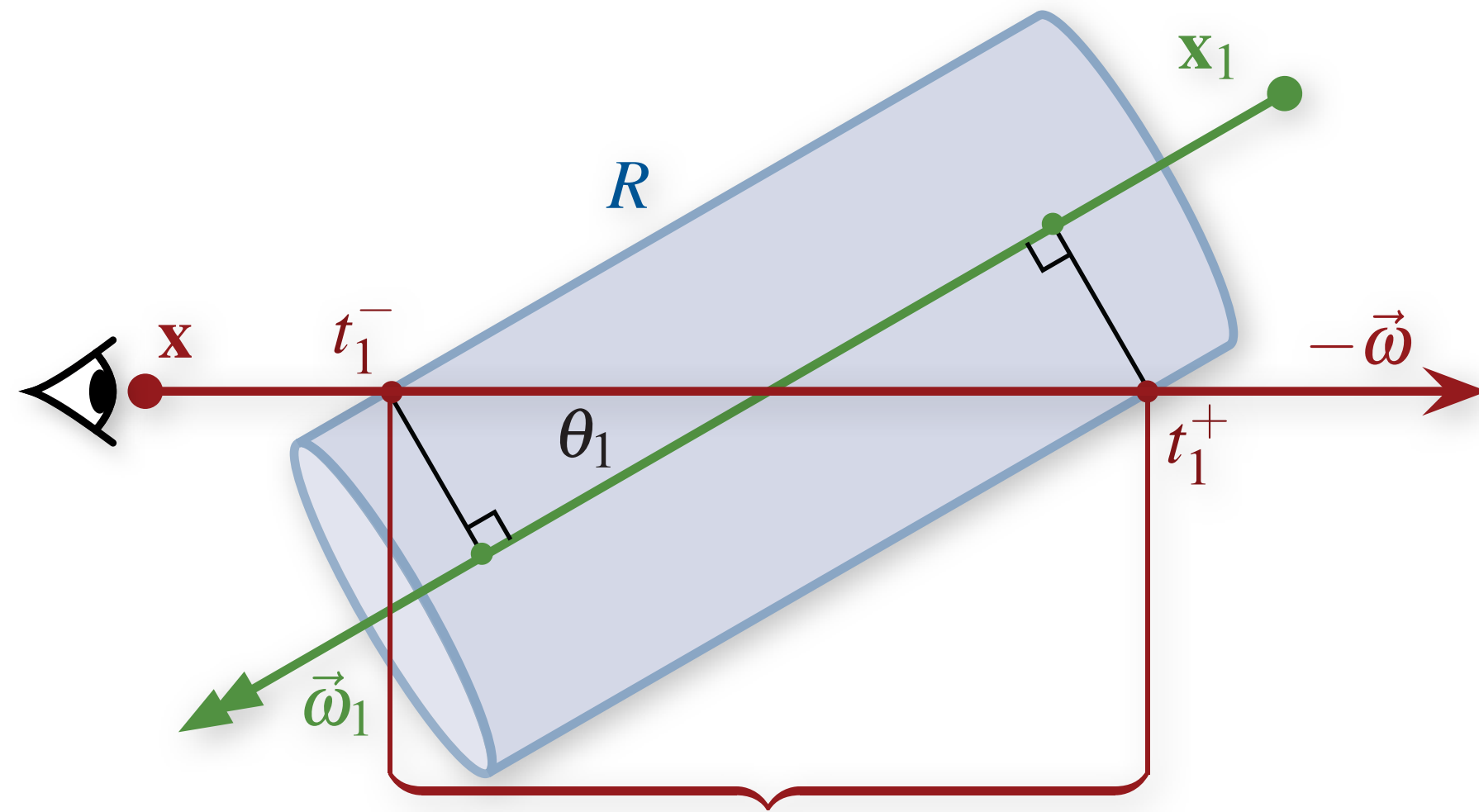


# Beam Query $\times$ Beam Data (2D blur)



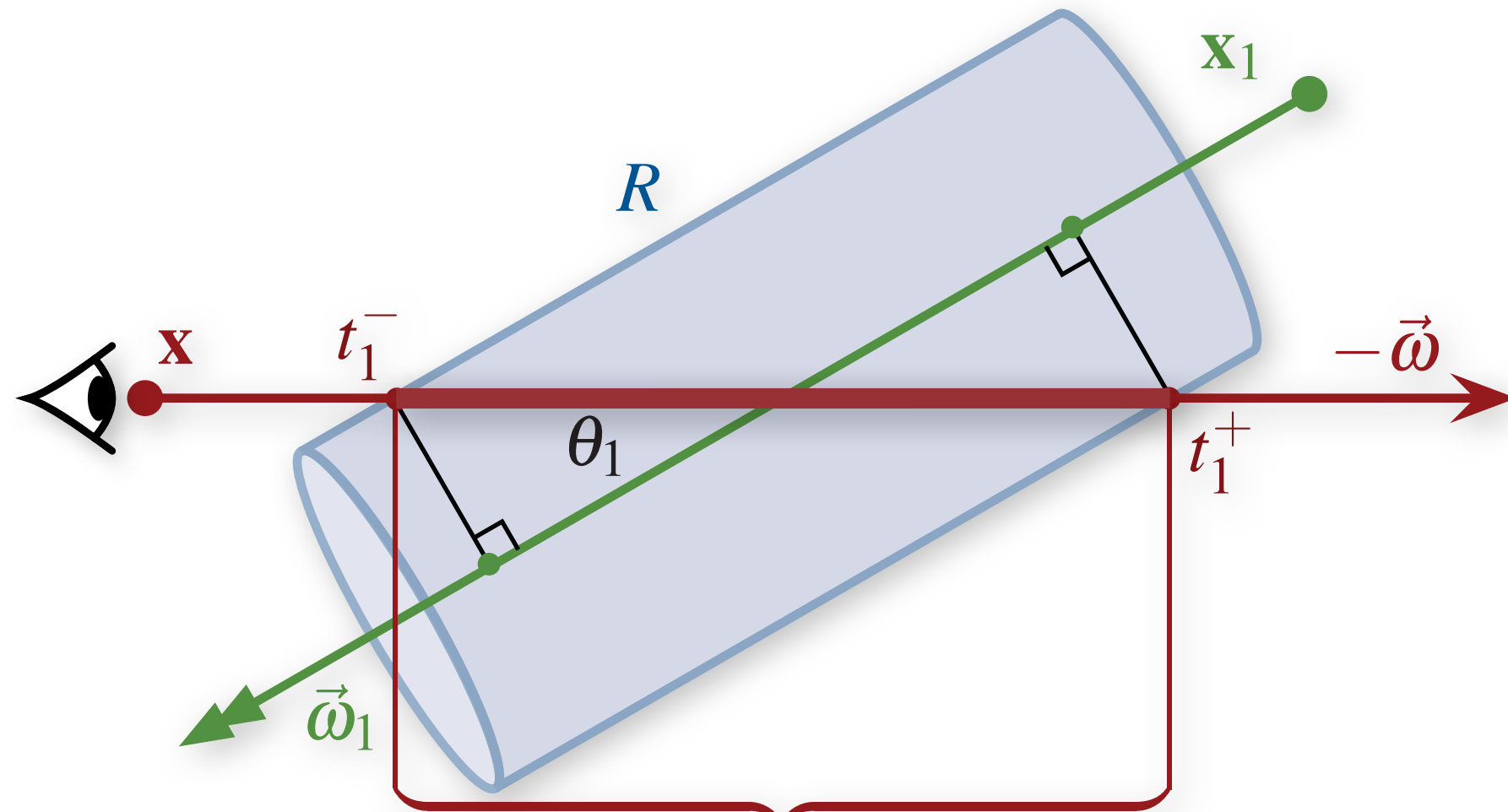


# Beam Query $\times$ Beam Data (2D blur)



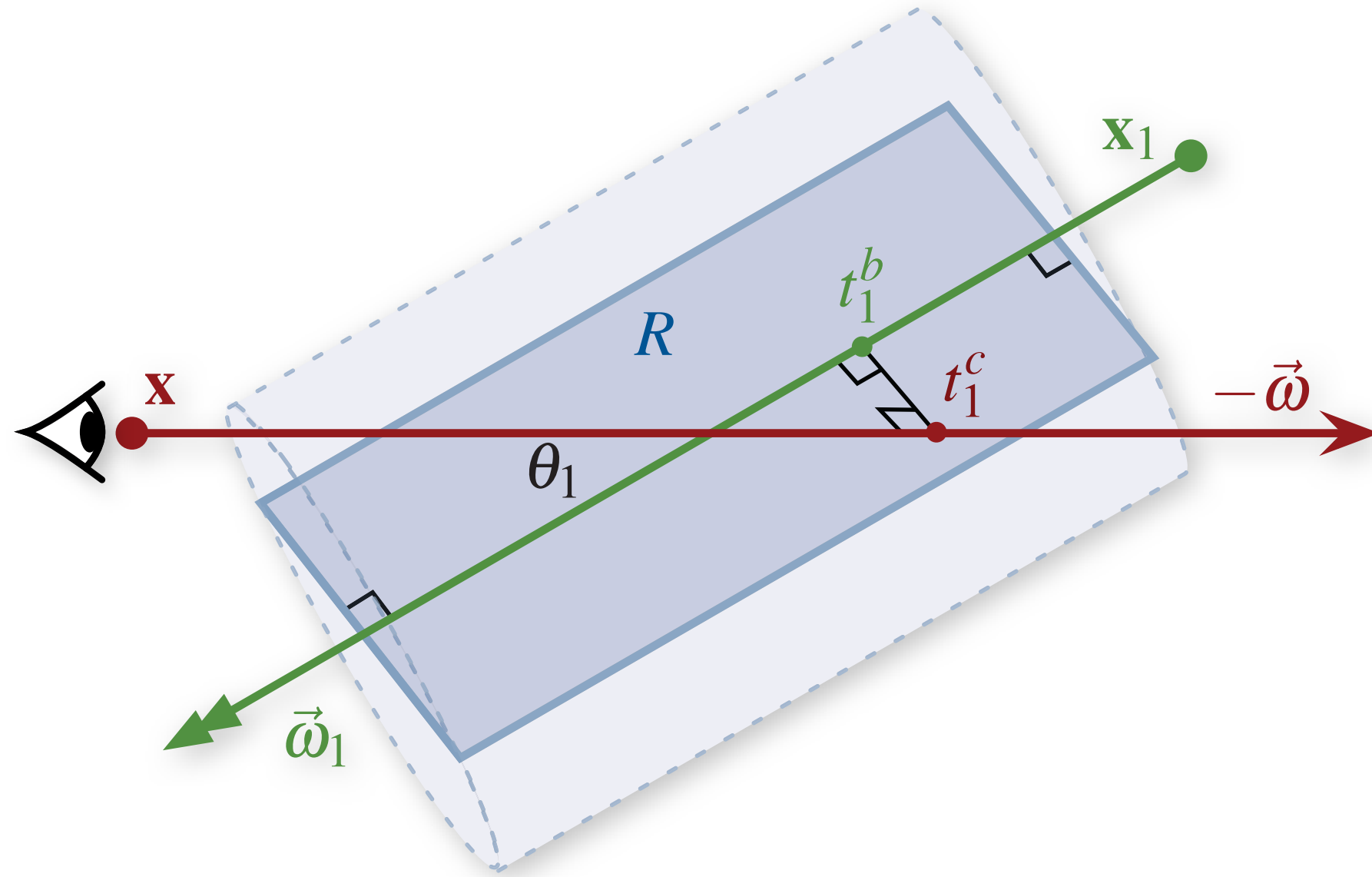
$$L \approx \frac{\sigma_s}{\mu_R(r^2)} \sum_i f(\theta_i) \Phi_i \int_{t_i^-}^{t_i^+} e^{-\sigma_t t_c} e^{-\sigma_t t_b} dt_c$$

# Beam Query $\times$ Beam Data (2D blur)



$$L \approx \frac{\sigma_s}{\mu_R(r^2)} \sum_i f(\theta_i) \Phi_i \int_{t_i^-}^{t_i^+} e^{-\sigma_t t_c} e^{-\sigma_t t_b} dt_c$$

# Beam Query × Beam Data (1D blur)



$$L \approx \frac{\sigma_s}{\mu_R(r)} \sum_i \frac{f(\theta_i) \Phi_i e^{-\sigma_t t_i^c} e^{-\sigma_t t_i^b}}{\sin \theta_i}$$



# Radiance Estimator Summary



# Radiance Estimator Summary

- Beam queries remove ray marching





# Radiance Estimator Summary

- Beam queries remove ray marching
- Beam data increases data density



# Radiance Estimator Summary

- Beam queries remove ray marching
- Beam data increases data density
- Lower blur dimension reduces bias and computation



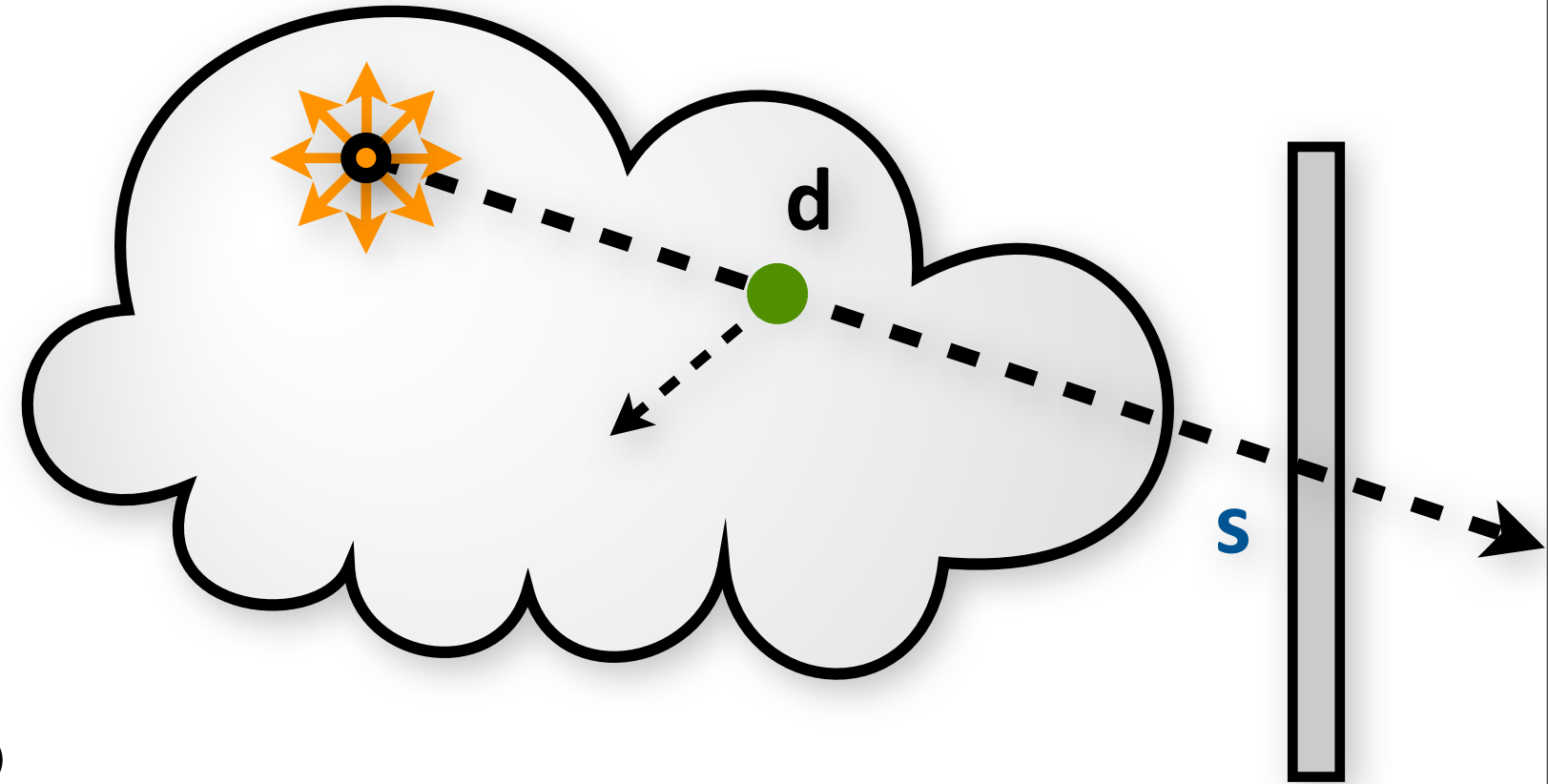
# Radiance Estimator Summary

- Beam queries remove ray marching
- Beam data increases data density
- Lower blur dimension reduces bias and computation
- **use: Beam Query x Beam Data (1D)**



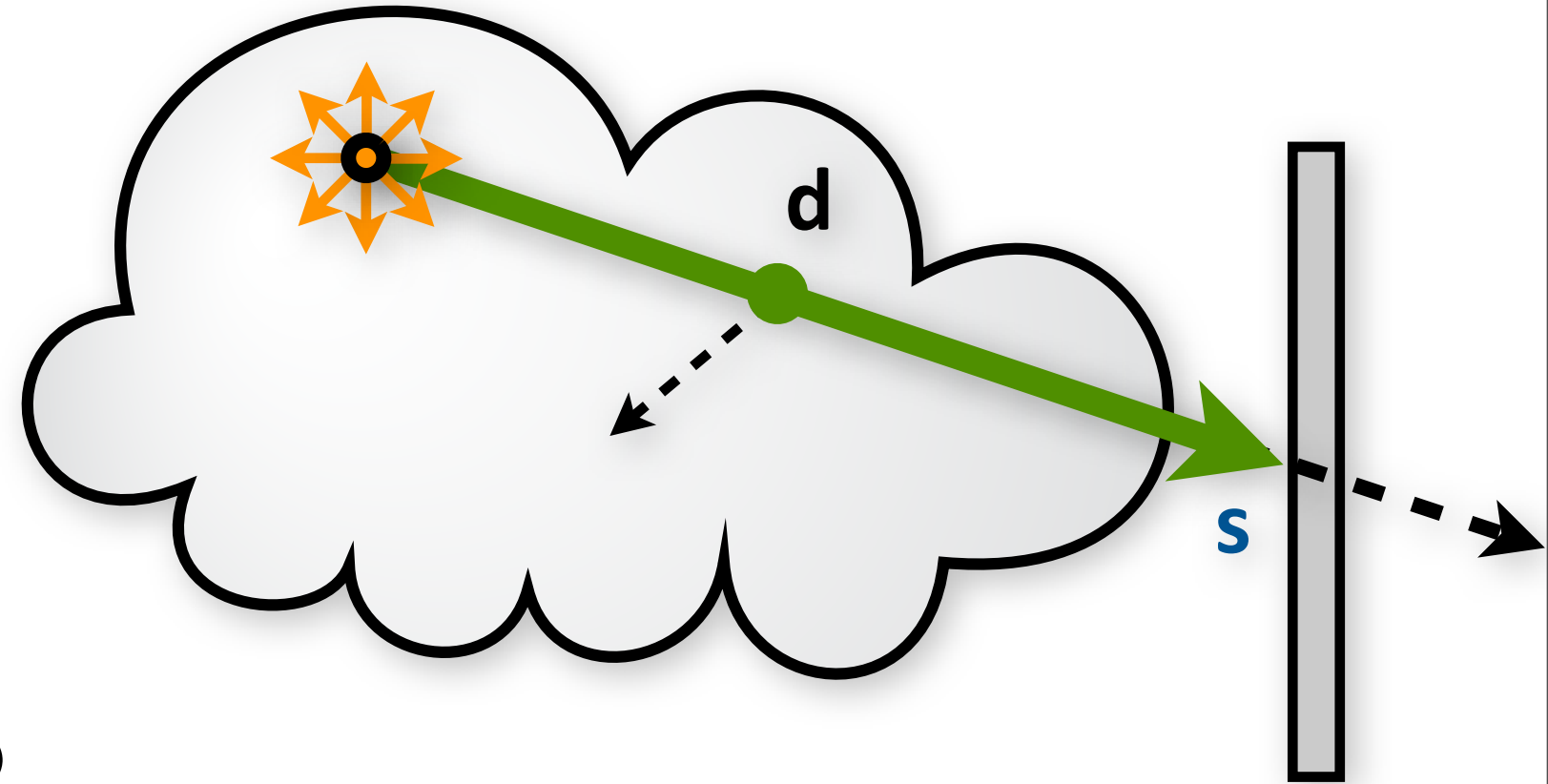
# Basic Volumetric Photon Tracer

```
void vPT(o,  $\omega$ ,  $\phi$ )  
  s = nearestSurfaceHit(o,  $\omega$ )  
  d = freeFlightDistance(o,  $\omega$ )  
  if (d < s) // media scattering  
    o += d *  $\omega$  // propagate photon  
    storeVolumePhoton(o,  $\omega$ ,  $\phi$ )  
    return vPT(o, samplePDF(),  $\phi * \sigma_s / \sigma_t$ )  
  else // surface scattering  
    o += s *  $\omega$  // propagate photon  
    storeSurfacePhoton(o,  $\omega$ ,  $\phi$ )  
    ( $\omega_i$ , pdfi) = sampleBRDF(o,  $\omega$ )  
    return vPT(o,  $\omega_i$ ,  $\phi * \text{BRDF}(o, \omega, \omega_i) / \text{pdf}_i$ )
```



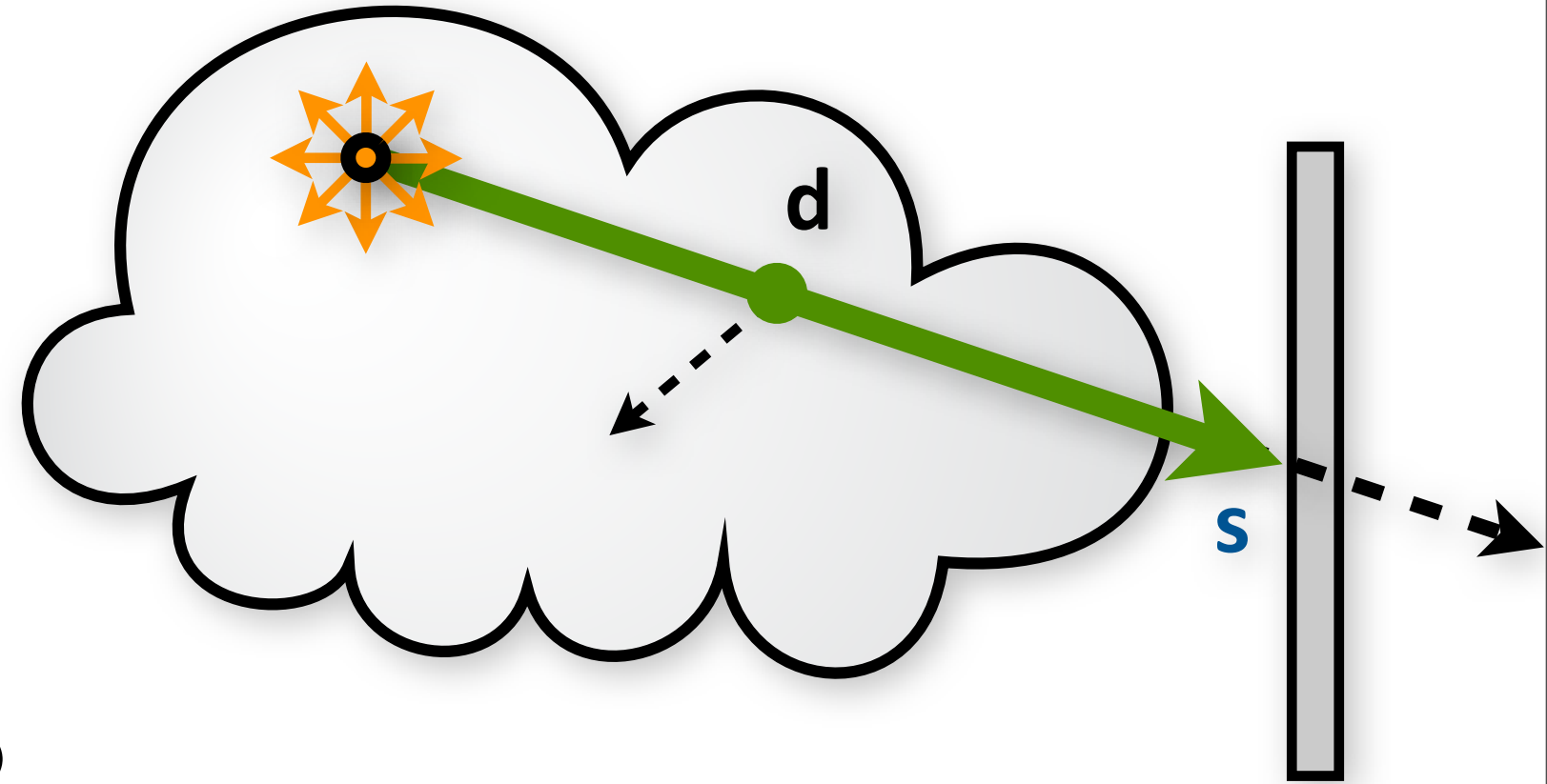
# Basic Volumetric Photon Tracer

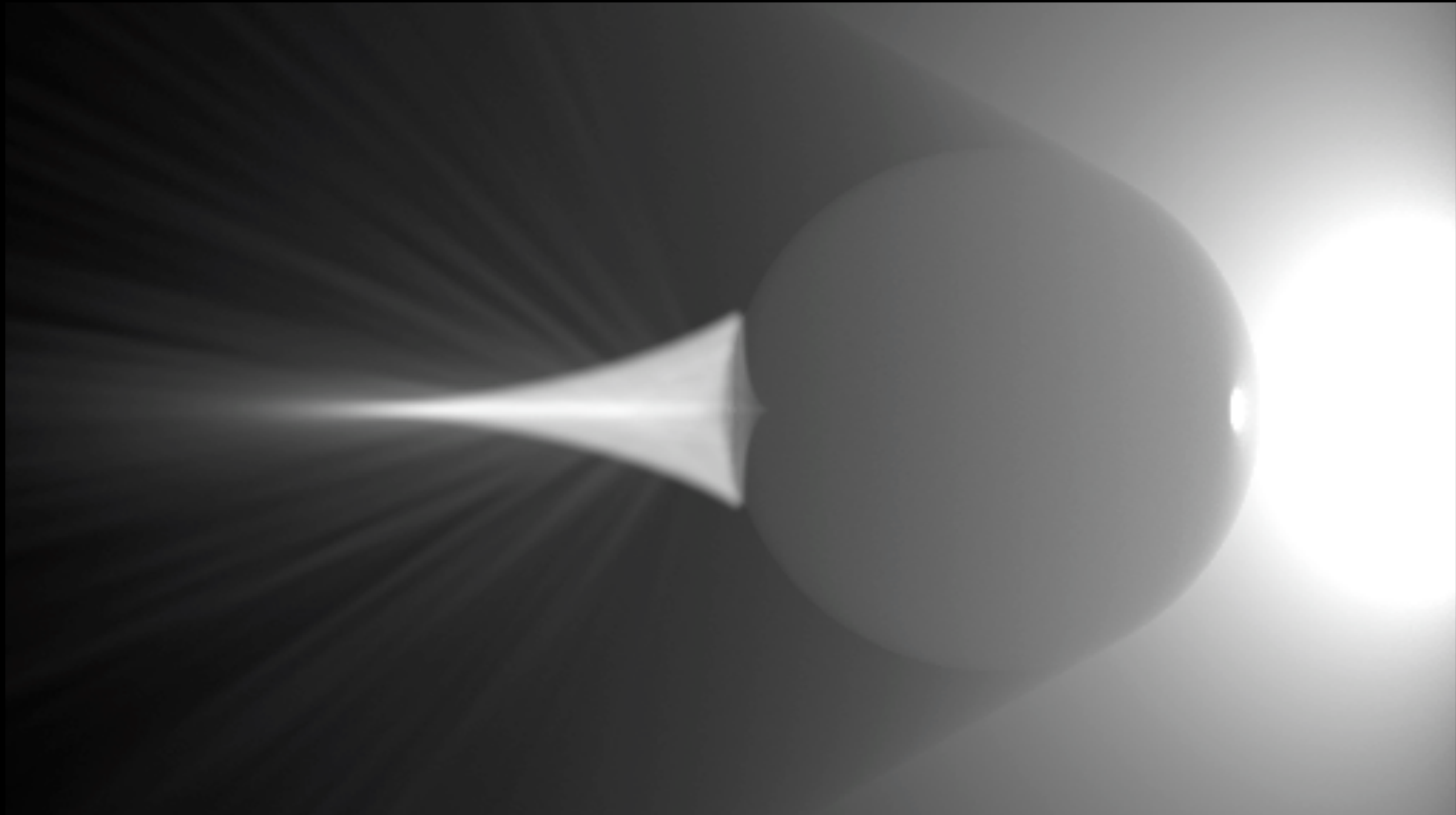
```
void vPT(o,  $\omega$ ,  $\phi$ )
  s = nearestSurfaceHit(o,  $\omega$ )
  storeVolumePhoton(o,  $\omega$ ,  $\phi$ )
  d = freeFlightDistance(o,  $\omega$ )
  if (d < s)           // media scattering
    o += d *  $\omega$       // propagate photon
    return vPT(o, samplePF(),  $\phi * \sigma_s / \sigma_t$ )
  else                 // surface scattering
    o += s *  $\omega$      // propagate photon
    storeSurfacePhoton(o,  $\omega$ ,  $\phi$ )
    ( $\omega_i$ , pdfi) = sampleBRDF(o,  $\omega$ )
    return vPT(o,  $\omega_i$ ,  $\phi * \text{BRDF}(o, \omega, \omega_i) / \text{pdf}_i$ )
```

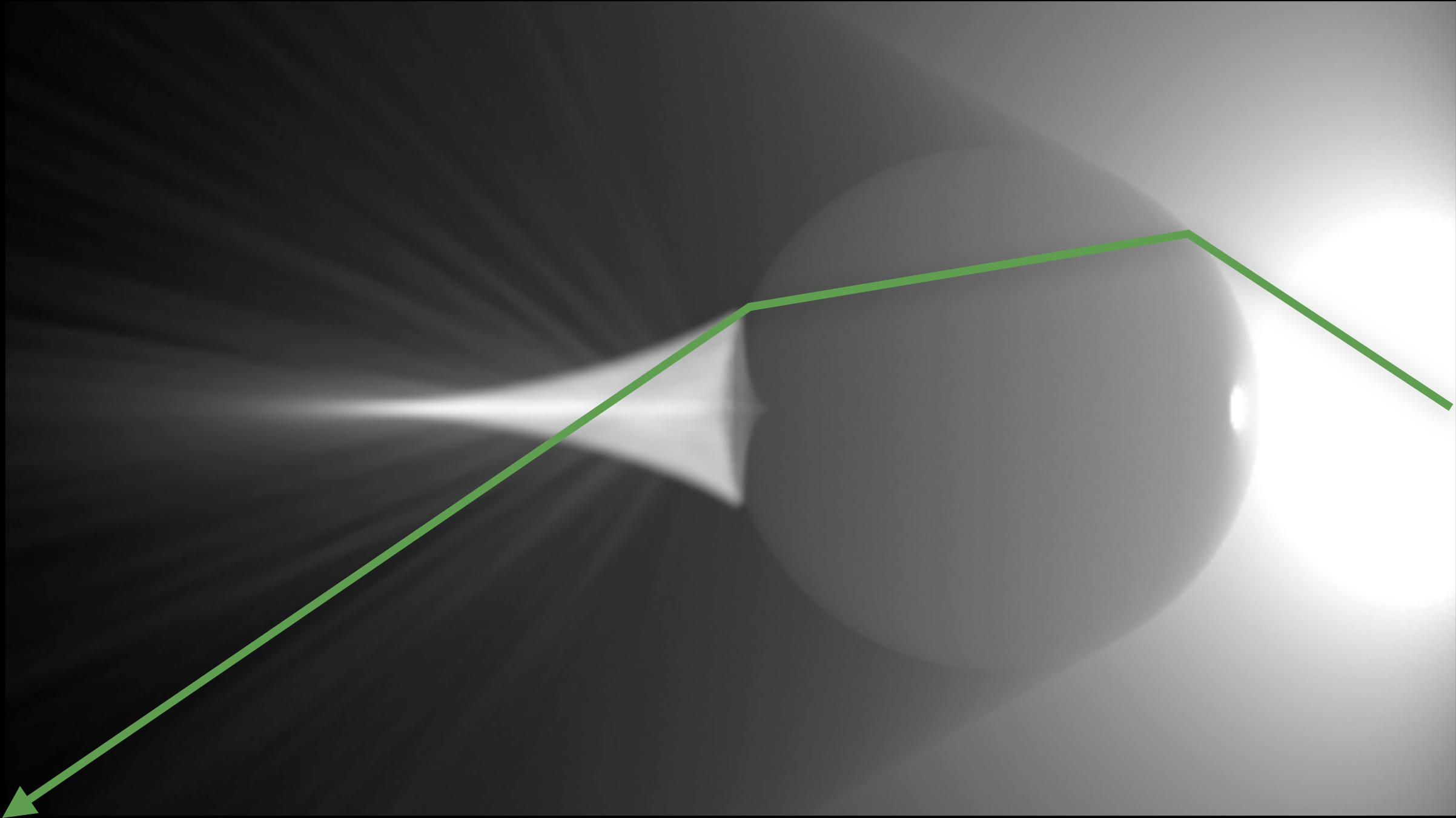


# Basic Volumetric Photon Tracer

```
void vPT(o,  $\omega$ ,  $\phi$ )
  s = nearestSurfaceHit(o,  $\omega$ )
  storePhotonBeam(o,  $\omega$ , s,  $\phi$ )
  d = freeFlightDistance(o,  $\omega$ )
  if (d < s)           // media scattering
    o += d* $\omega$        // propagate photon
    return vPT(o, samplePDF(),  $\phi * \sigma_s / \sigma_t$ )
  else                 // surface scattering
    o += s* $\omega$        // propagate photon
    storeSurfacePhoton(o,  $\omega$ ,  $\phi$ )
    ( $\omega_i$ , pdf $_i$ ) = sampleBRDF(o,  $\omega$ )
    return vPT(o,  $\omega_i$ ,  $\phi * \text{BRDF}(o, \omega, \omega_i) / \text{pdf}_i$ )
```

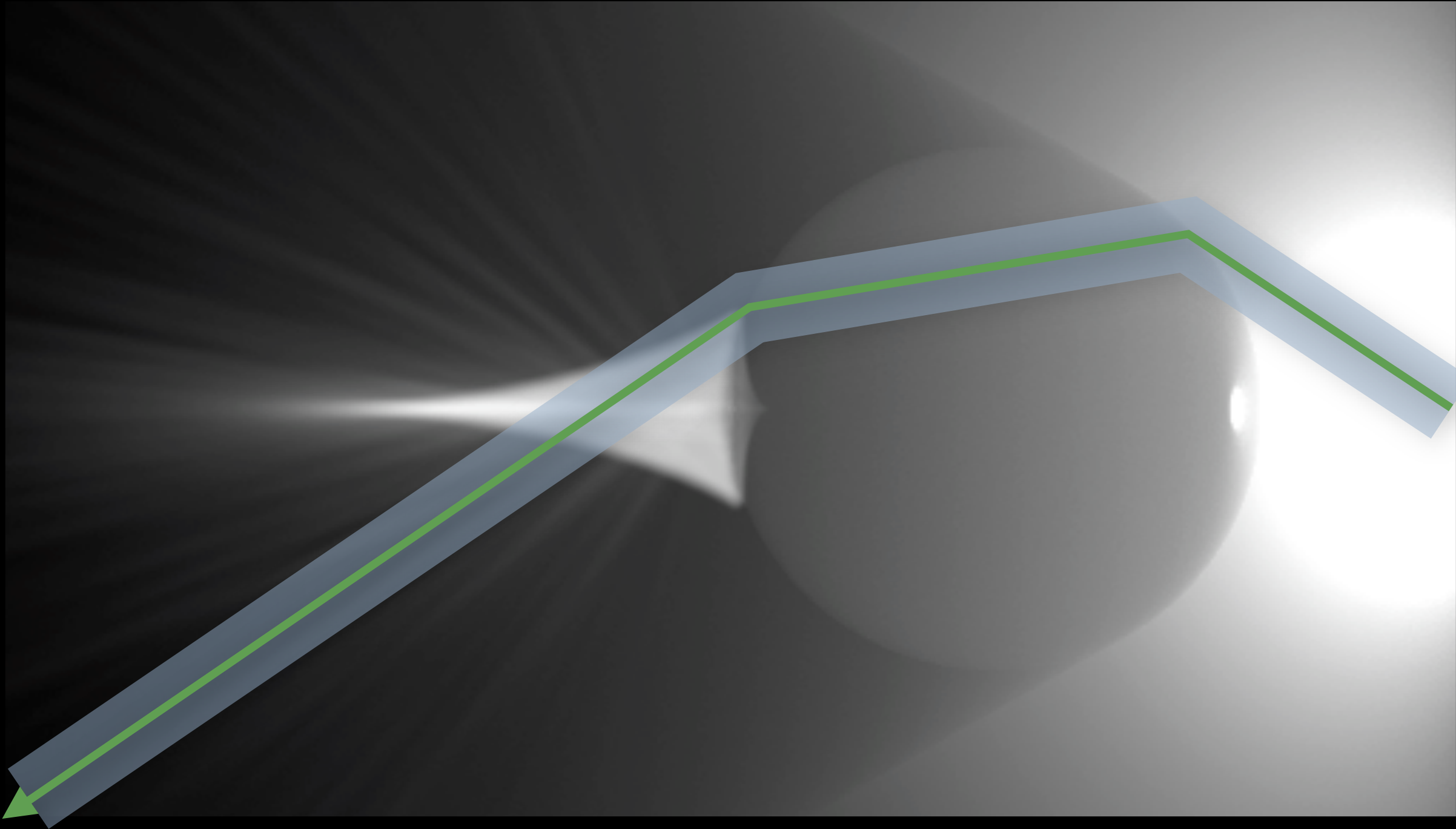




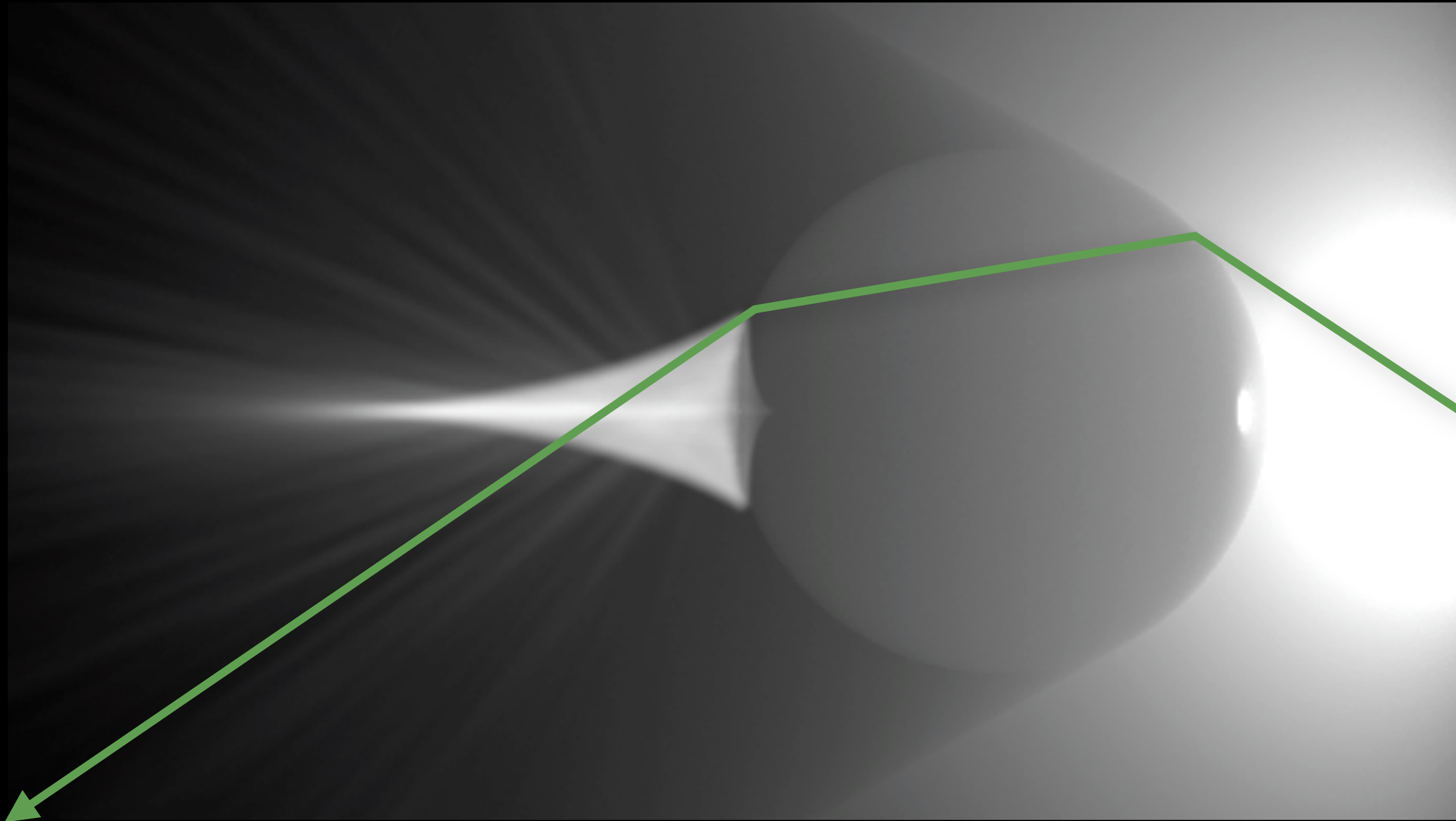




# Fixed-width Beams

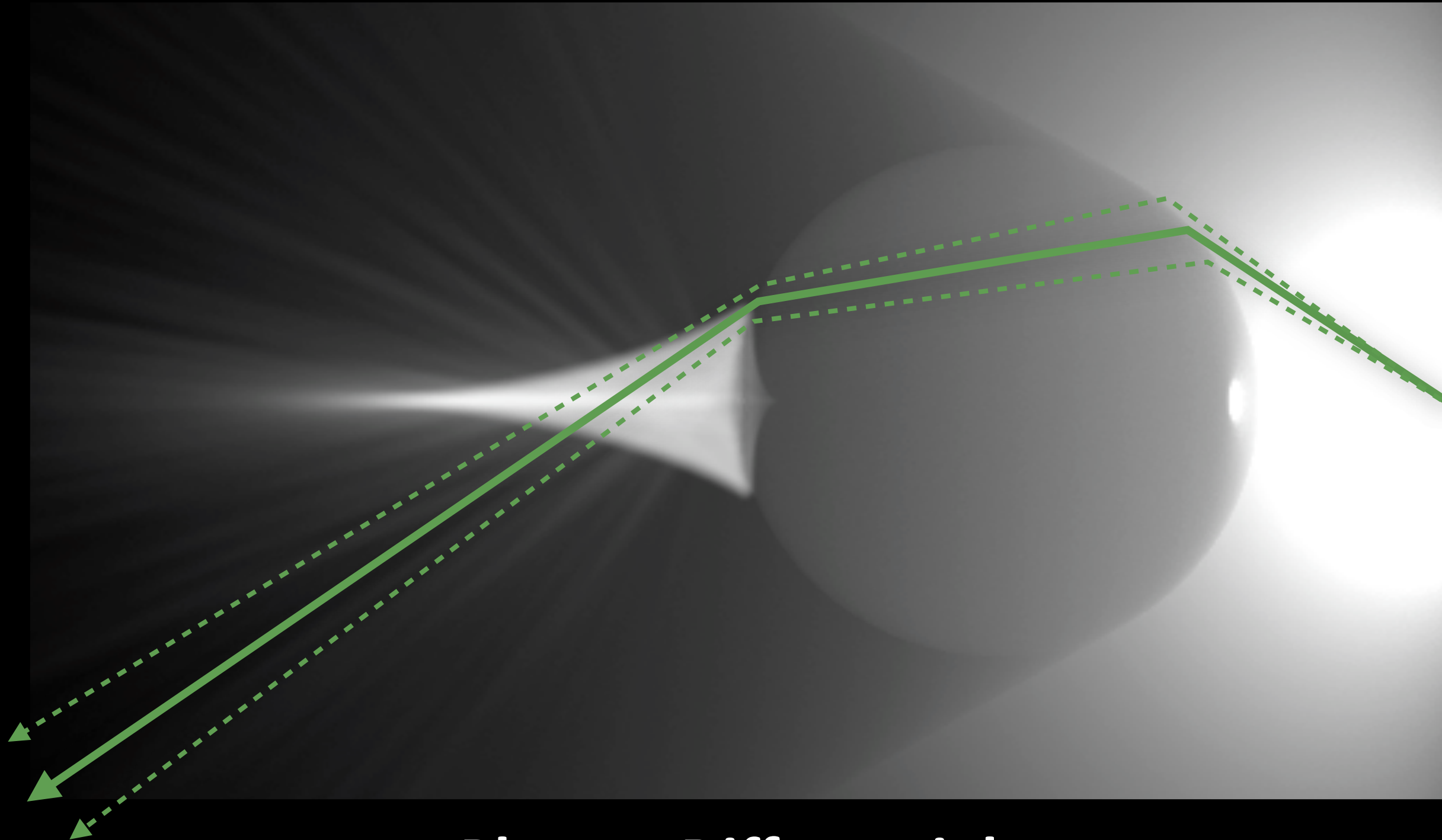


# Fixed-width Beams



**Photon Differentials**  
[Igehy 99, Schjøth et al. 07]

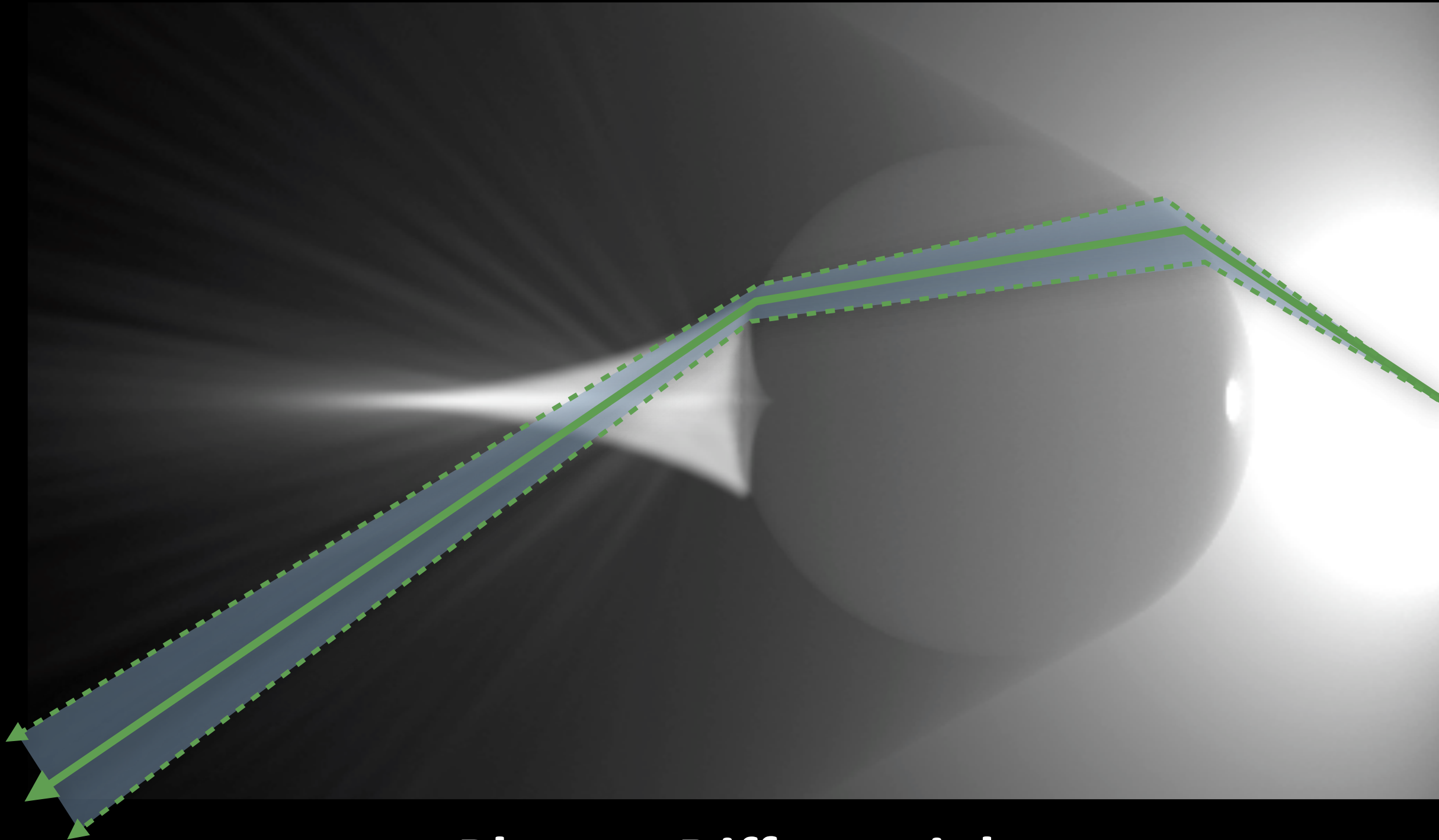
# Fixed-width Beams



**Photon Differentials**

[Igehy 99, Schjøth et al. 07]

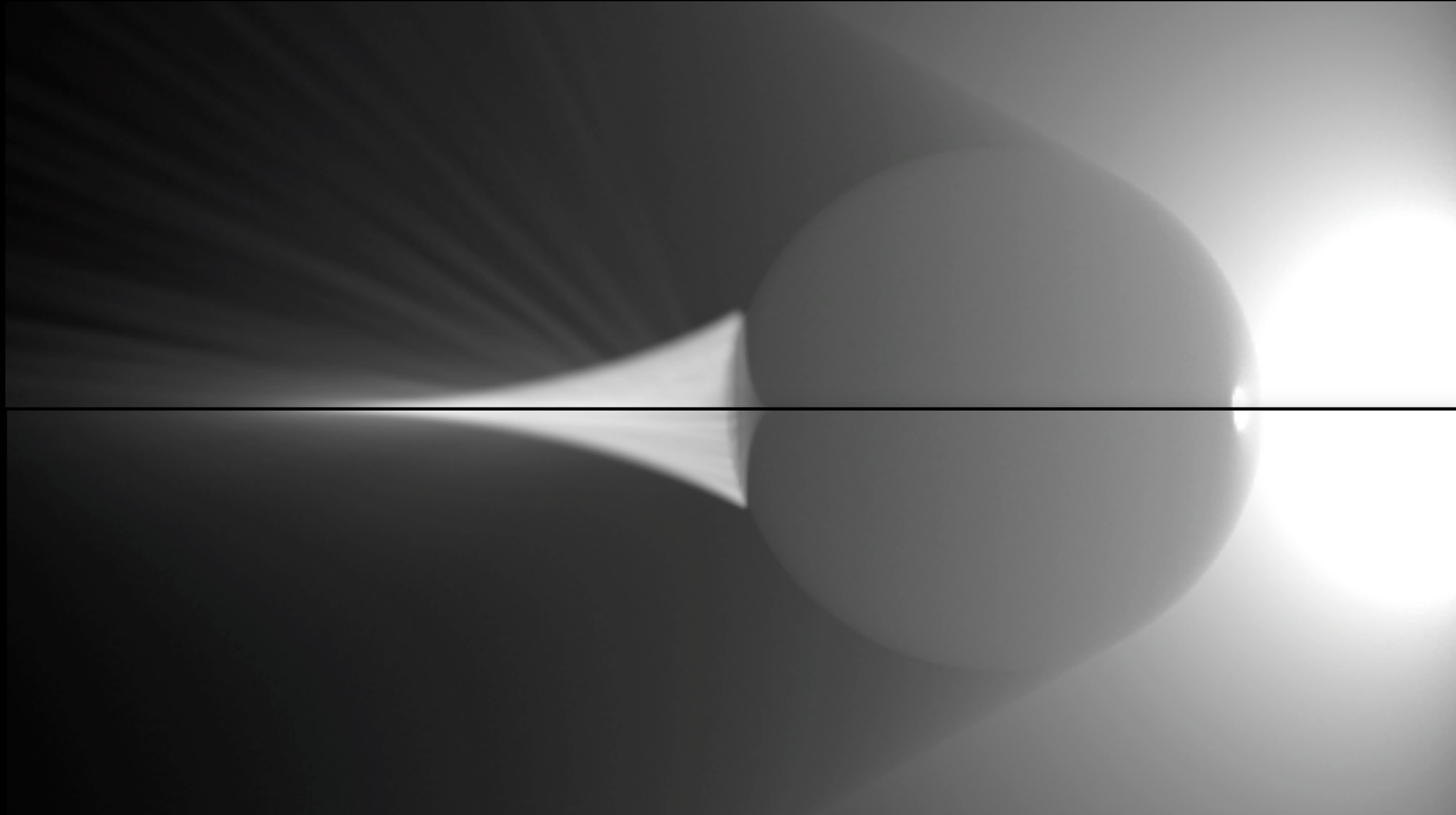
# Fixed-width Beams



**Photon Differentials**

[Igehy 99, Schjøth et al. 07]

# Fixed-width Beams



# Adaptive-width Beams



# Rendering



# Rendering

- Need to intersect each ray with all photon beams (expensive!)



# Rendering

- Need to intersect each ray with all photon beams (expensive!)
- Place photon beams in an acceleration structure





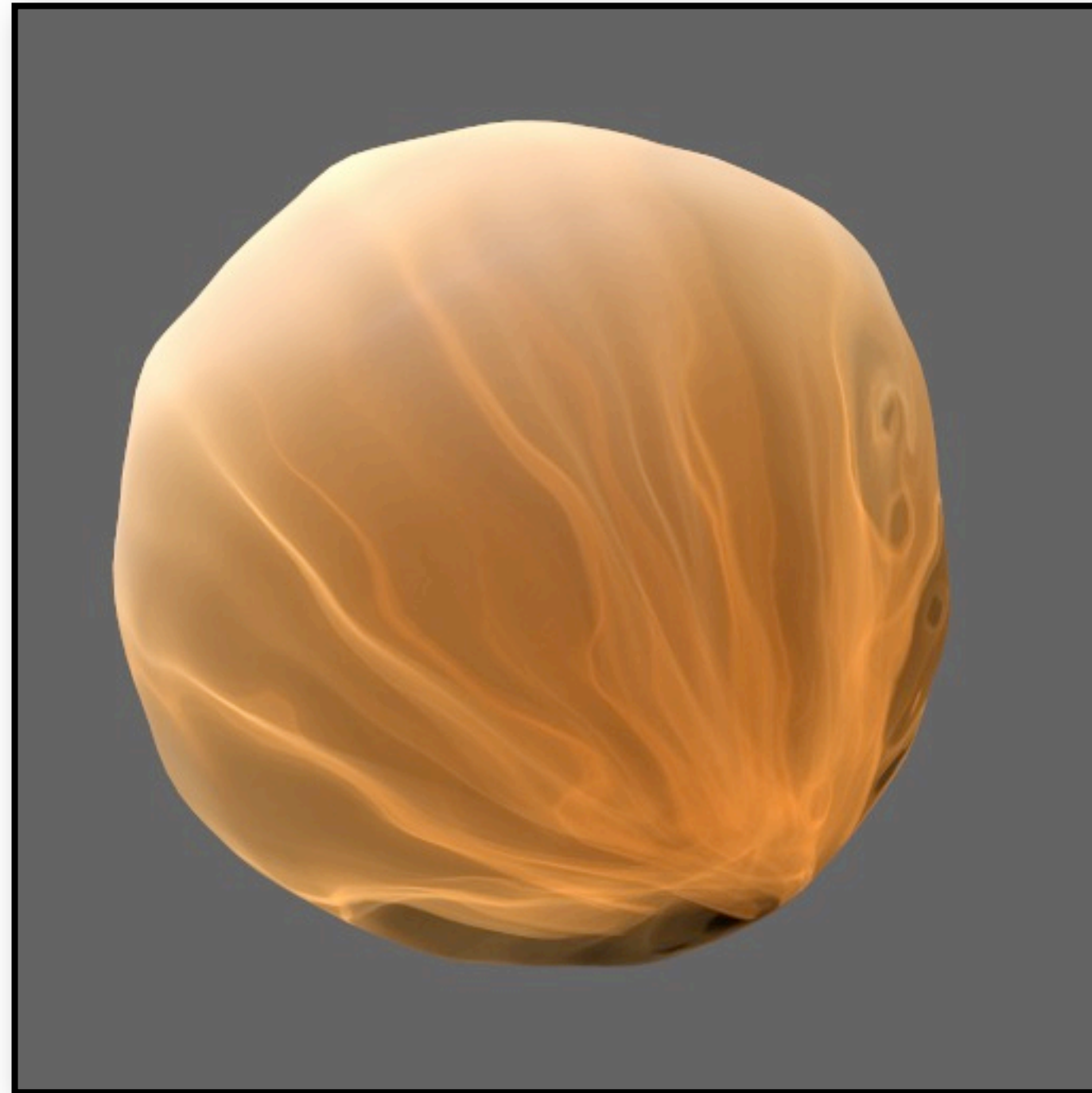
# Rendering

- Need to intersect each ray with all photon beams (expensive!)
- Place photon beams in an acceleration structure
- Rasterization (beams are just axial billboards!)



# Bumpy Sphere

courtesy of Bruce Walter

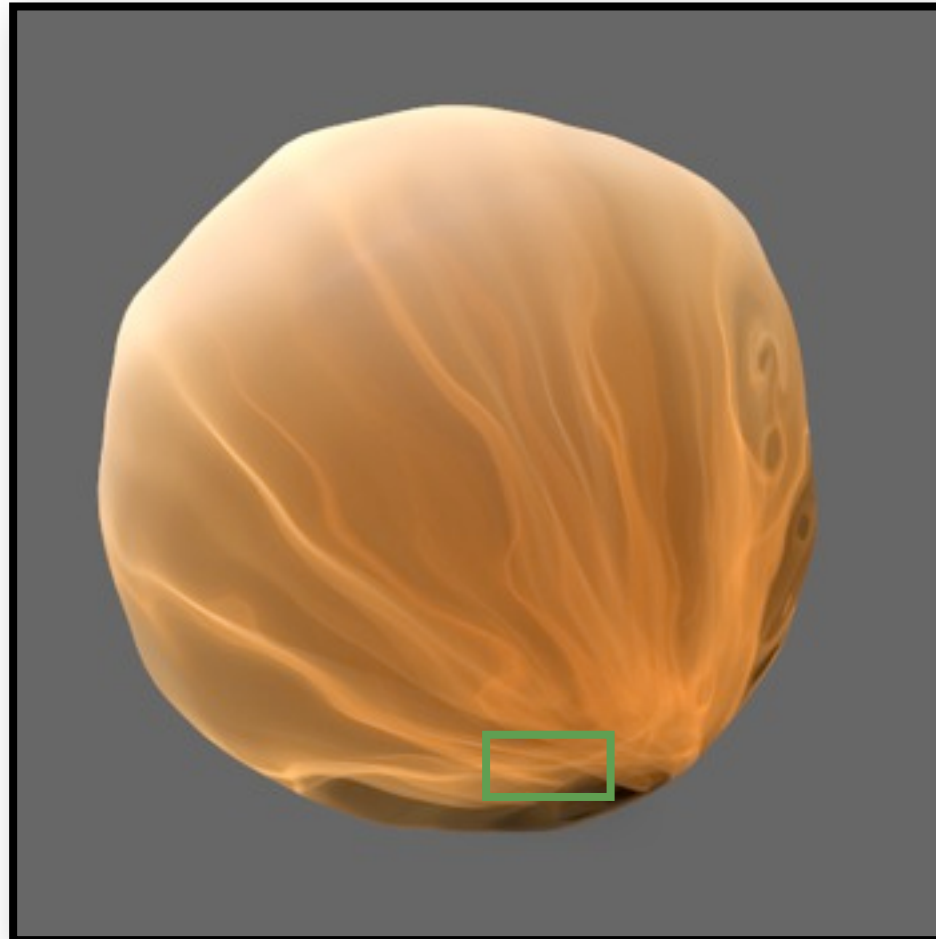




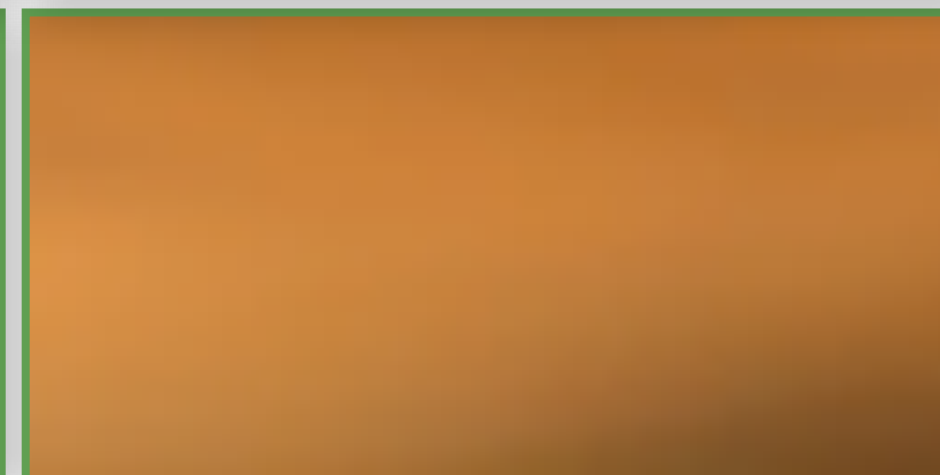
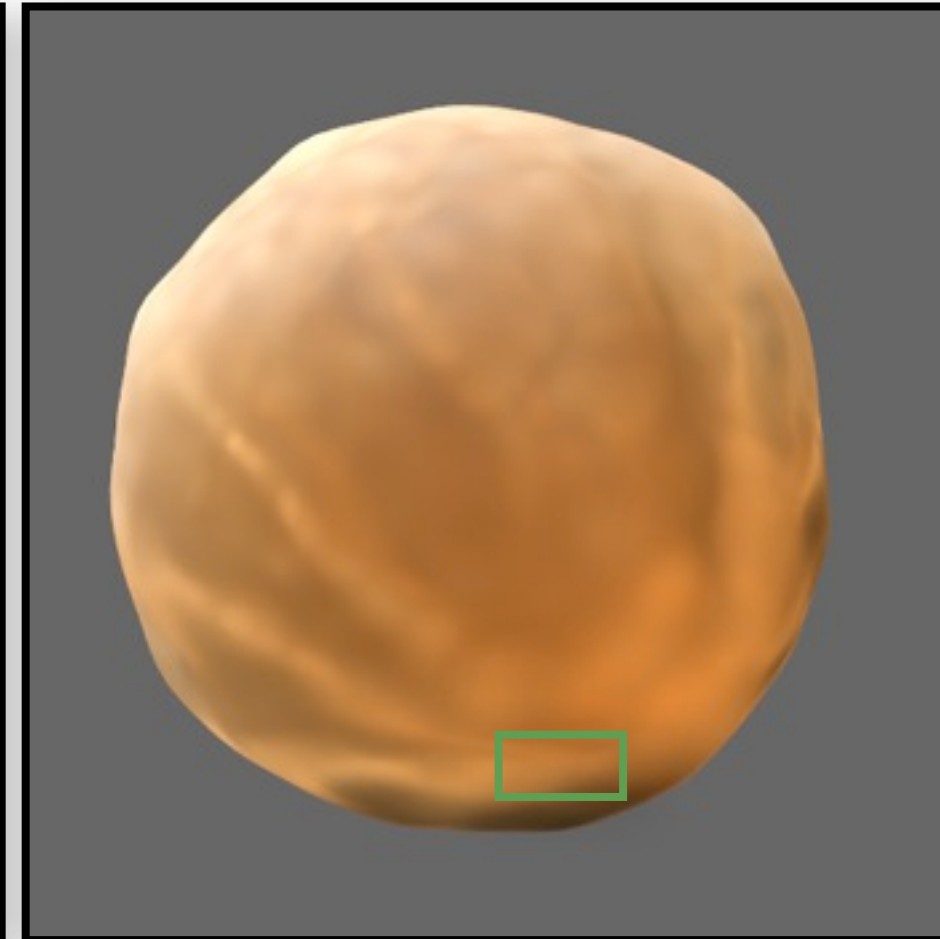
# Bumpy Sphere

courtesy of Bruce Walter

Ground Truth



90k Photon Points

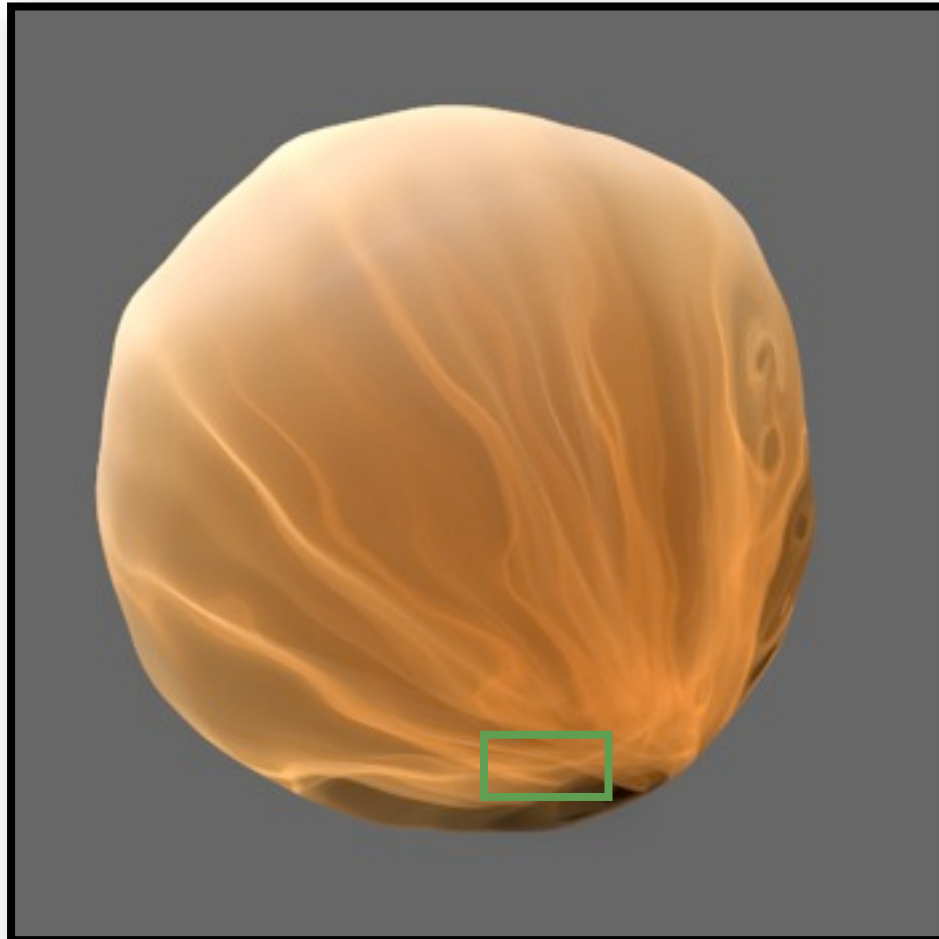




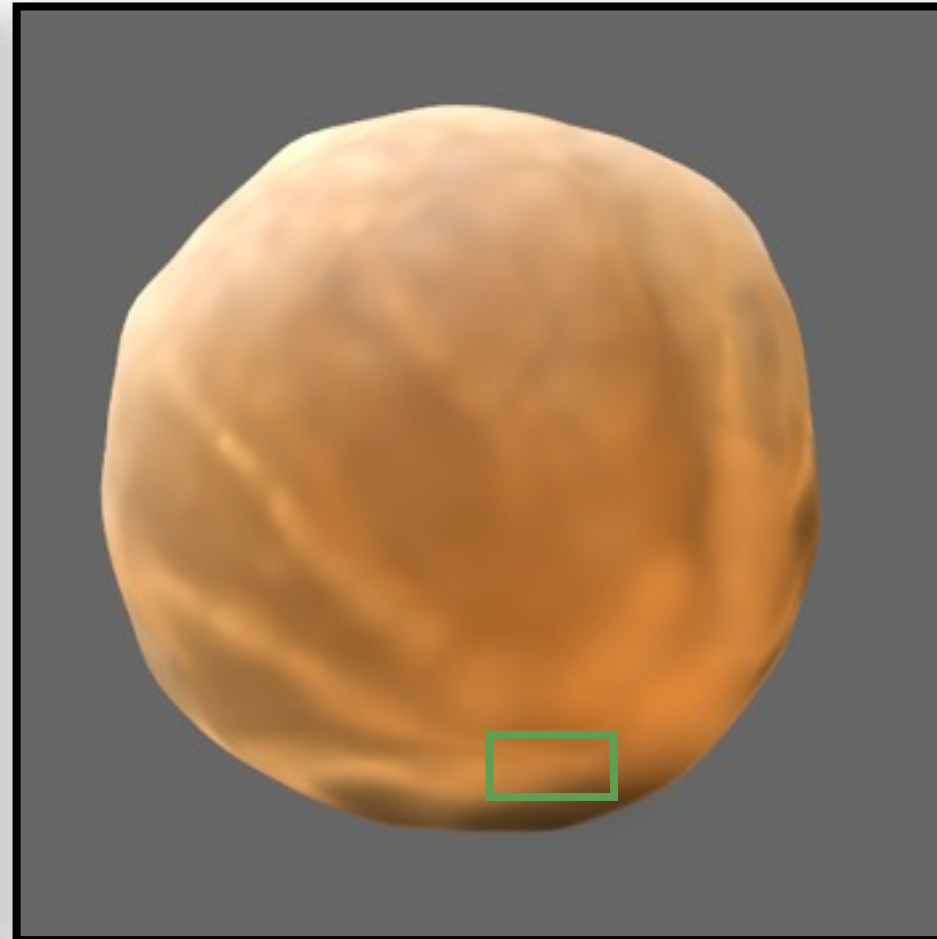
# Bumpy Sphere

courtesy of Bruce Walter

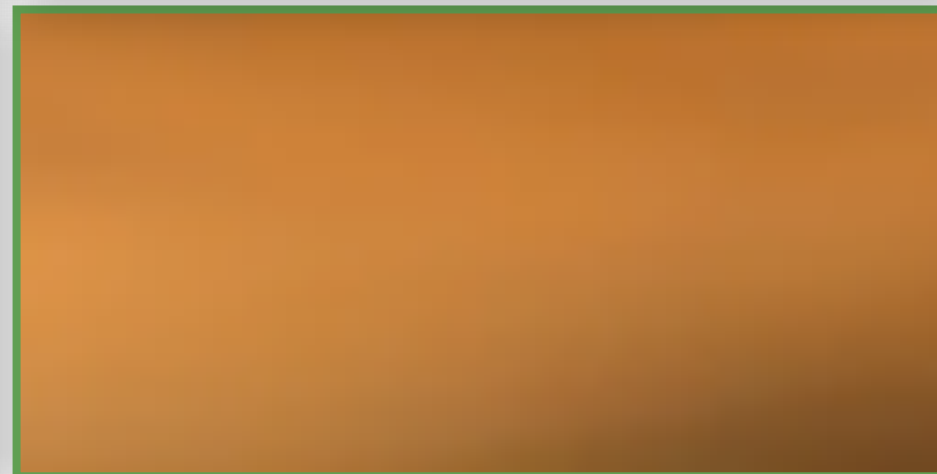
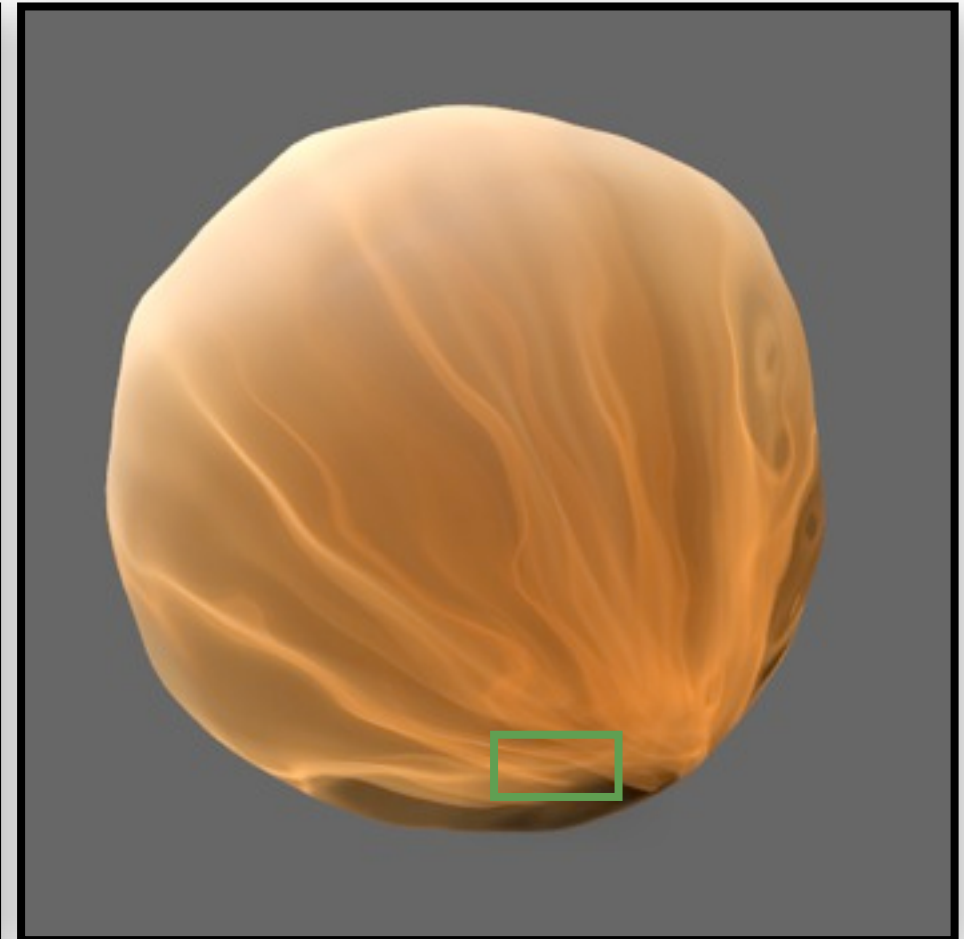
Ground Truth



90k Photon Points



90k Photon Beams



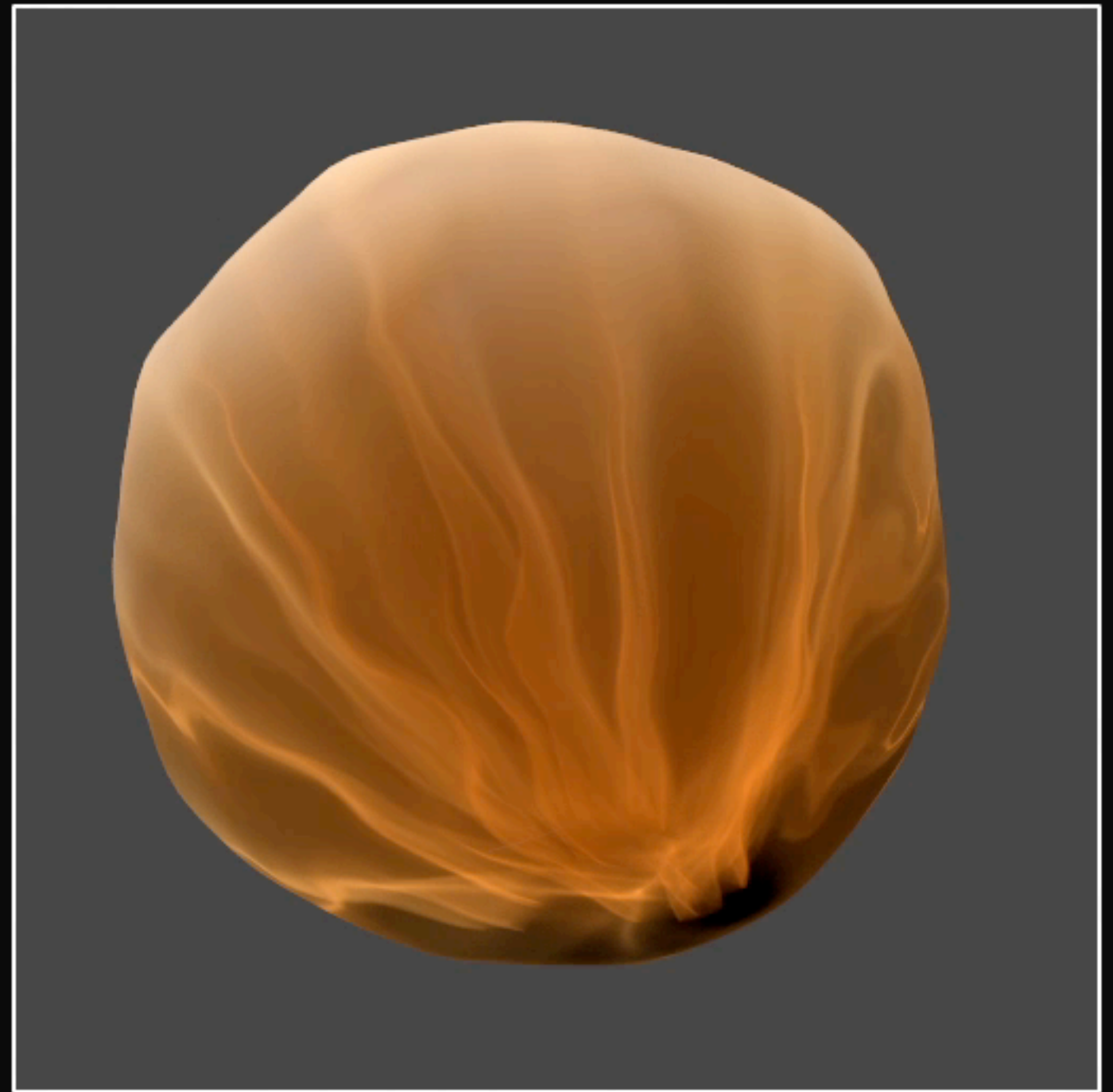
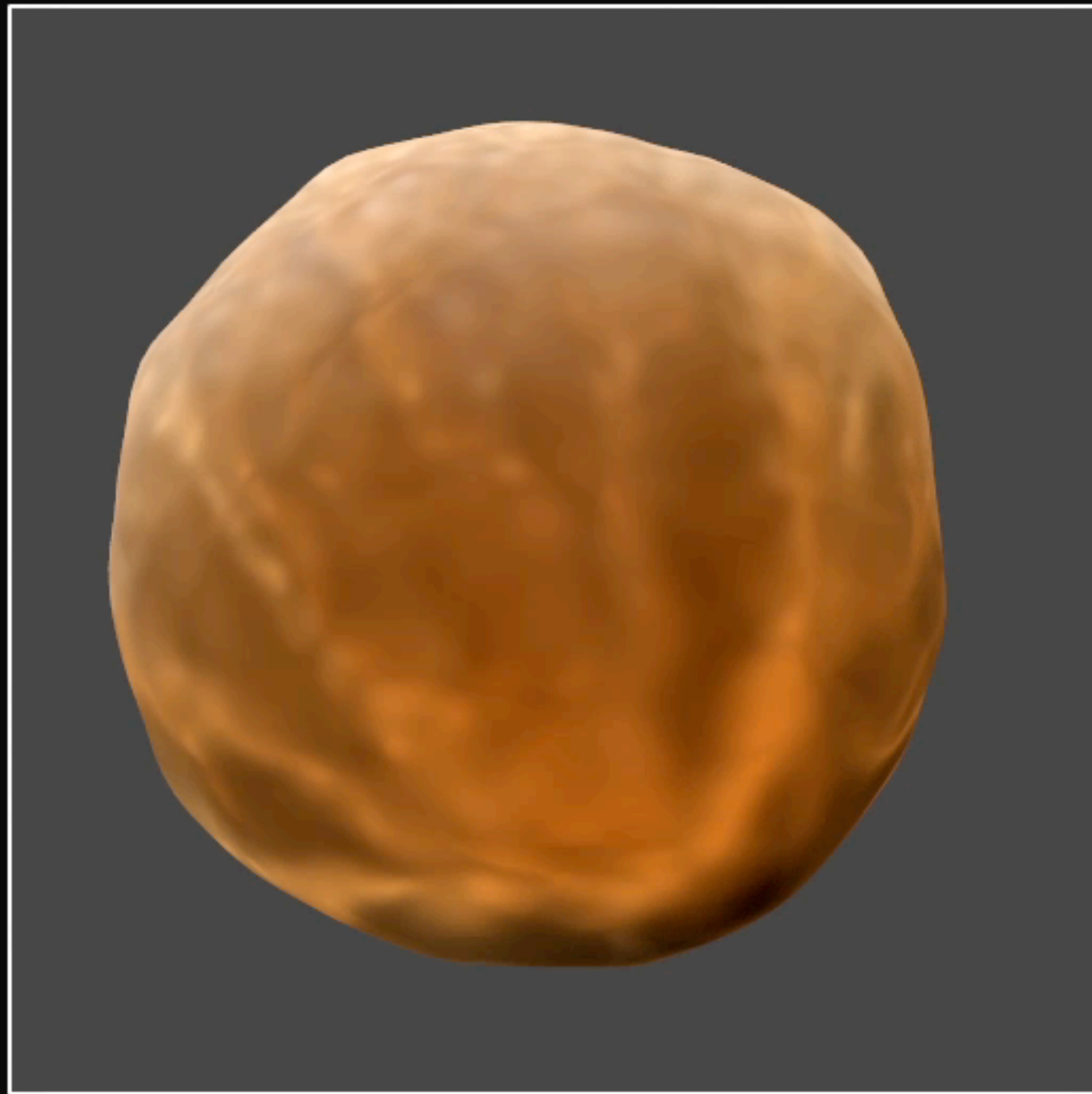
# Bumpy Sphere

Rendered at 512x512 with up to 16 samples/pixel

# Equal Photon Count

Photon Points

Photon Beams



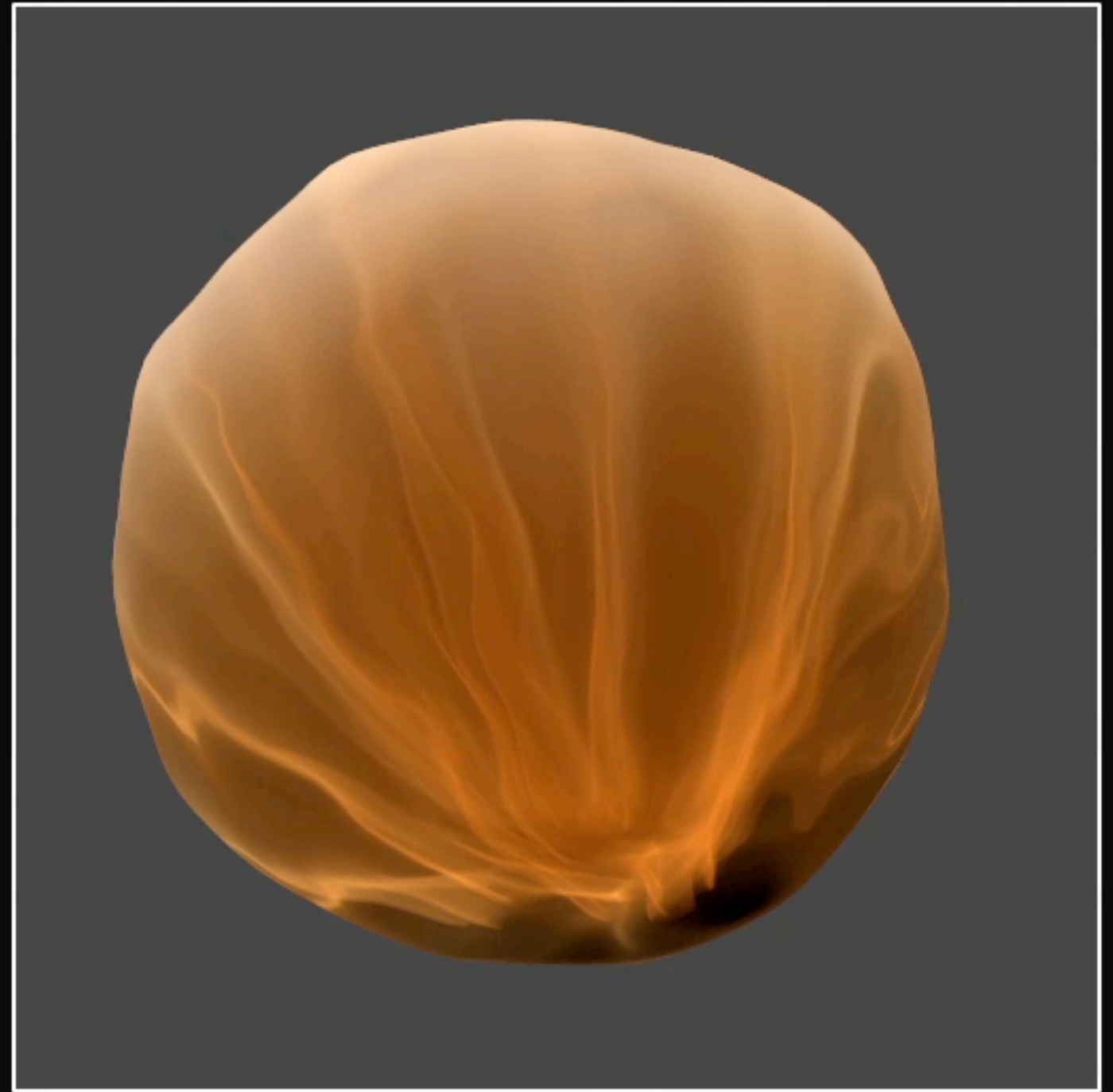
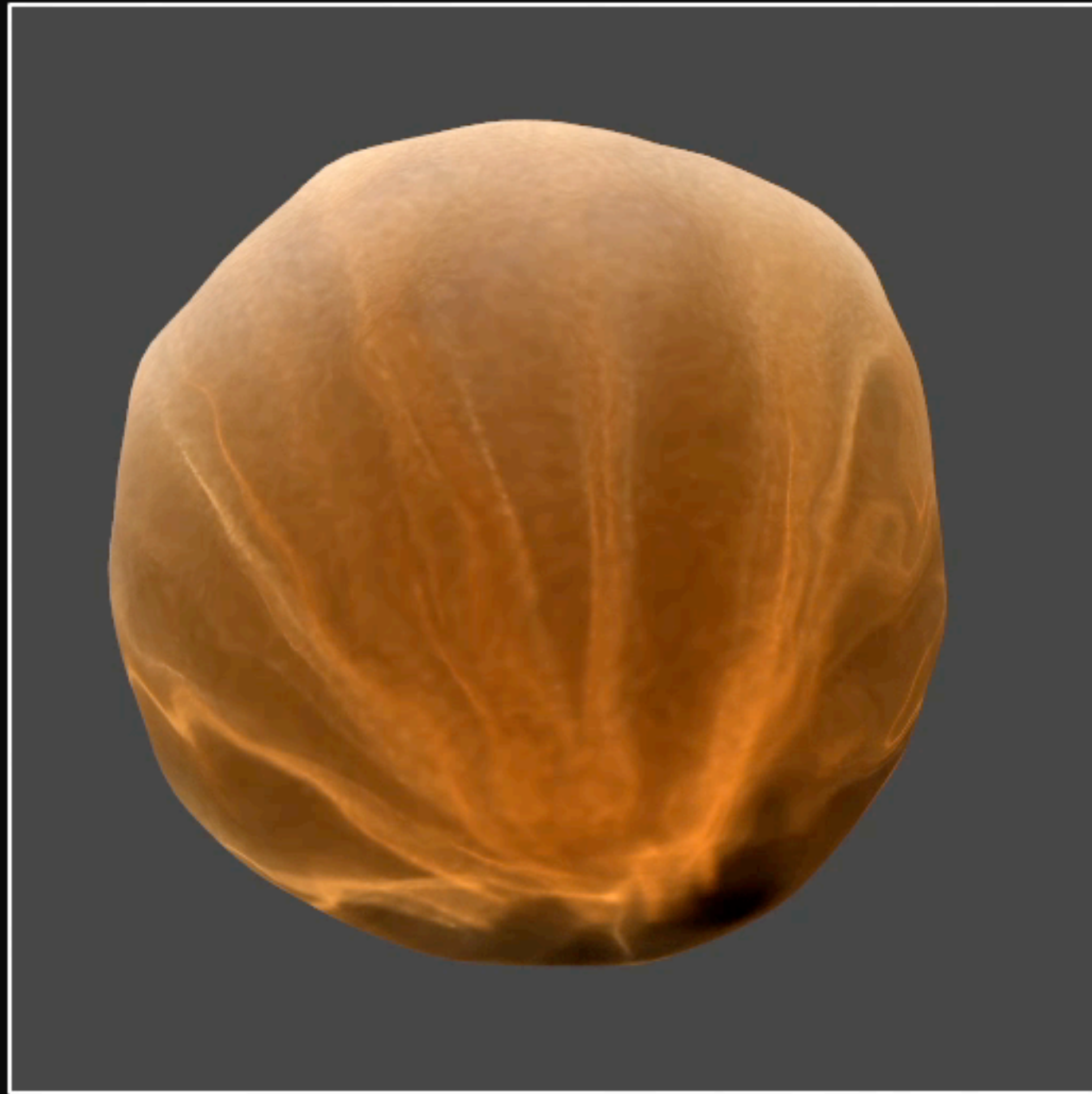
90K Photon **Points**  
~ 40 seconds/frame

90K Photon **Beams**  
~ 103 seconds/frame

# Equal Render Time

Photon Points

Photon Beams



1.3M Photon **Points**  
~ 101 seconds/frame

90K Photon **Beams**  
~ 103 seconds/frame

# Lighthouse

**Photon Points**



10K Photon **Points**  
~ 31 seconds/frame

**Roughly Equal Time**

**Photon Beams**



700 Photon **Beams**  
~ 25 seconds/frame





# Lighthouse

Jarosz et al. '08

Our Method

# Underwater Sun Beams

Rendered at 1024x576 with up to 16 samples/pixel

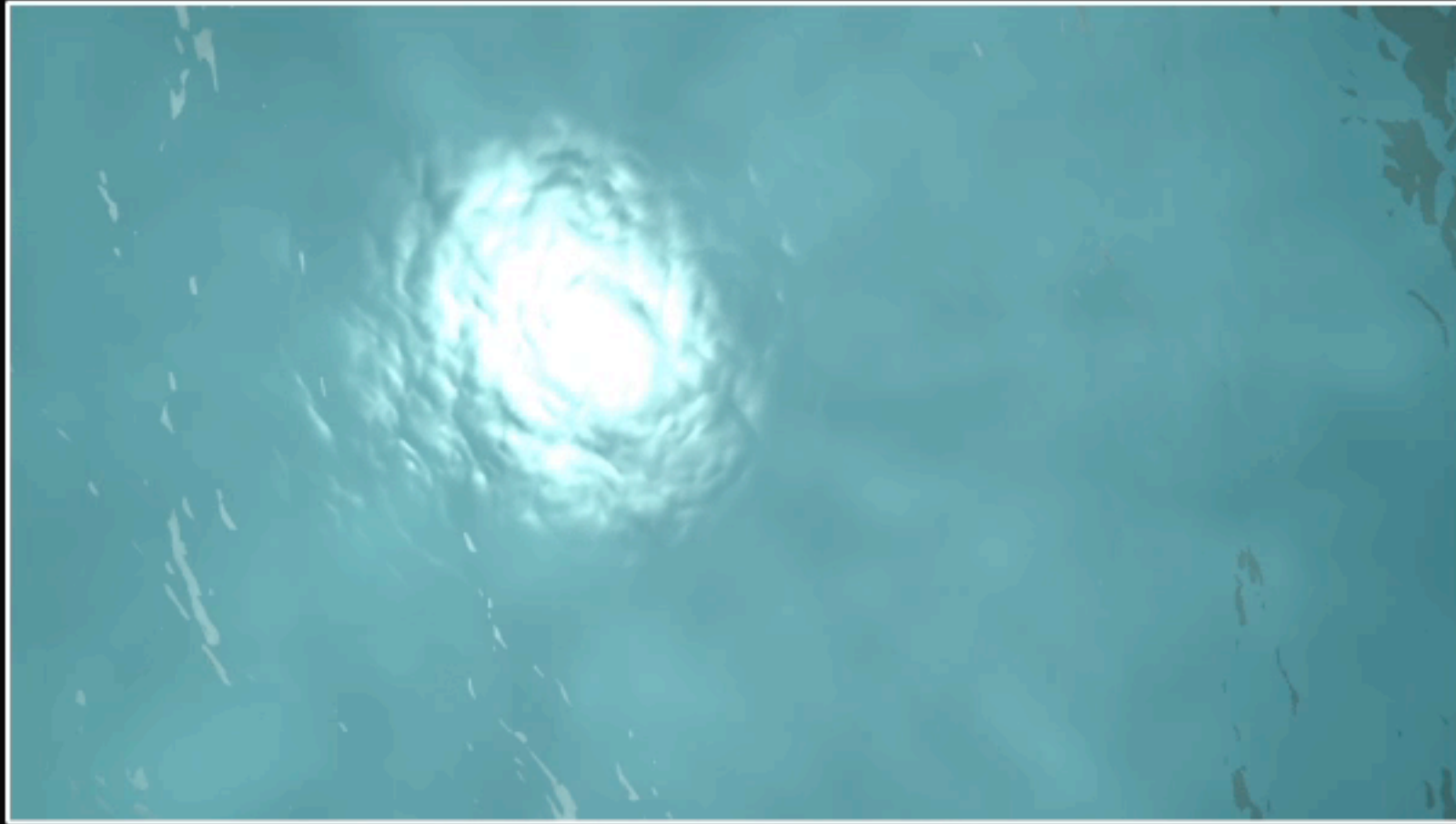
1M Photon Points  
~ 226 seconds/frame

**9x Render Time**

700 Photon Beams  
~ 25 seconds/frame

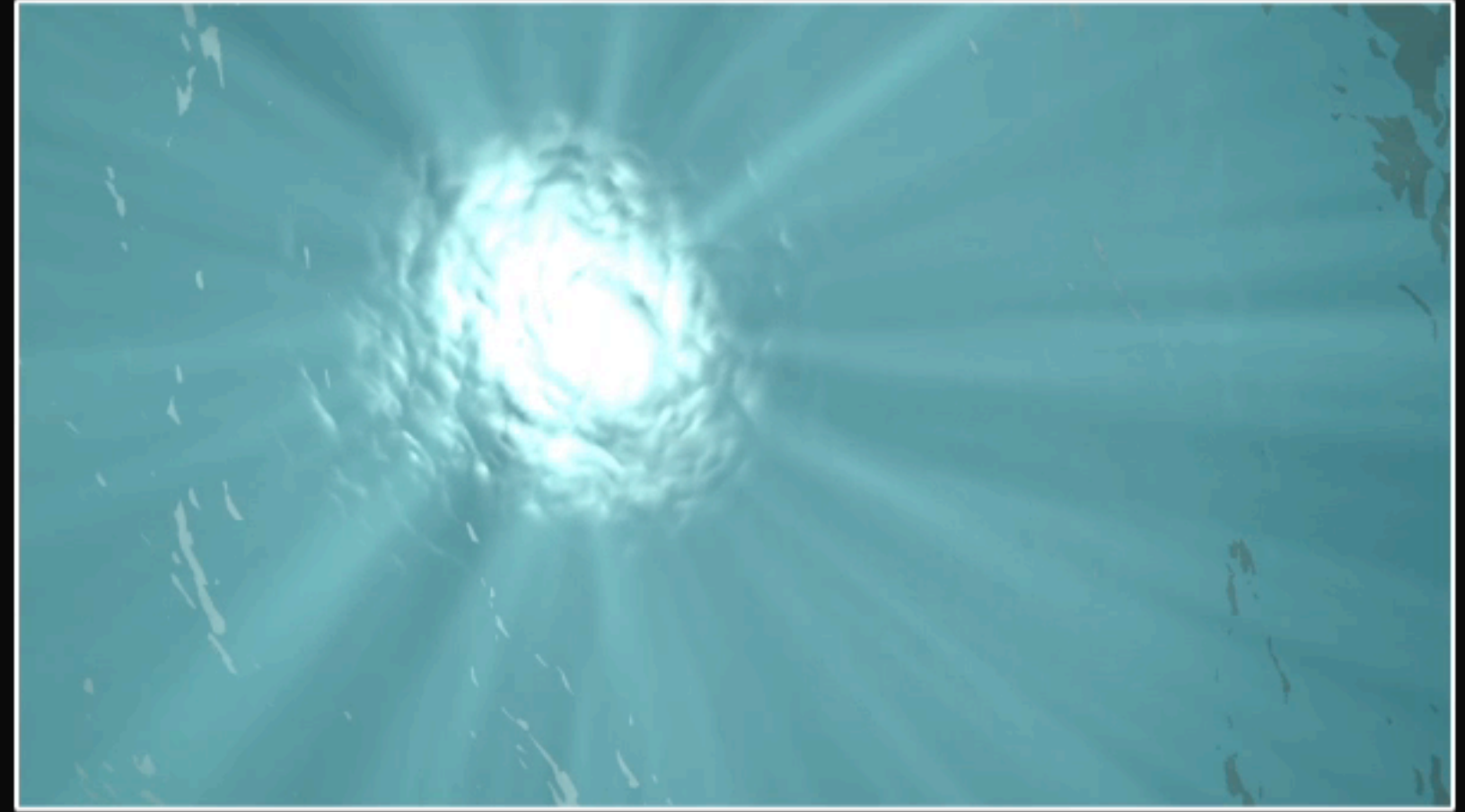
# Underwater Sun Beams

Photon Points



100K Photon **Points**  
~ 204 seconds/frame

Photon Beams



25K Photon **Beams**  
~ 200 seconds/frame

**Roughly Equal Time**



# Progressive Photon Beams



# Progressive Photon Beams

- Combine benefits of:



# Progressive Photon Beams

- Combine benefits of:
  - photon beams



# Progressive Photon Beams

- Combine benefits of:
  - photon beams
  - progressive photon mapping



# Statistical Convergence

- Previous derivations not directly applicable
  - beam density vs. point density





# Statistical Convergence

- Previous derivations not directly applicable
  - beam density vs. point density
- Reduction factor:  $f_i = \frac{i + \alpha}{i + 1}$



# Statistical Convergence

- Previous derivations not directly applicable
  - beam density vs. point density
- Reduction factor:  $f_i = \frac{i + \alpha}{i + 1}$
- *Application* of factor depends on blur dimensionality
  - Surfaces (2D):  $r_{i+1}^2 = f_i \cdot r_i^2$



# Statistical Convergence

- Previous derivations not directly applicable
  - beam density vs. point density
- Reduction factor:  $f_i = \frac{i + \alpha}{i + 1}$
- *Application* of factor depends on blur dimensionality
  - Surfaces (2D):  $r_{i+1}^2 = f_i \cdot r_i^2$
  - Volumetric photon mapping (3D):  $r_{i+1}^3 = f_i \cdot r_i^3$



# Statistical Convergence

- Previous derivations not directly applicable
  - beam density vs. point density
- Reduction factor:  $f_i = \frac{i + \alpha}{i + 1}$
- *Application* of factor depends on blur dimensionality
  - Surfaces (2D):  $r_{i+1}^2 = f_i \cdot r_i^2$
  - Volumetric photon mapping (3D):  $r_{i+1}^3 = f_i \cdot r_i^3$
  - Beam × Beam (1D):  $r_{i+1} = f_i \cdot r_i$



# Algorithm



# Algorithm

## Step 1:

- Photon tracing: emit, scatter, store beams
- Scale beam widths by global factor  $r_i$



# Algorithm

## Step 1:

- Photon tracing: emit, scatter, store beams
- Scale beam widths by global factor  $r_i$

## Step 2:

- Trace random camera path, evaluate radiance estimate along each ray using beams



# Algorithm

## Step 1:

- Photon tracing: emit, scatter, store beams
- Scale beam widths by global factor  $r_i$

## Step 2:

- Trace random camera path, evaluate radiance estimate along each ray using beams
- Display running average





# Algorithm

## Step 1:

- Photon tracing: emit, scatter, store beams
- Scale beam widths by global factor  $r_i$

## Step 2:

- Trace random camera path, evaluate radiance estimate along each ray using beams
- Display running average
- *Reduce* global factor  $r_i$  and *repeat*



# Algorithm

Step 1:

- Photon tracing: emit, scatter, store beams
- Scale beam widths by global factor  $r_i$

Step 2:

## Trivially Parallelizable

- Trace random camera path, evaluate radiance estimate along each ray using beams
- Display running average
- *Reduce* global factor  $r_i$  and *repeat*



# Evaluating the Transmittance

- Need to compute transmittance: along photon beam, along camera ray



# Evaluating the Transmittance

- Need to compute transmittance: along photon beam, along camera ray
- Homogeneous: analytic



# Evaluating the Transmittance

- Need to compute transmittance: along photon beam, along camera ray
- Homogeneous: analytic
- Heterogeneous: use progressive deep shadow maps



# Results & Implementation

- 3 implementations:
  - GPU-only OptiX ray-tracer
  - GPU-only rasterization
  - General: Hybrid CPU/GPU



# Results & Implementation

- 3 implementations:
  - GPU-only OptiX ray-tracer
  - GPU-only rasterization
  - General: Hybrid CPU/GPU

# BUMPYSPHERE

## OPTIX IMPLEMENTATION

scene courtesy of Bruce Walter



alpha: 0.60    beams per pass: 1024    pass number: 1    render time per pass: 132.97 ms

**2x speed**





# Results & Implementation

- 3 implementations:
  - GPU-only OptiX ray-tracer
  - GPU-only **rasterization**
  - General: Hybrid CPU/GPU

alpha = 0.5  
P = 0.037695  
Shadow map resolution: 64 x 64  
pass number: 14  
average render time per pass: 33 ms

[www.fraps.com](http://www.fraps.com)

# OCEAN

OPENGL  
RASTERIZATION-ONLY  
IMPLEMENTATION



$\alpha = 0.5$

2x speed



# Results & Implementation

- 3 implementations:
  - GPU-only OptiX ray-tracer
  - GPU-only rasterization
  - General: Hybrid CPU/GPU

# CARS

1280x720, Depth-of-Field

Pass 1



Homogeneous



Heterogeneous

Pass 1



Average of Passes 1..1



Pass 2



Average of Passes 1..2



Pass 4



Average of Passes 1..4



Pass 8



Average of Passes 1..8





Pass 16



Average of Passes 1..16



Pass 32



Average of Passes 1..32



Pass 64



Average of Passes 1..64



Pass 128



Average of Passes 1..128



Pass 256



Average of Passes 1..256



Pass 512



Average of Passes 1..512



Pass 1024

Average of Passes 1..1024



# CARS

1280x720, Depth-of-Field

**Homogeneous**

14.55M Photon Beams

9.5 minutes



**Heterogeneous**

15.04M Photon Beams

16.8 minutes





# CARS

1280x720, Depth-of-Field

**Homogeneous**

14.55M Photon Beams

9.5 minutes



**Heterogeneous**

15.04M Photon Beams

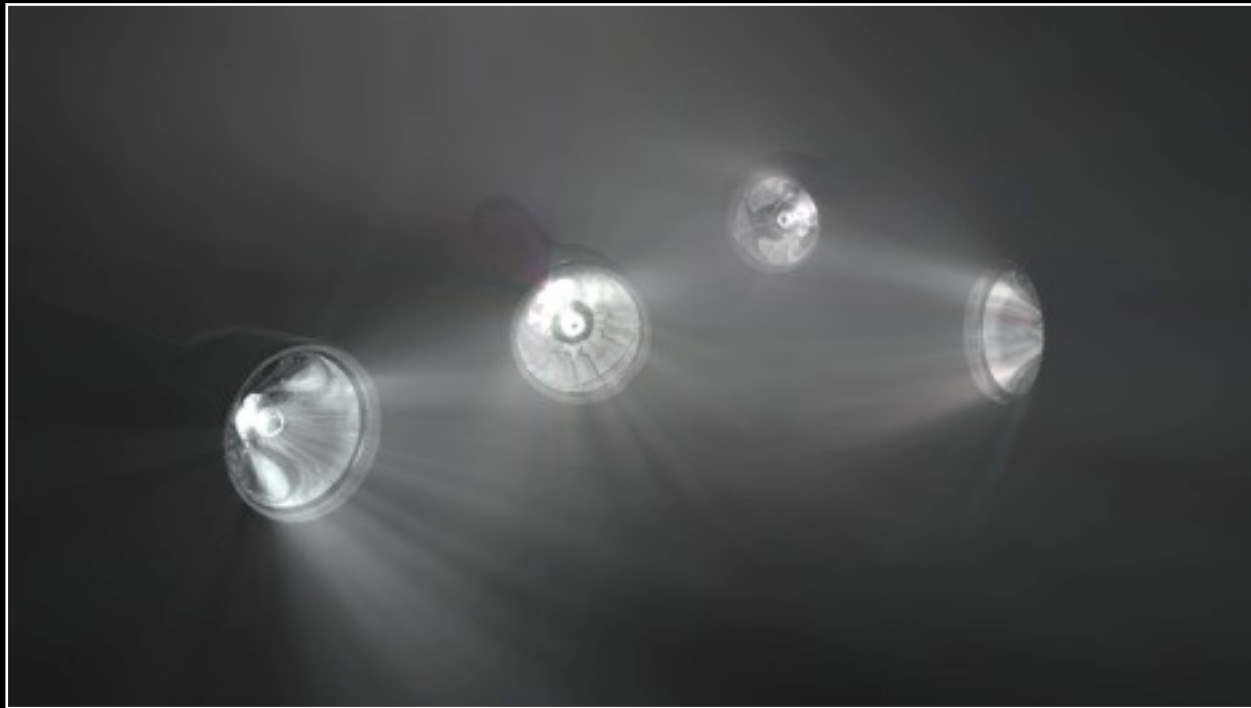
16.8 minutes



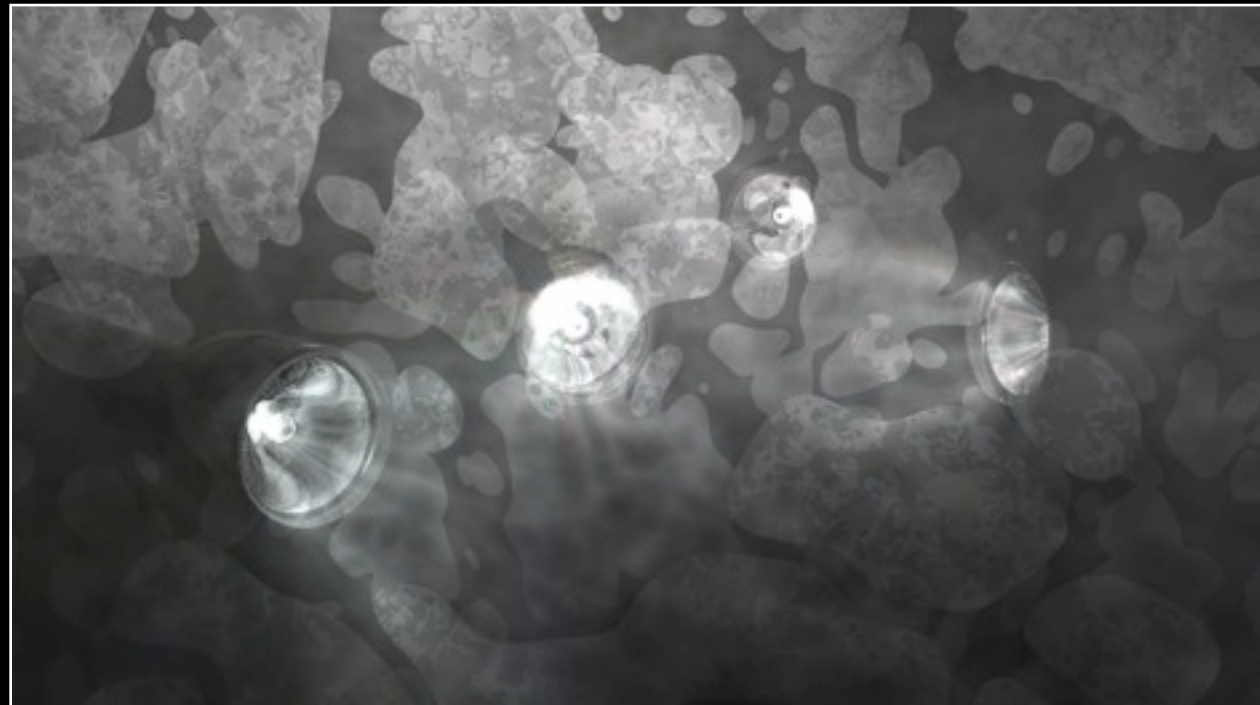
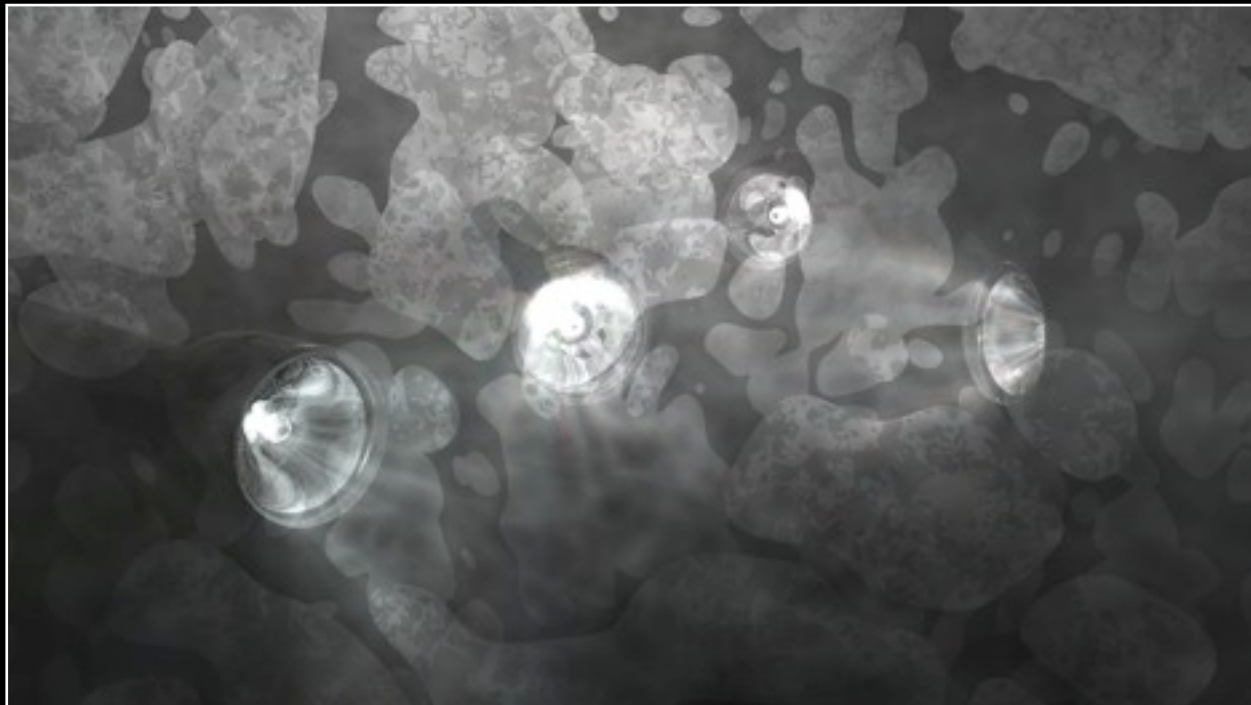
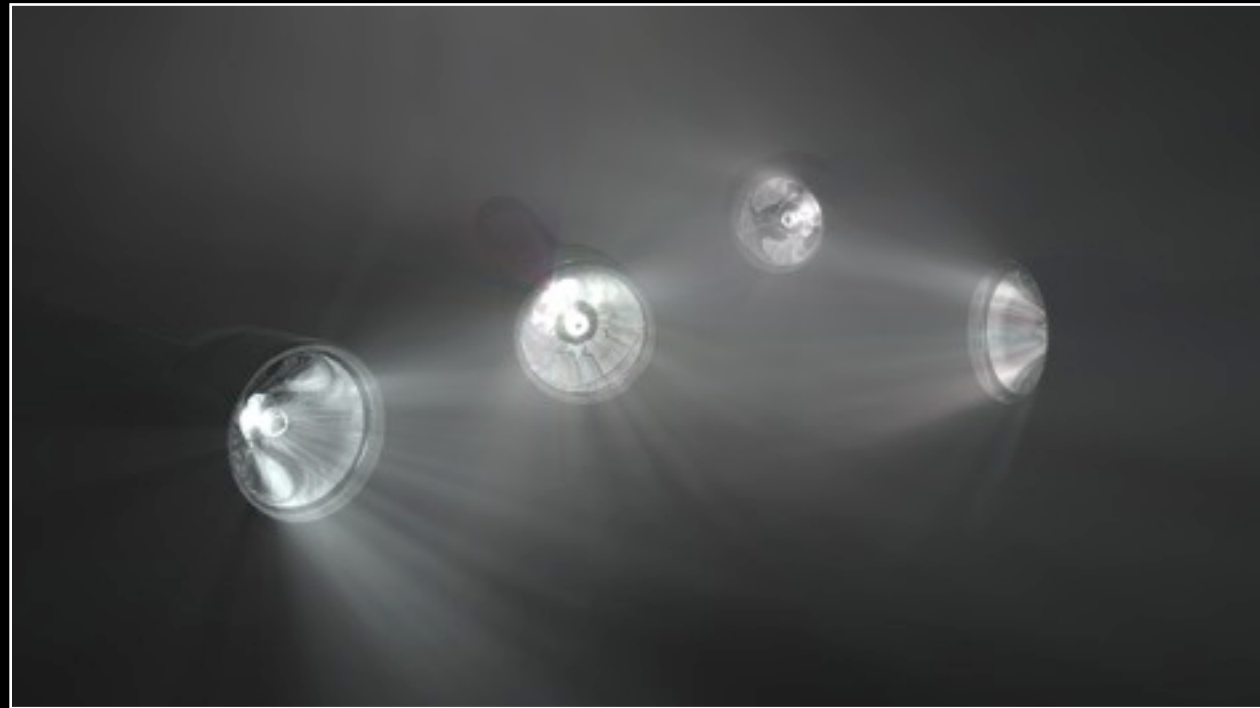
# FLASHLIGHTS

1280x720, Depth-of-Field

Pass 1



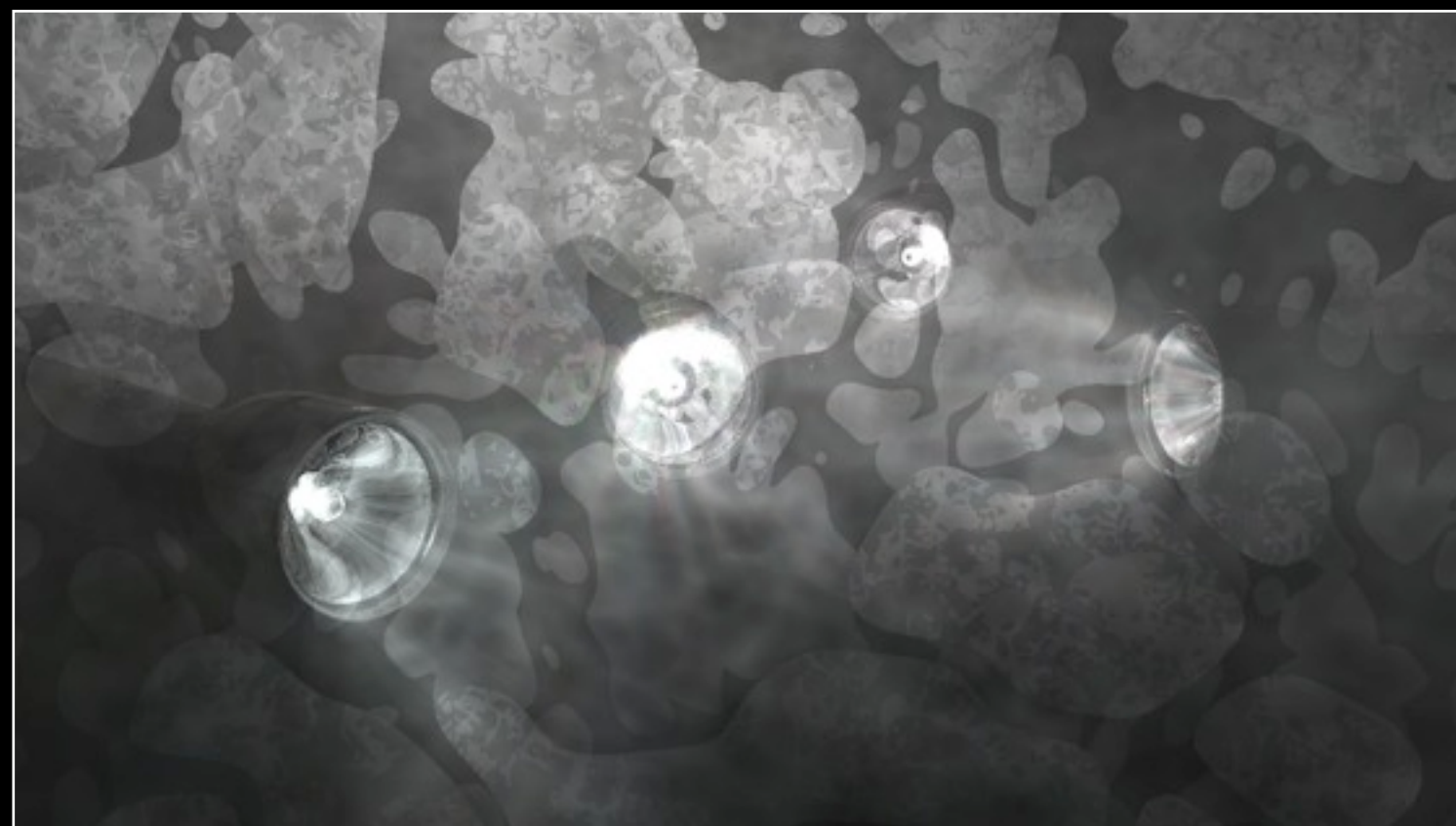
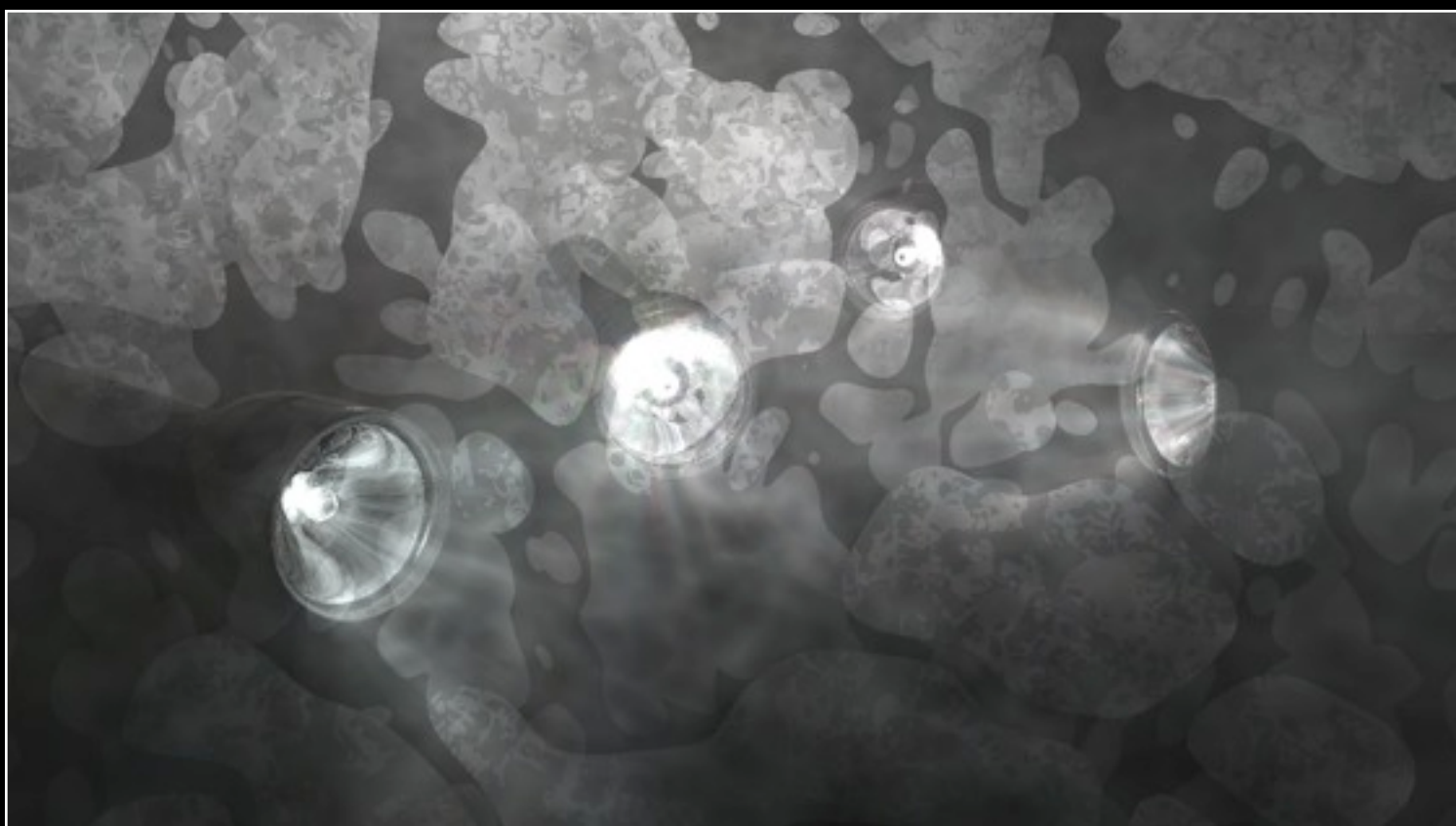
Average of Passes 1..1



Pass 1



Average of Passes 1..1



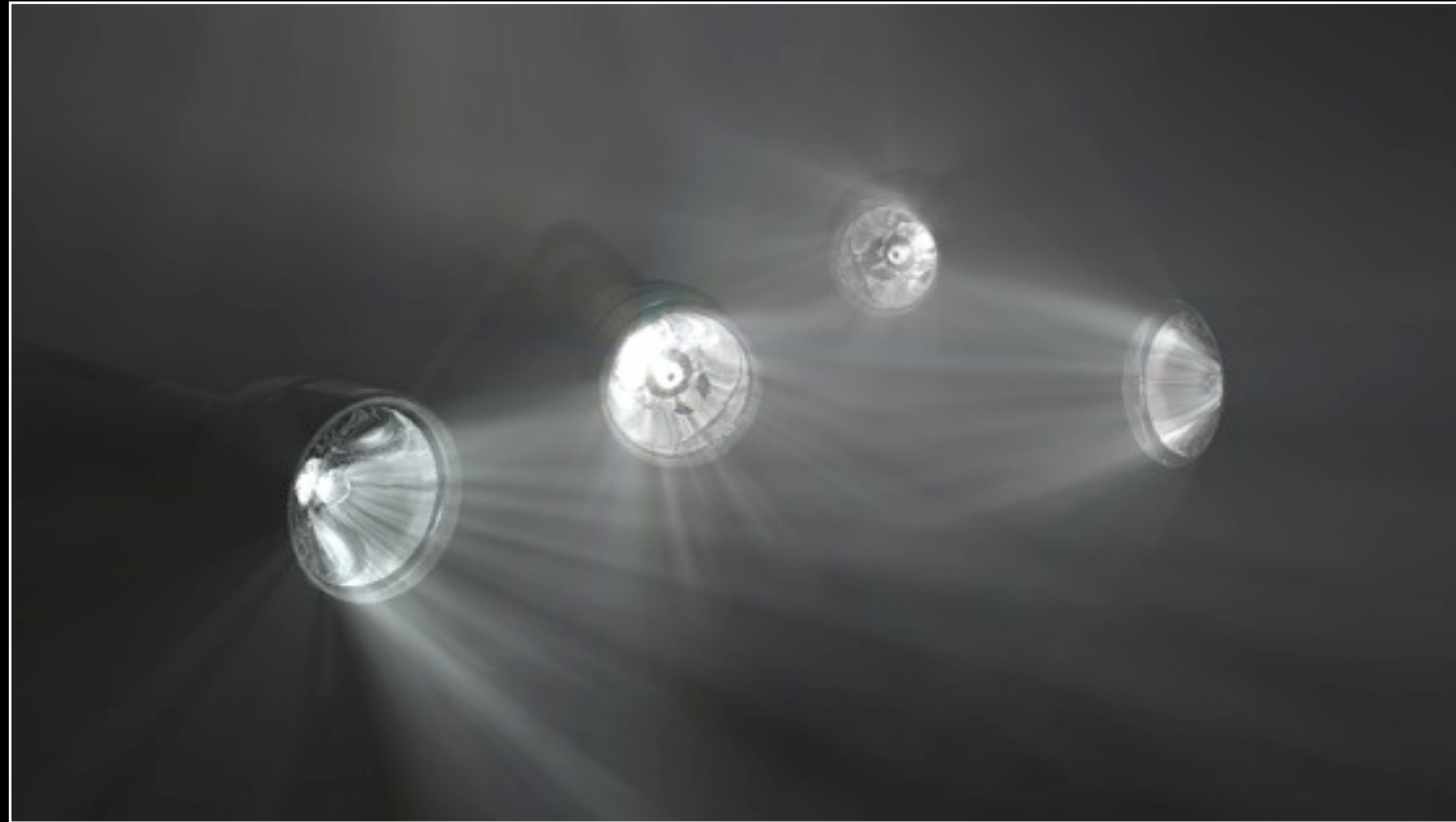
Pass 2



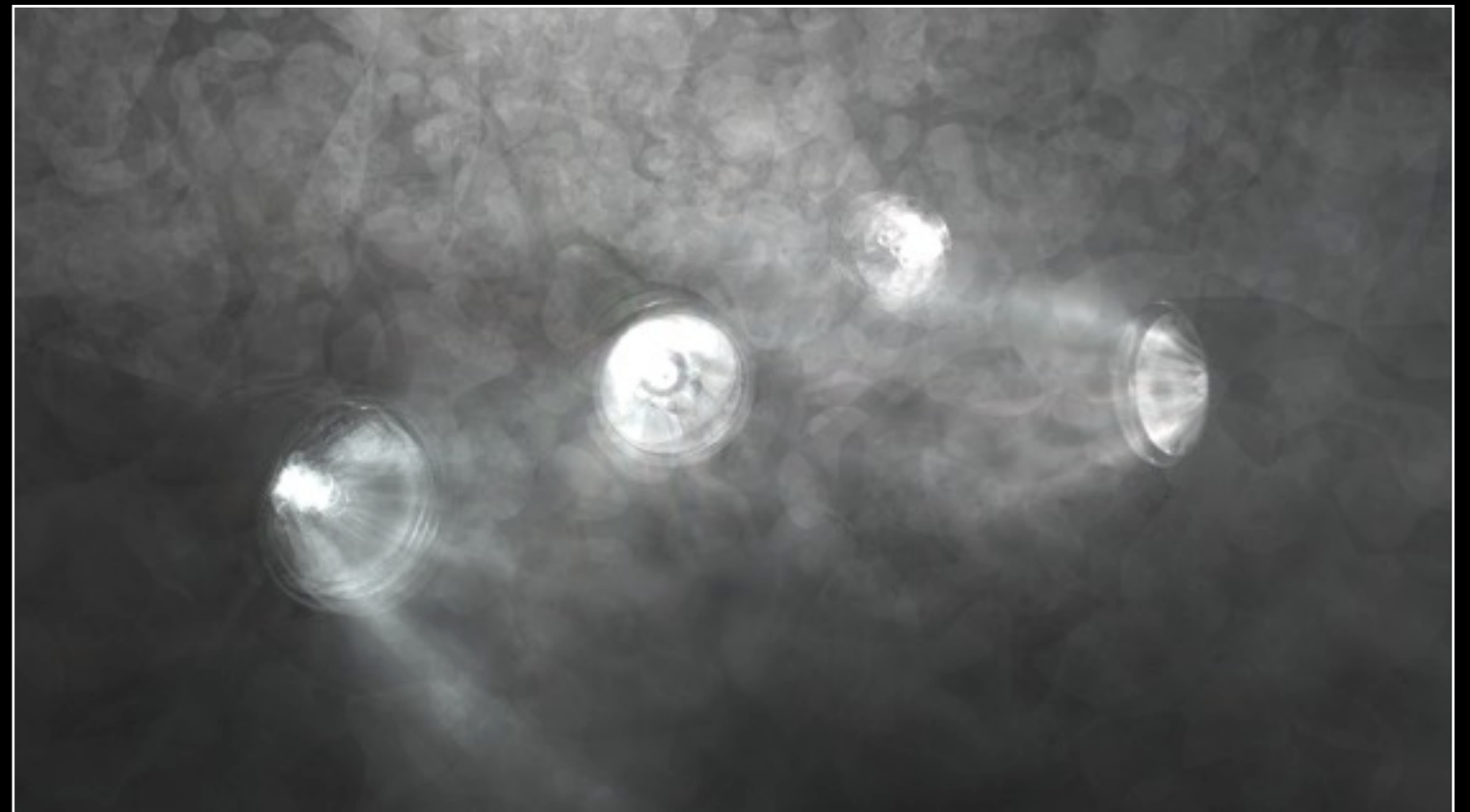
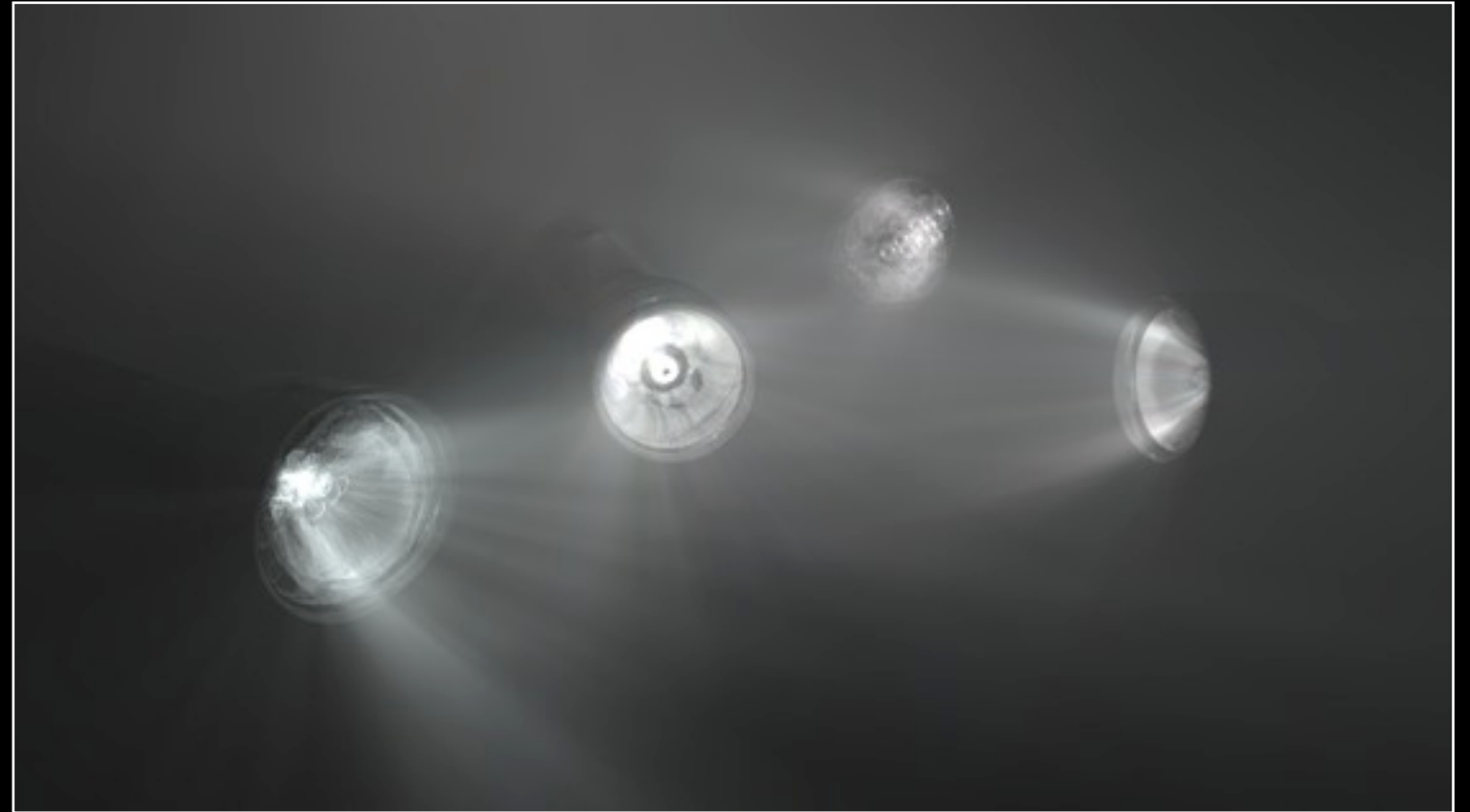
Average of Passes 1..2



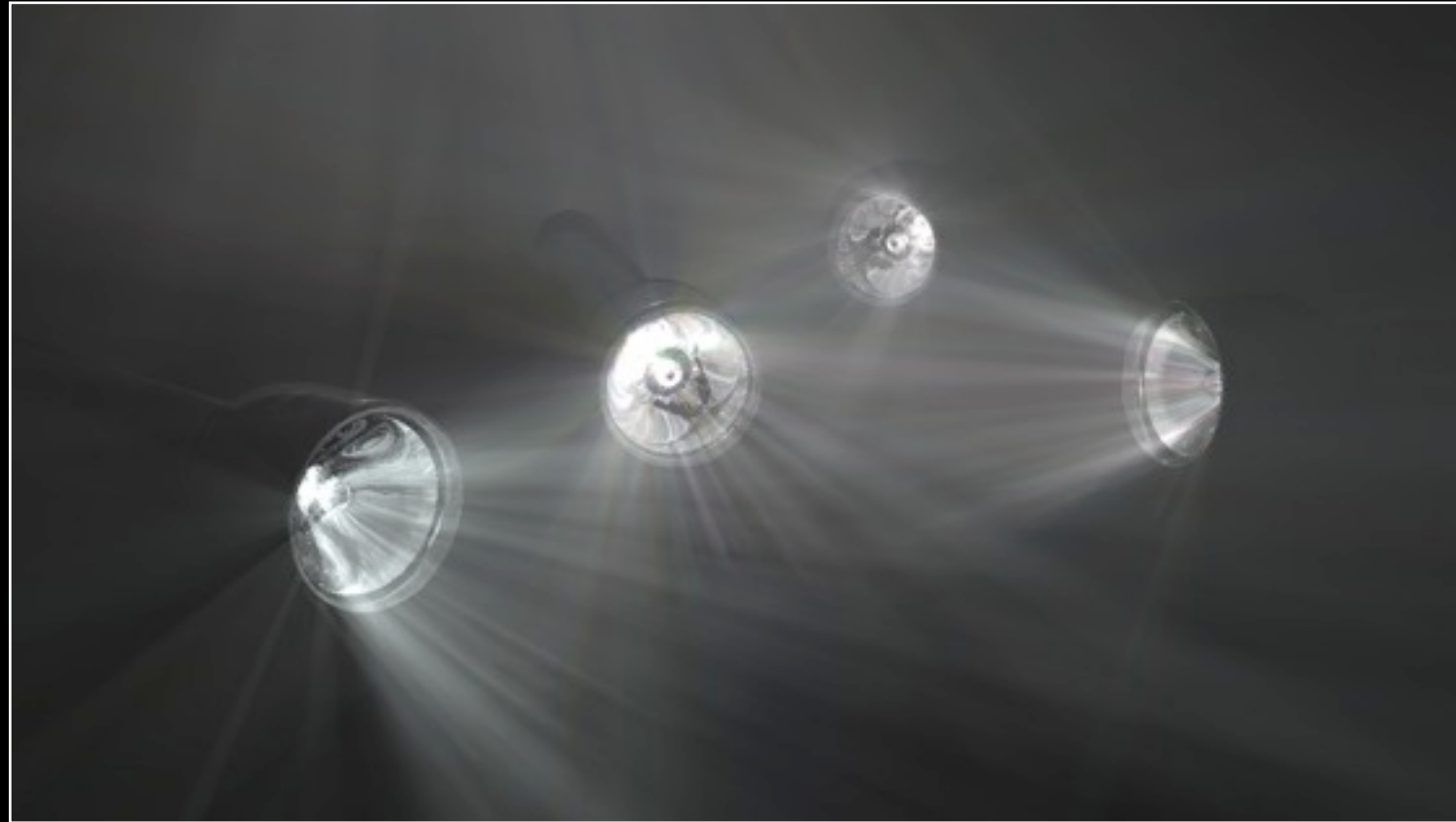
Pass 4



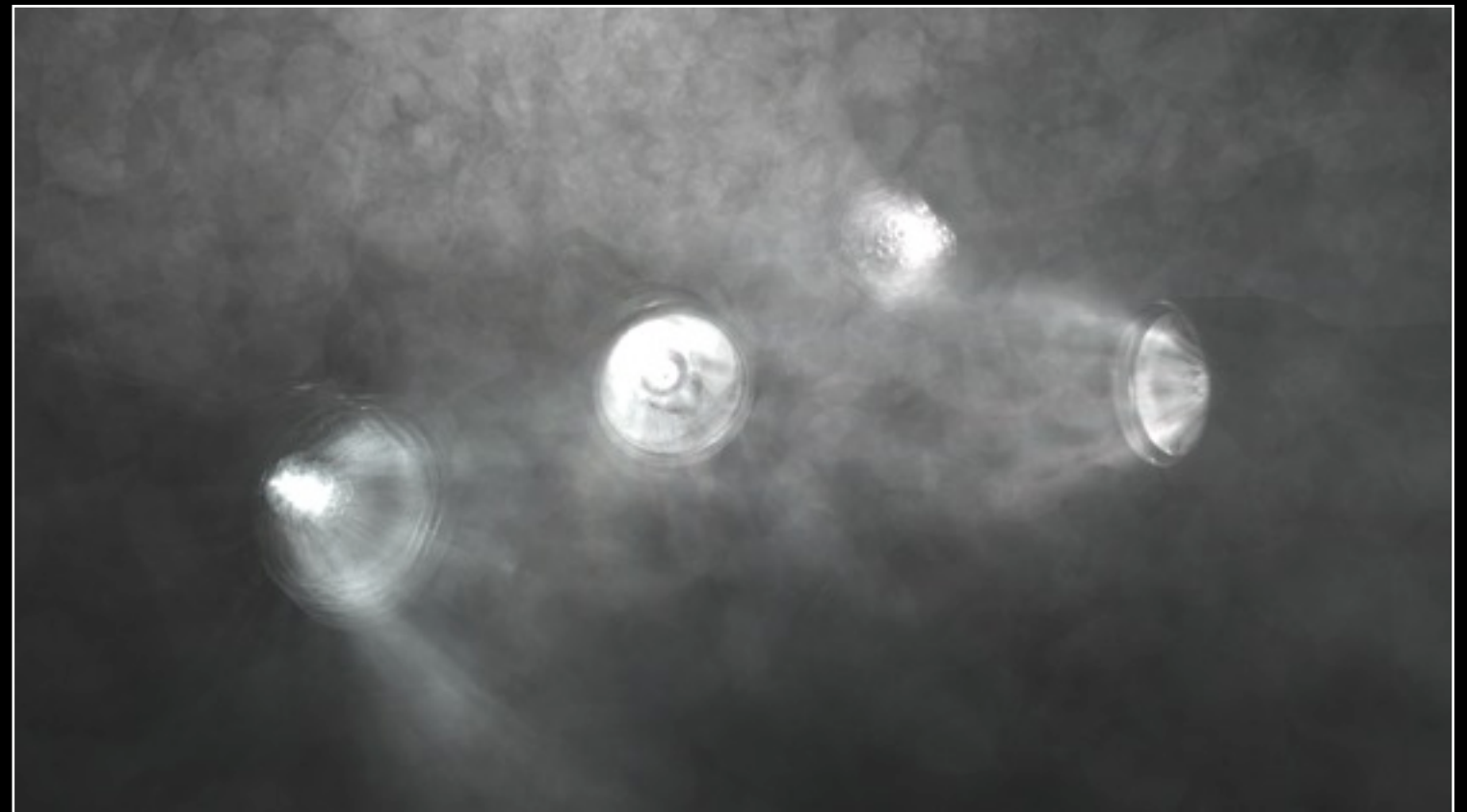
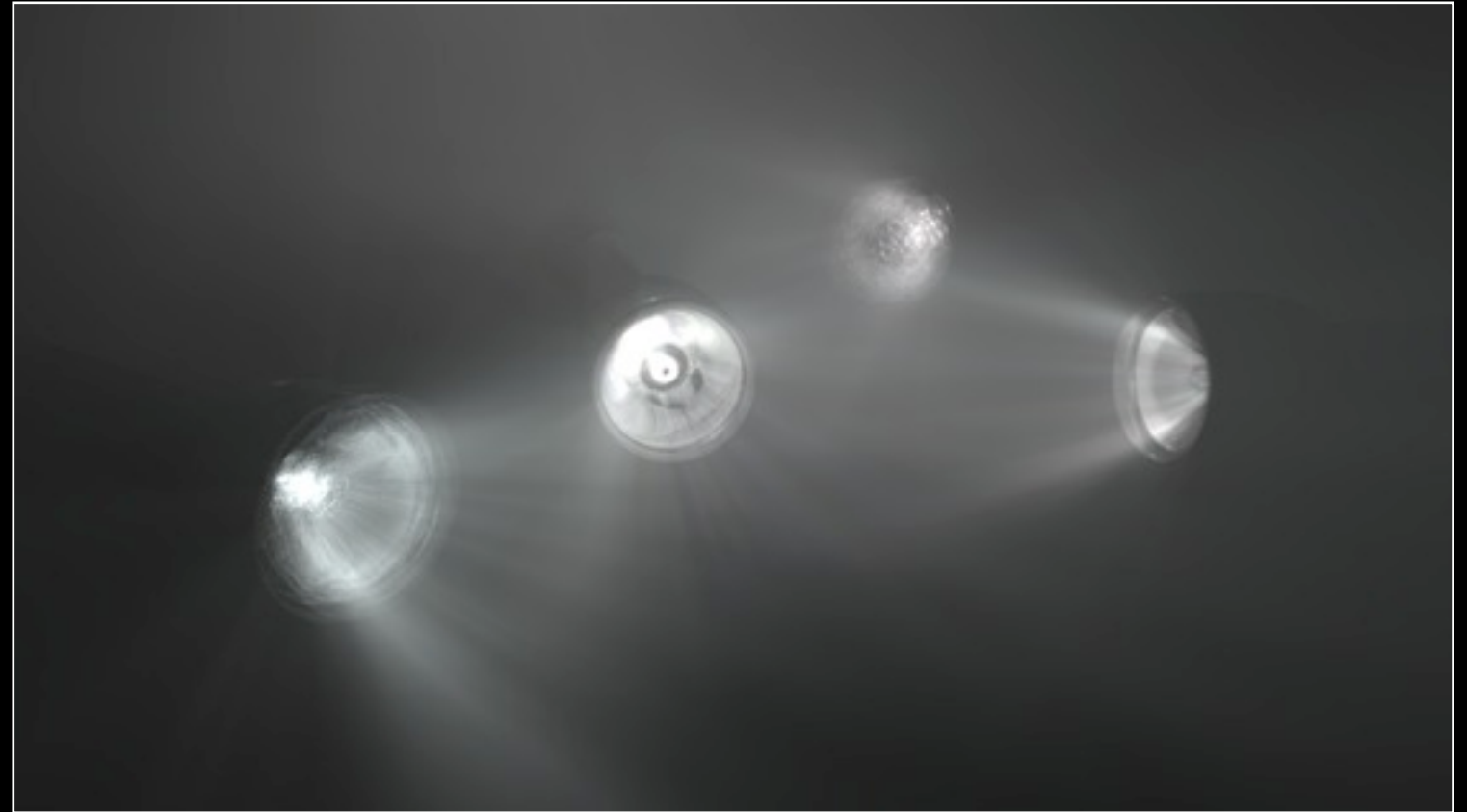
Average of Passes 1..4



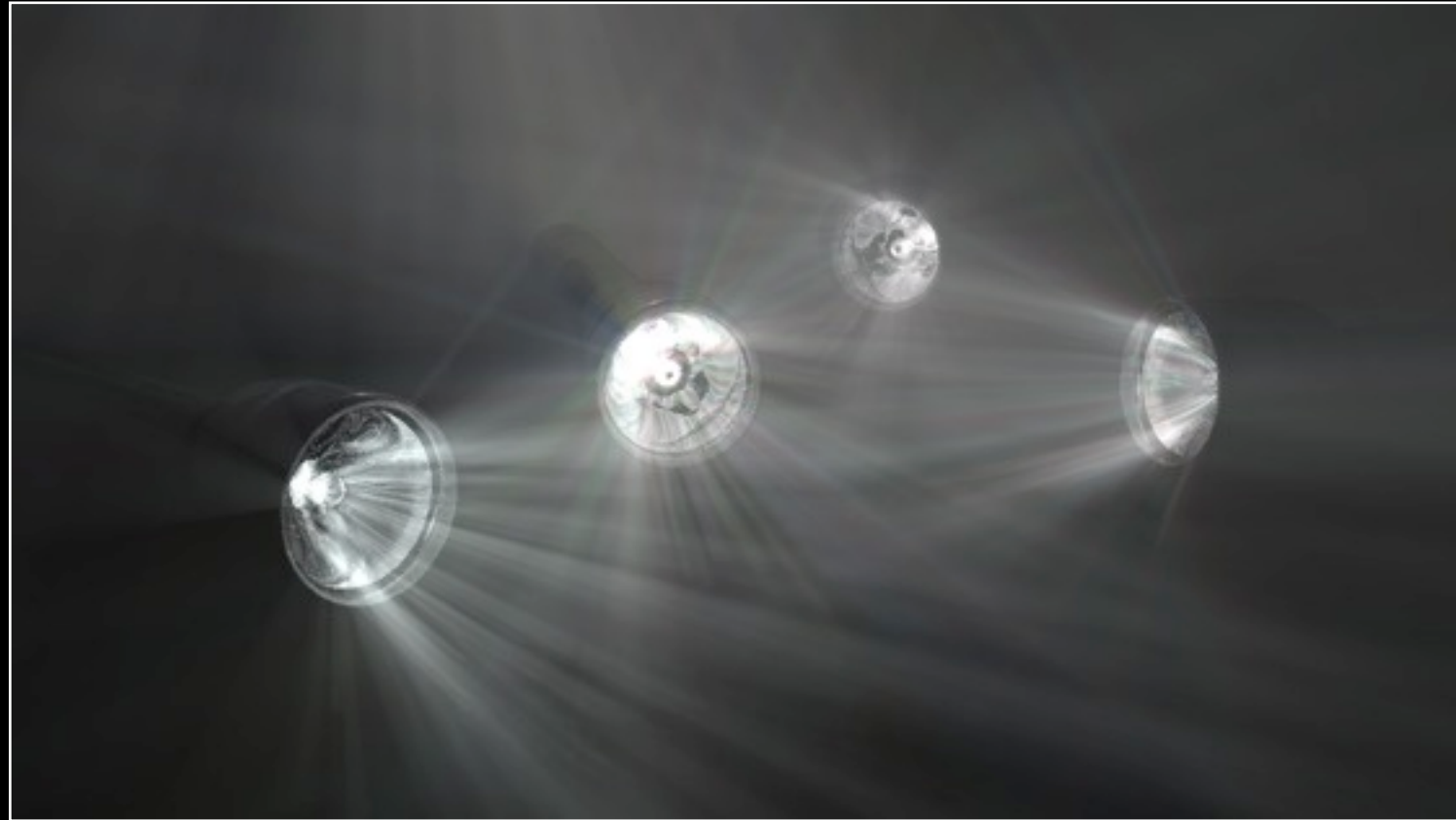
Pass 8



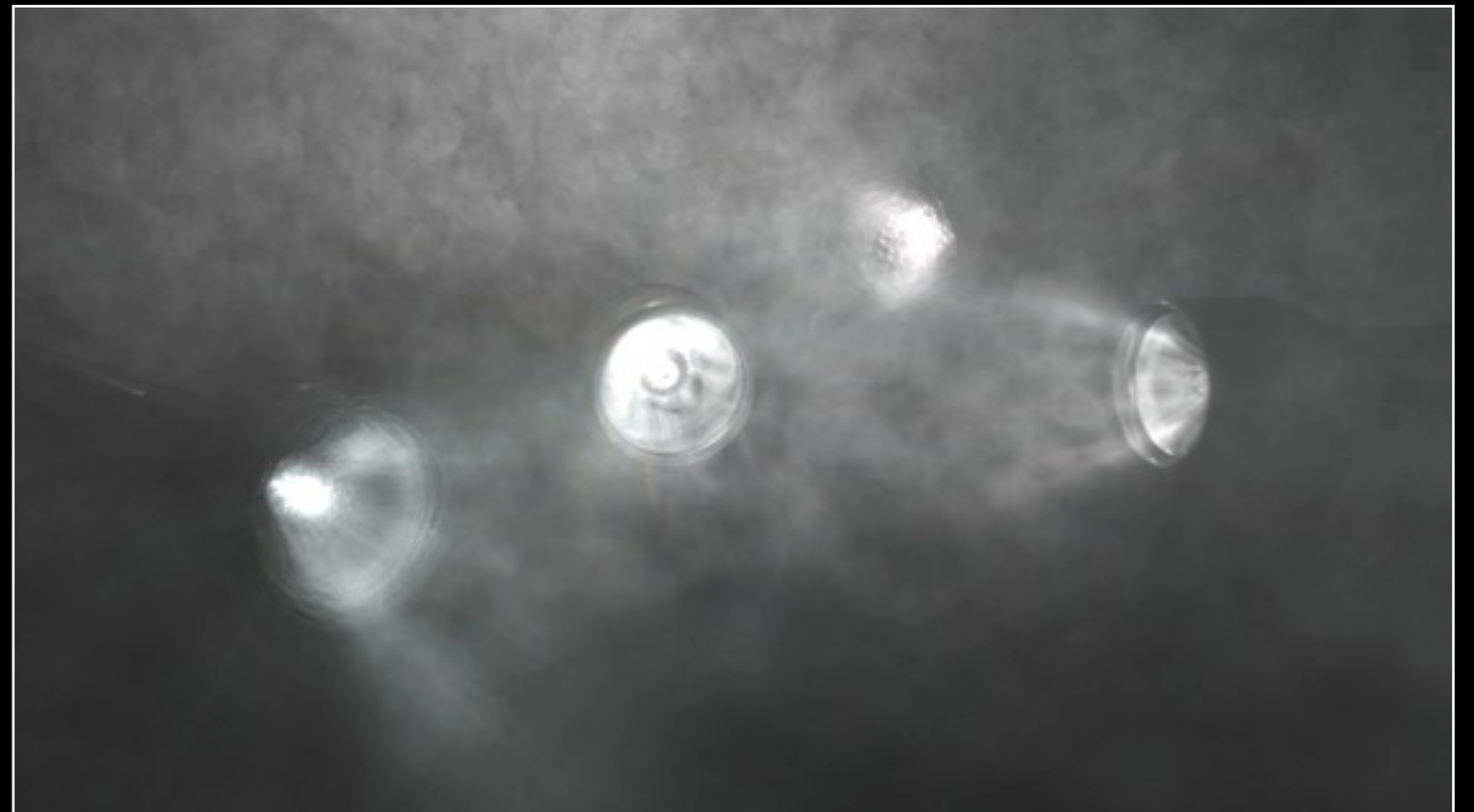
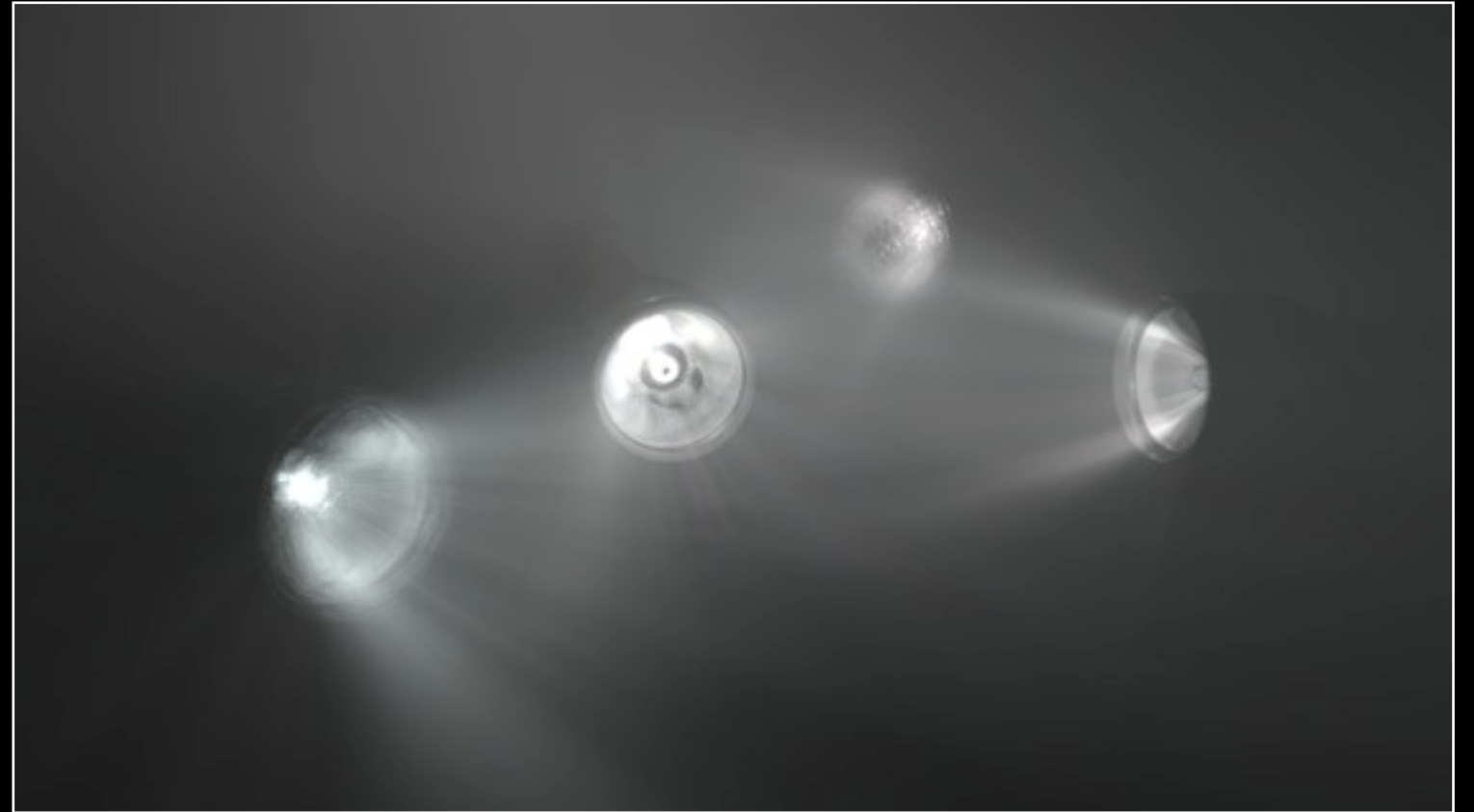
Average of Passes 1..8



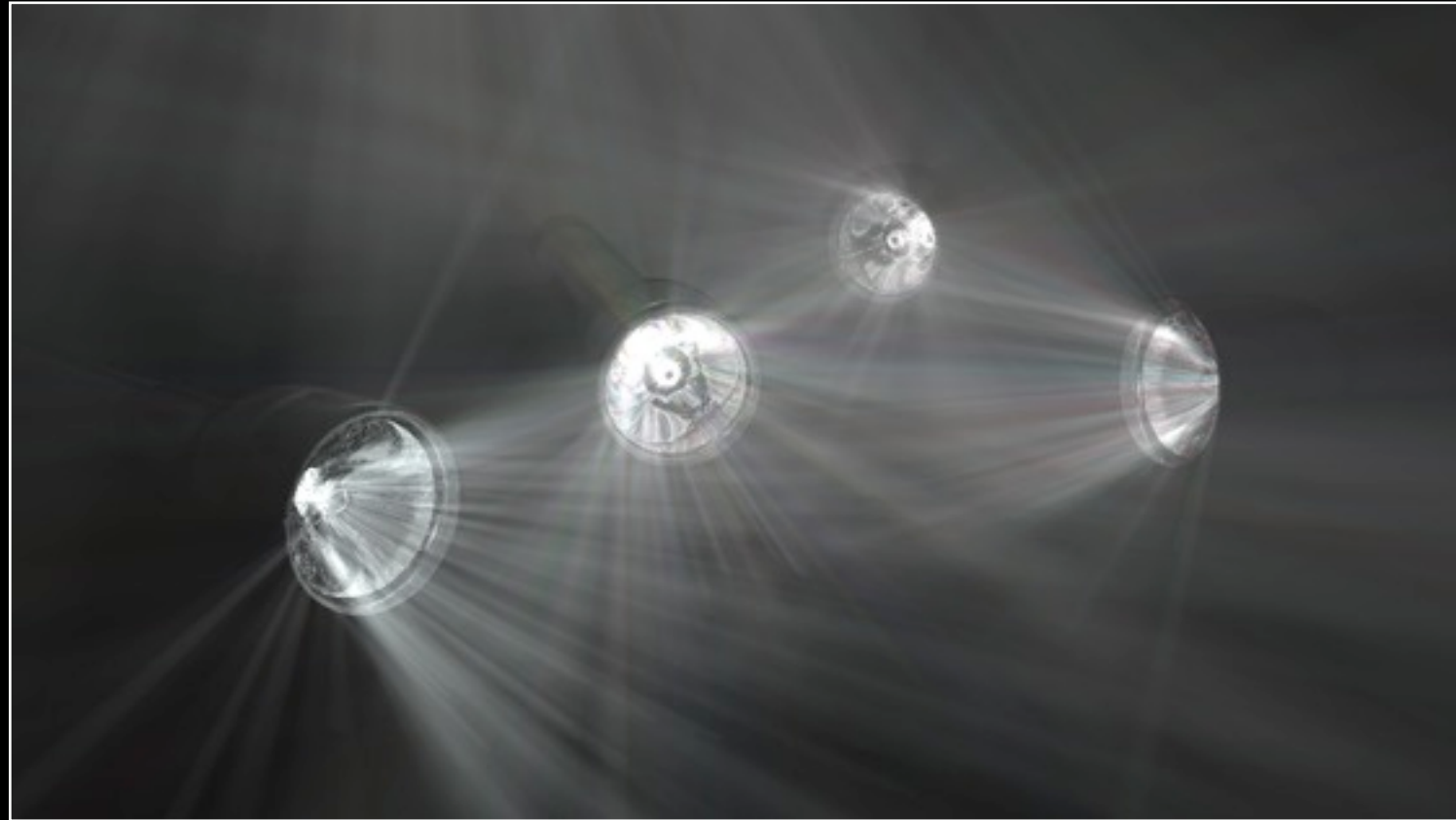
Pass 16



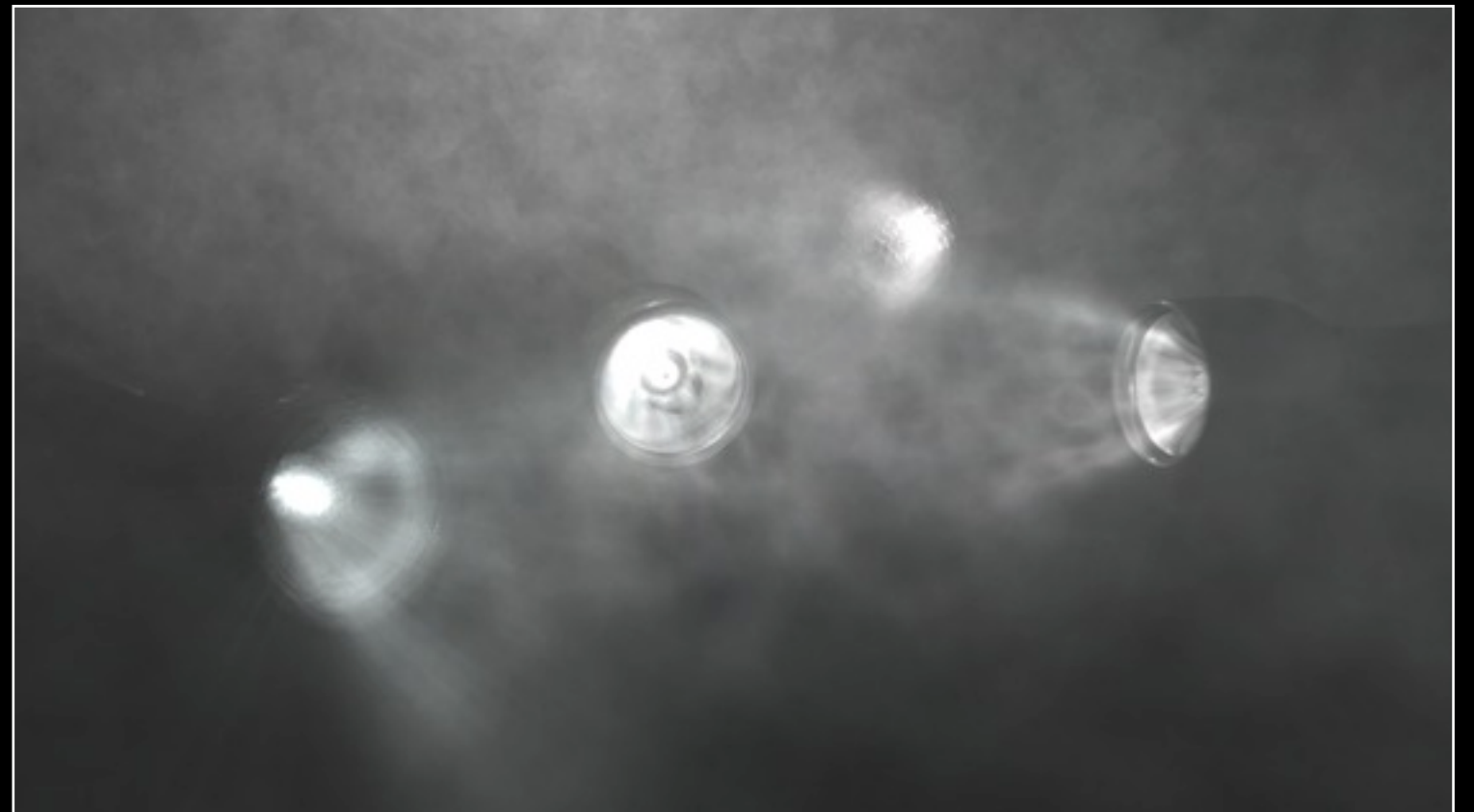
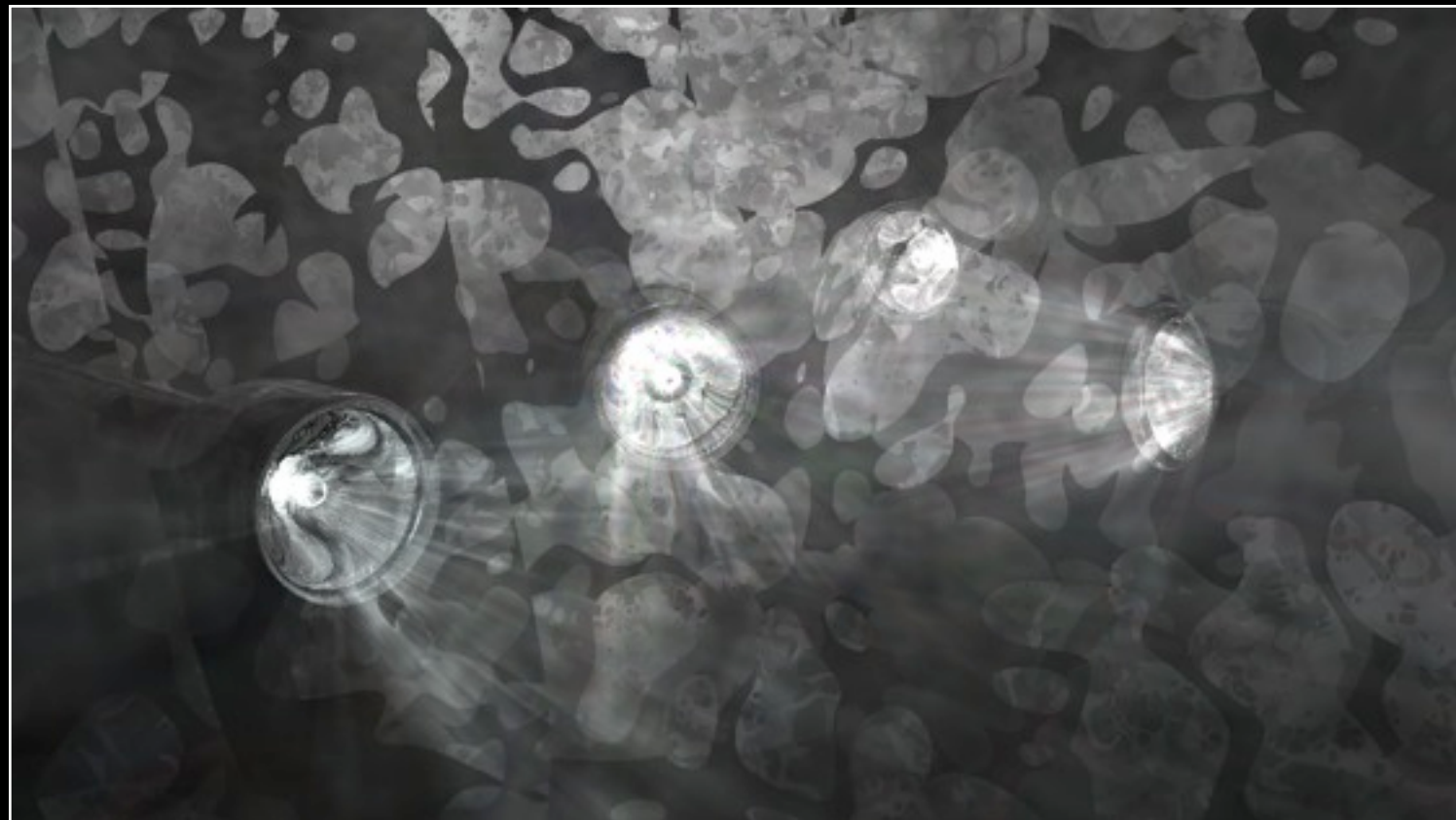
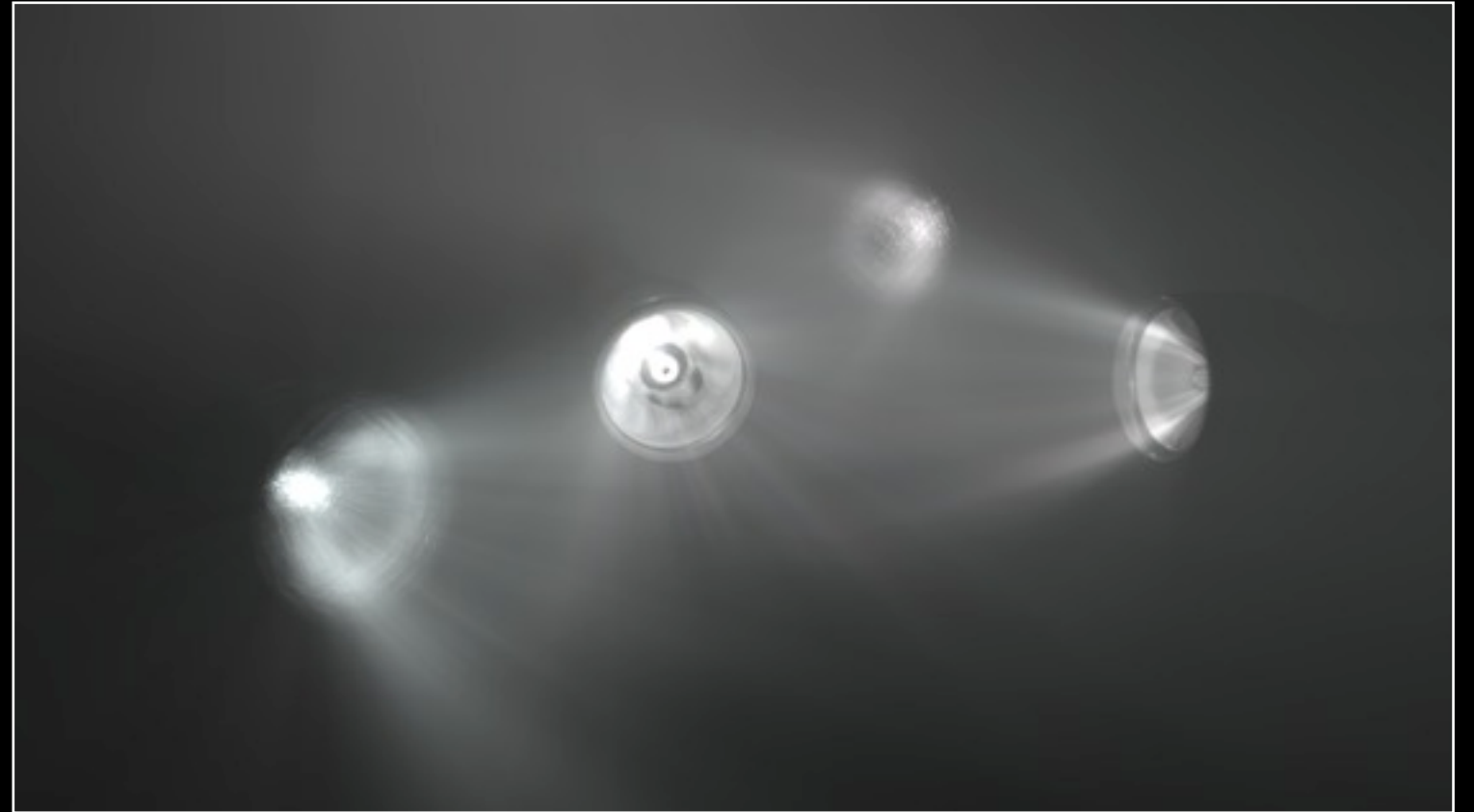
Average of Passes 1..16



Pass 32

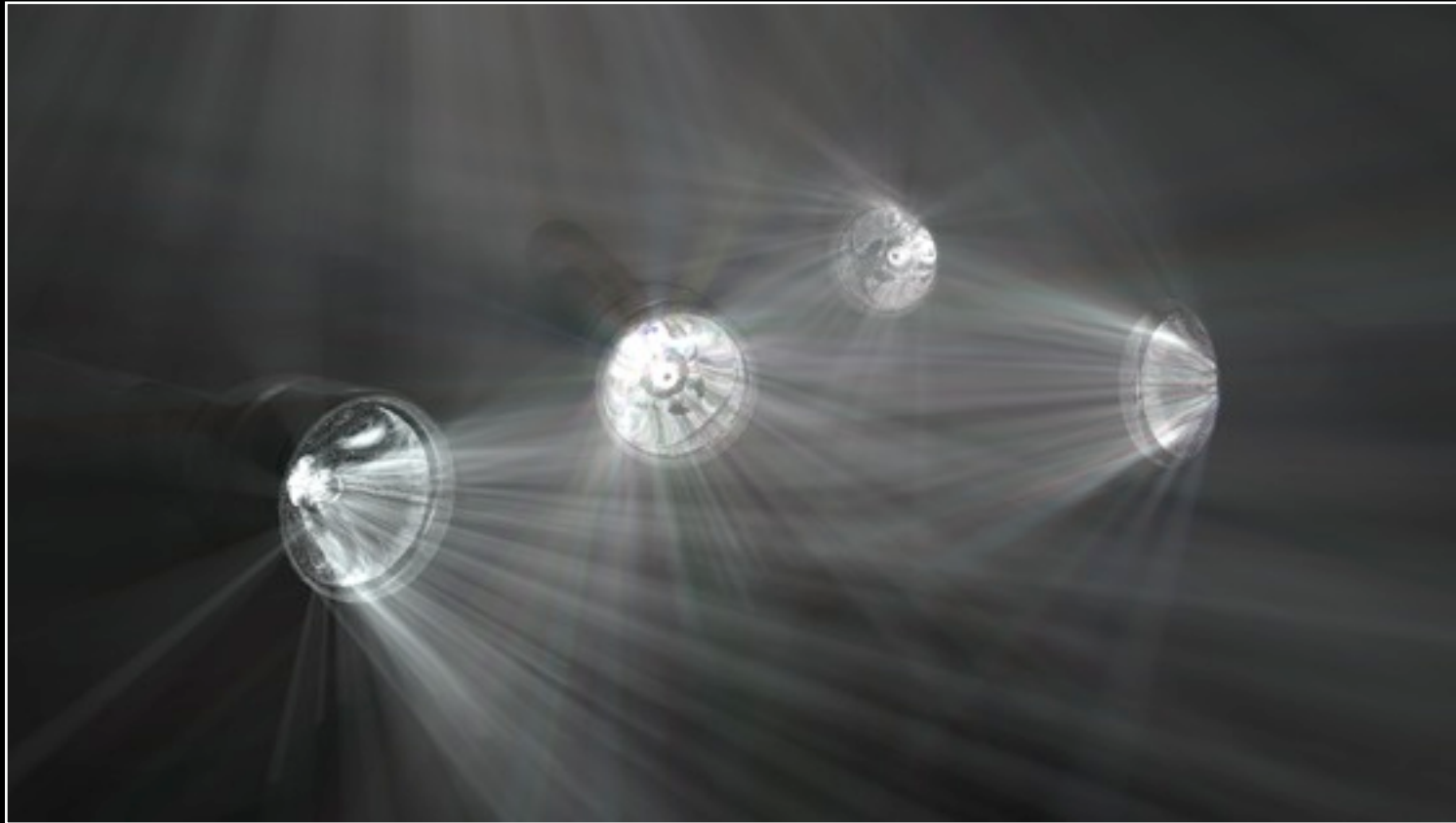


Average of Passes 1..32

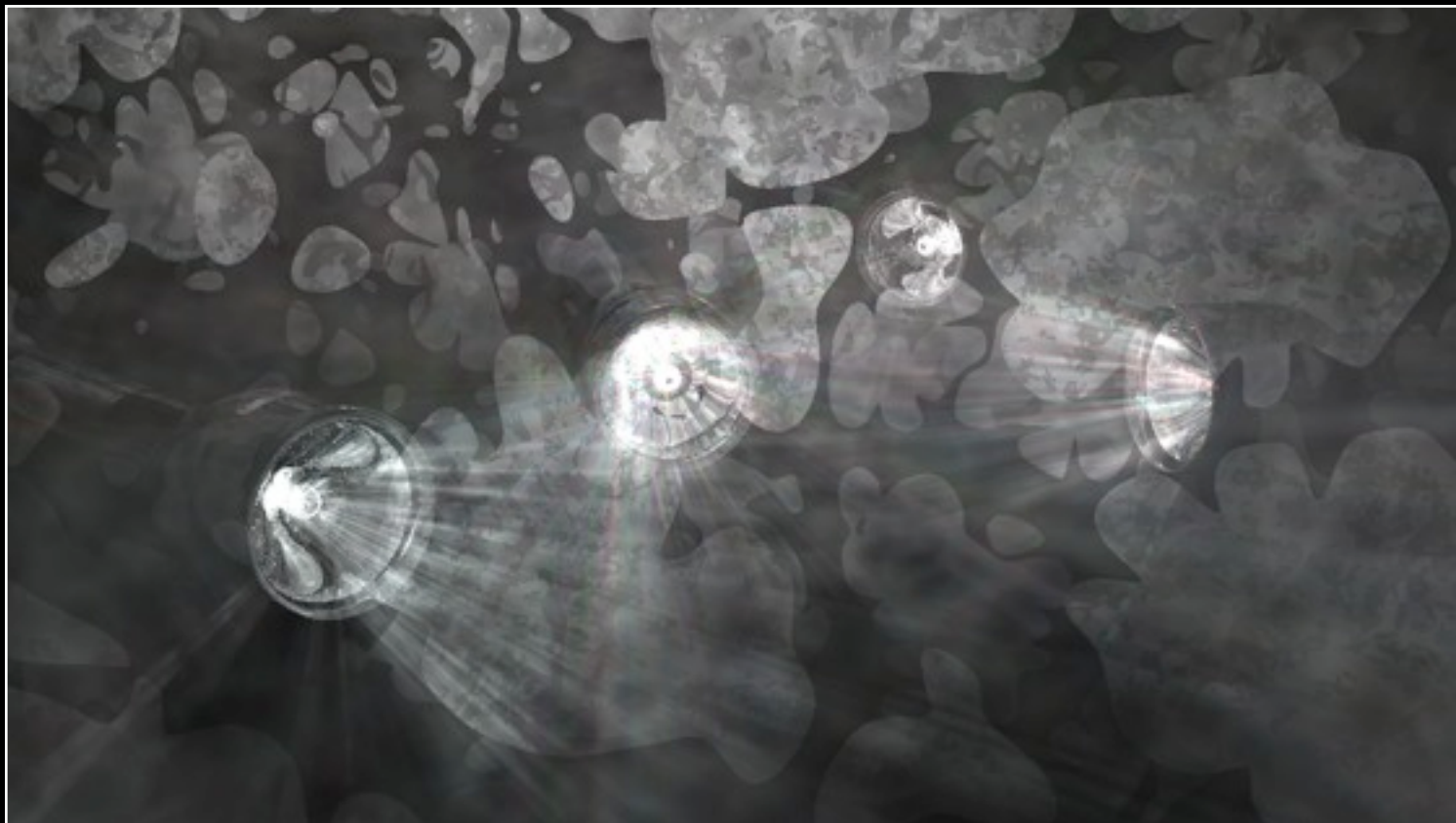
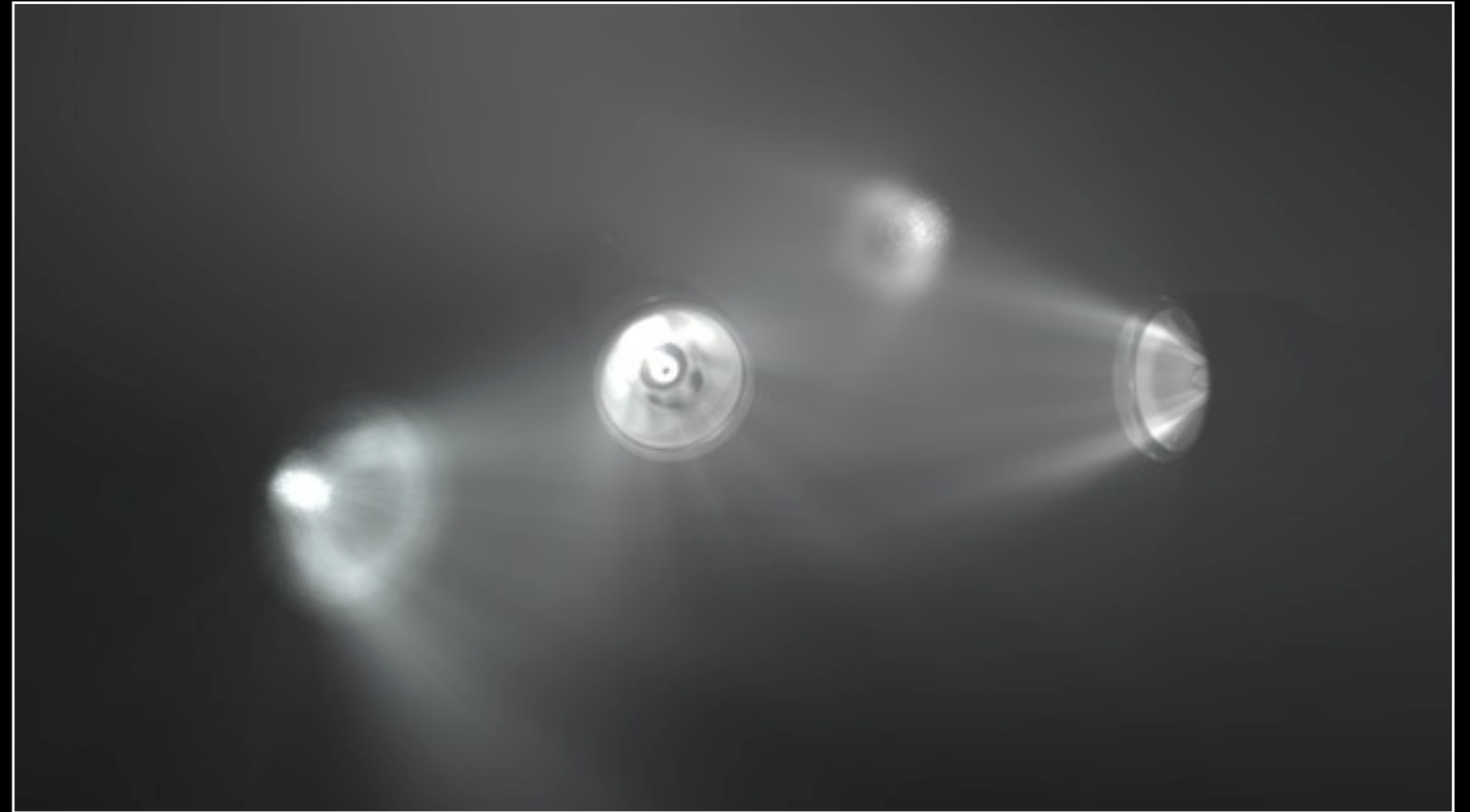




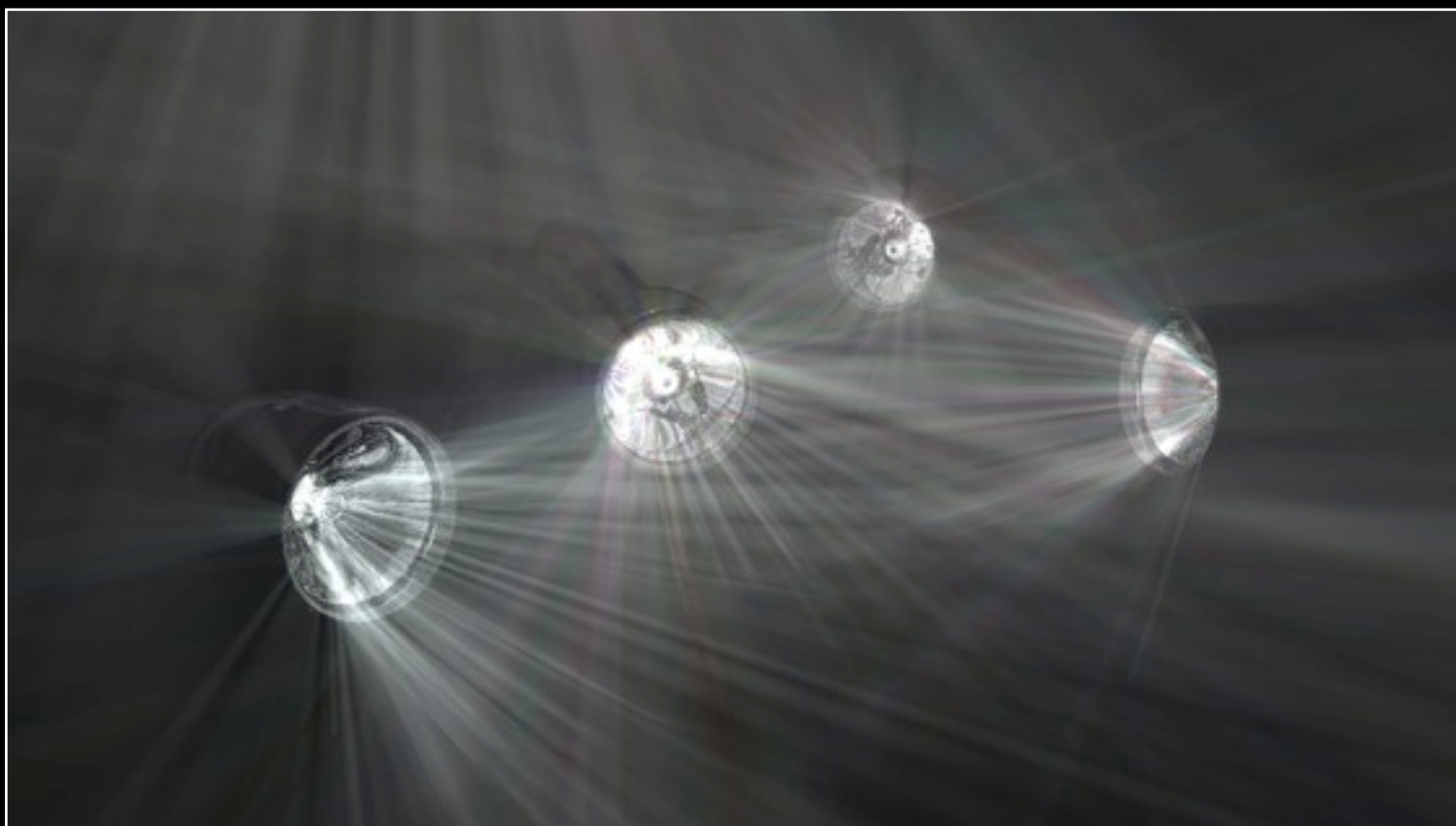
Pass 64



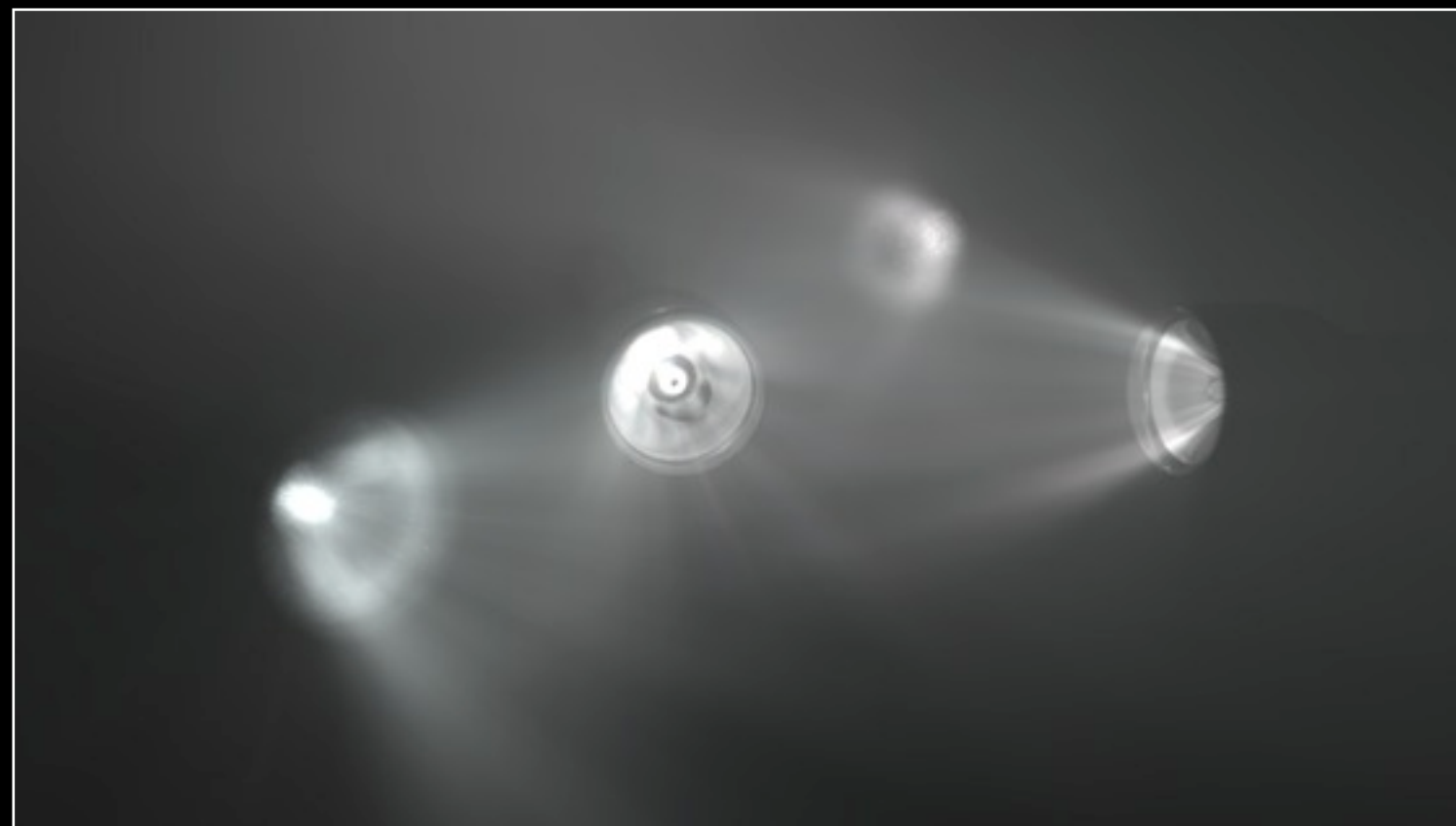
Average of Passes 1..64



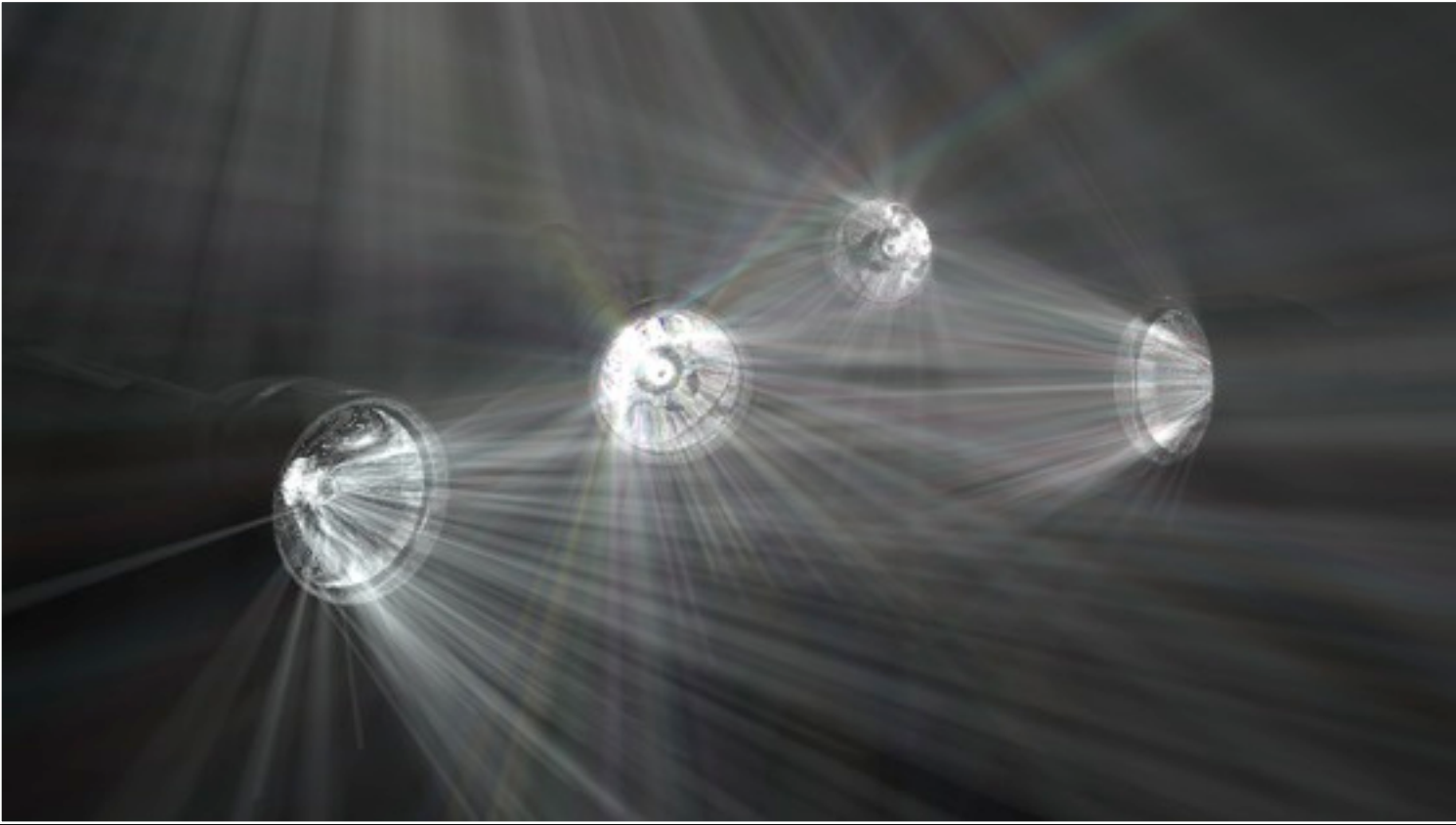
Pass 128



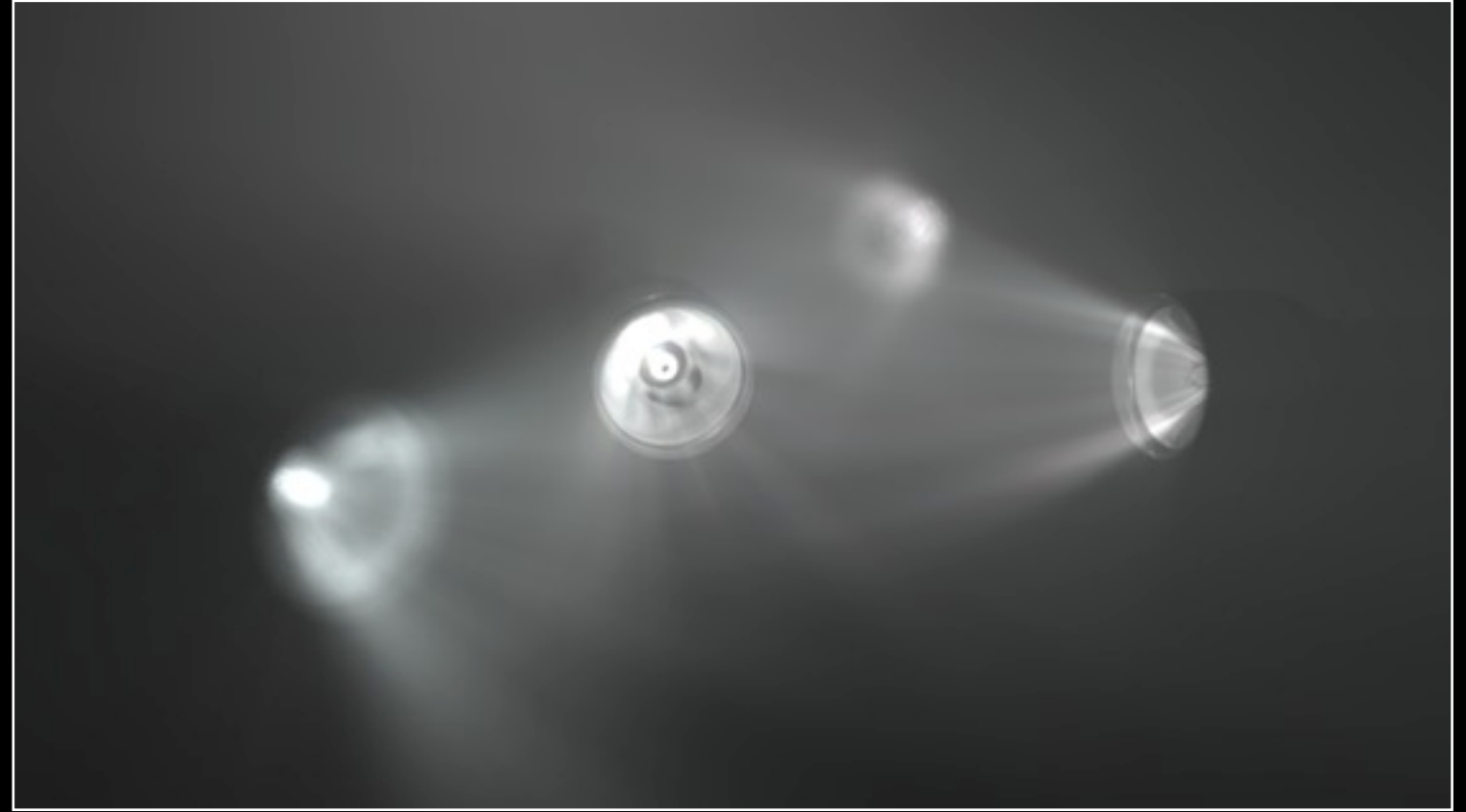
Average of Passes 1..128



Pass 256



Average of Passes 1..256



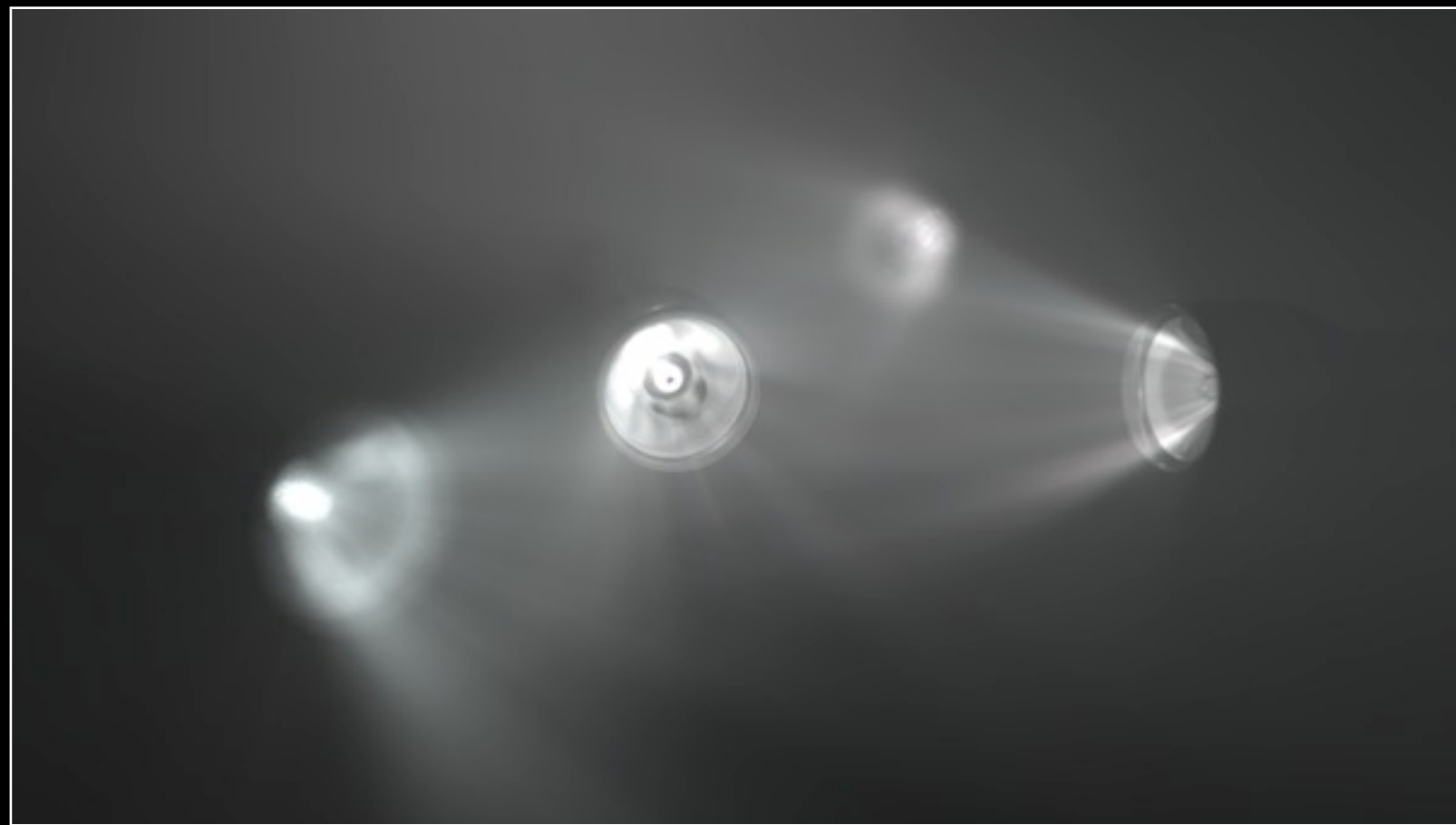
# FLASHLIGHTS

1280x720, Depth-of-Field

**Homogeneous**

2.1M Photon Beams

8 minutes



**Heterogeneous**

2.1M Photon Beams

10.8 minutes



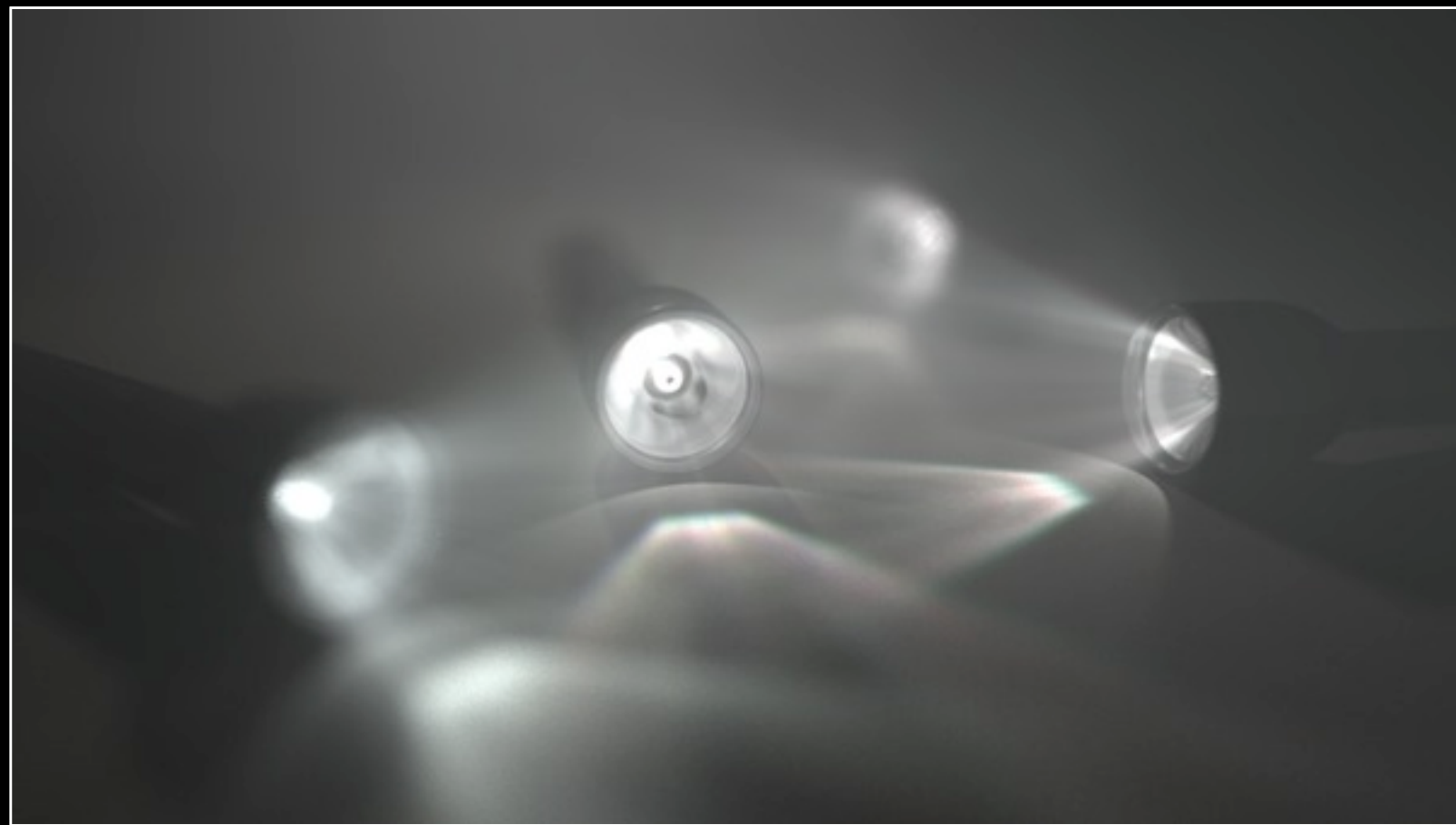
# FLASHLIGHTS

1280x720, Depth-of-Field

**Homogeneous**

2.1M Photon Beams

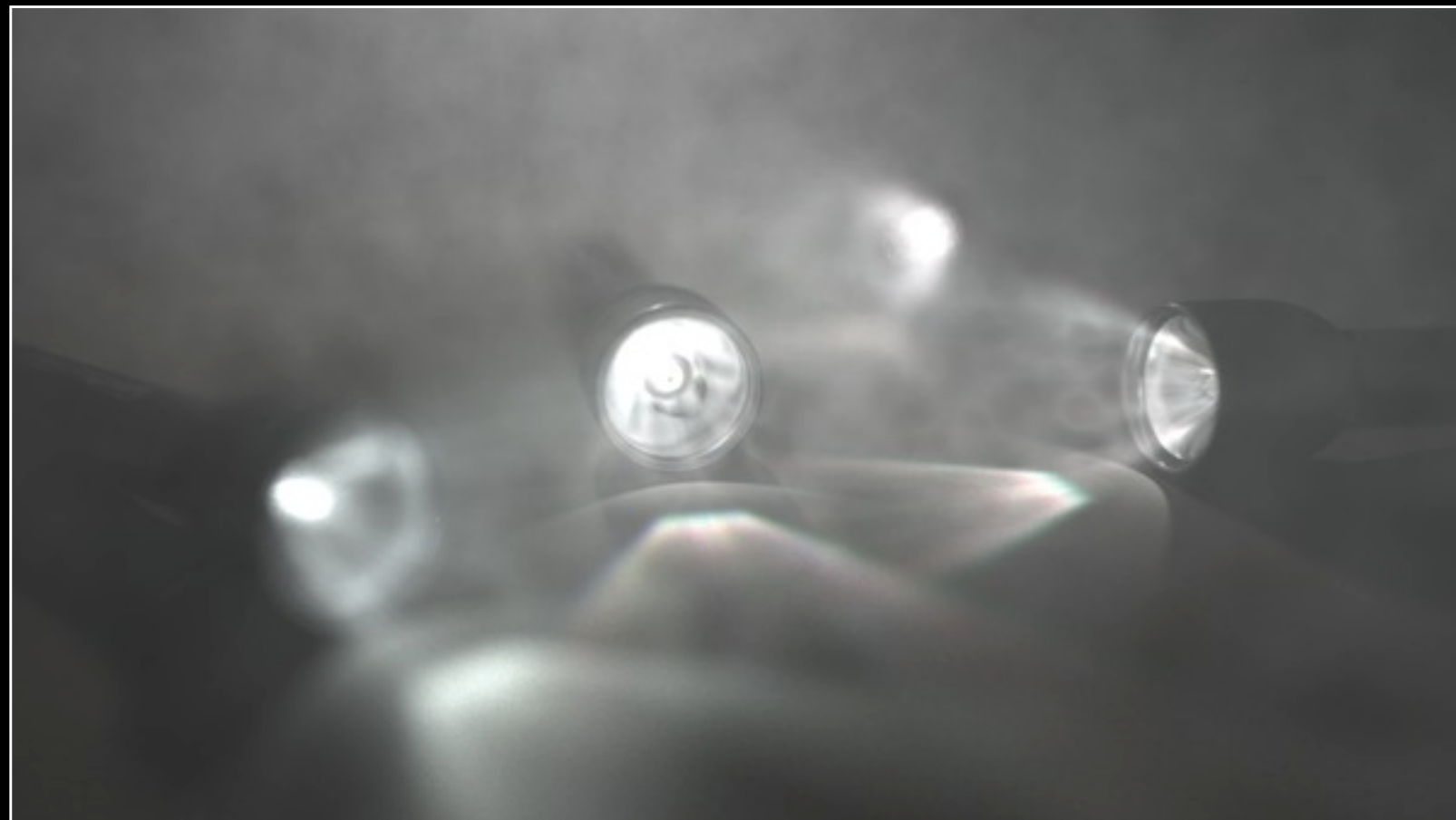
8 minutes



**Heterogeneous**

2.1M Photon Beams

10.8 minutes

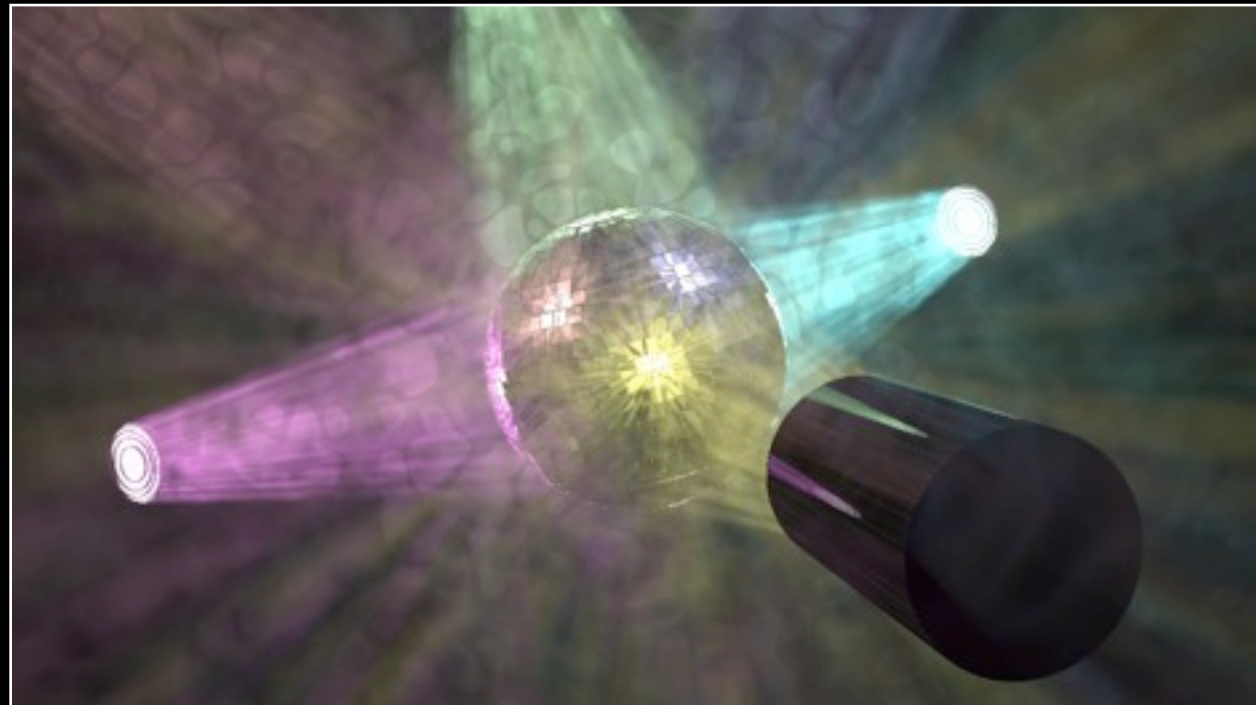
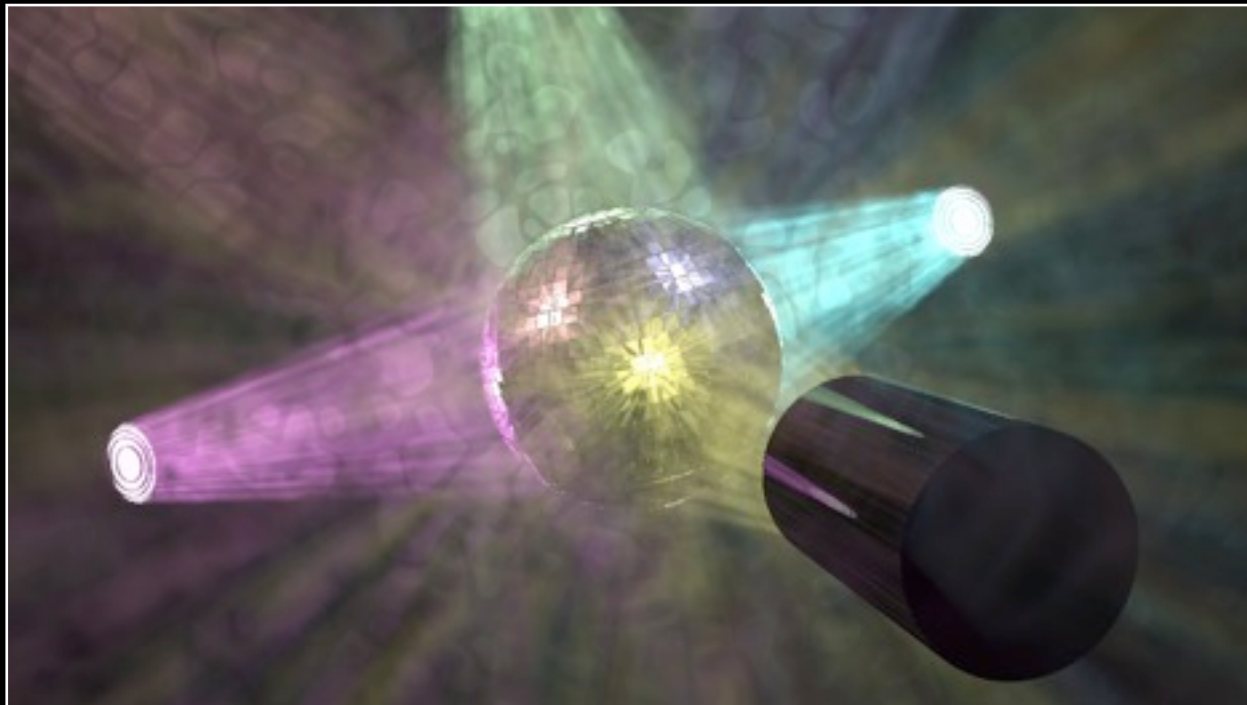
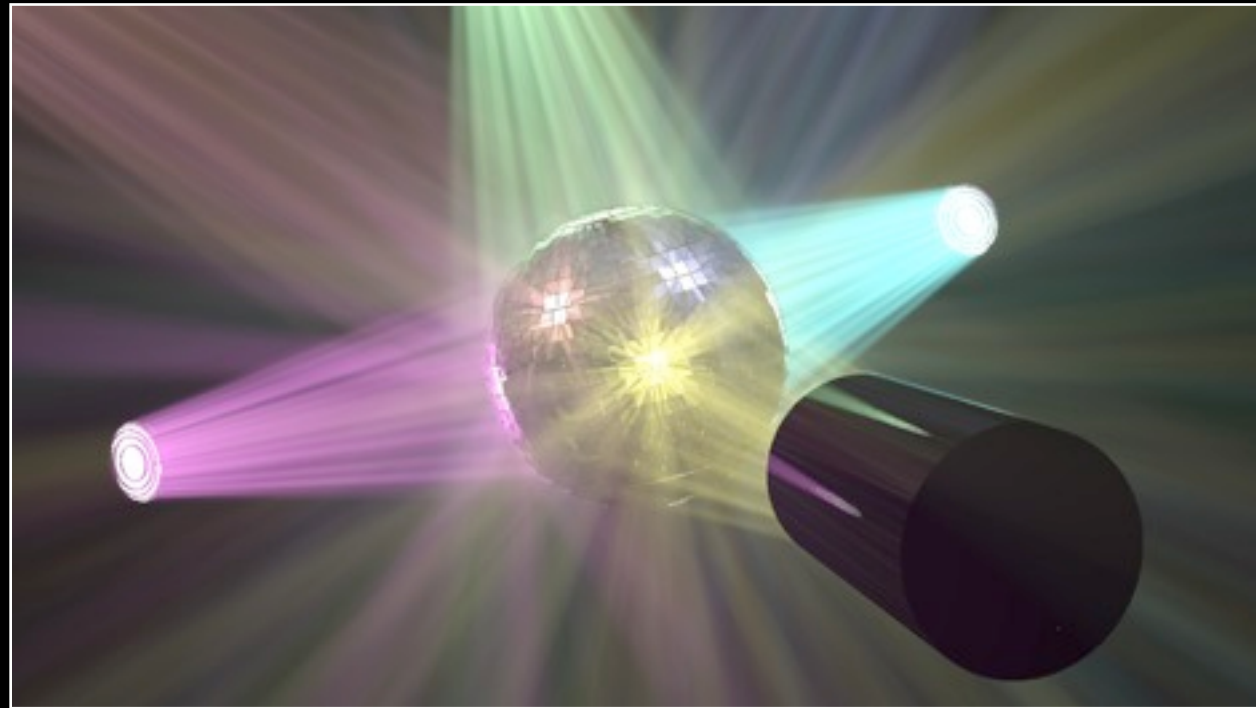
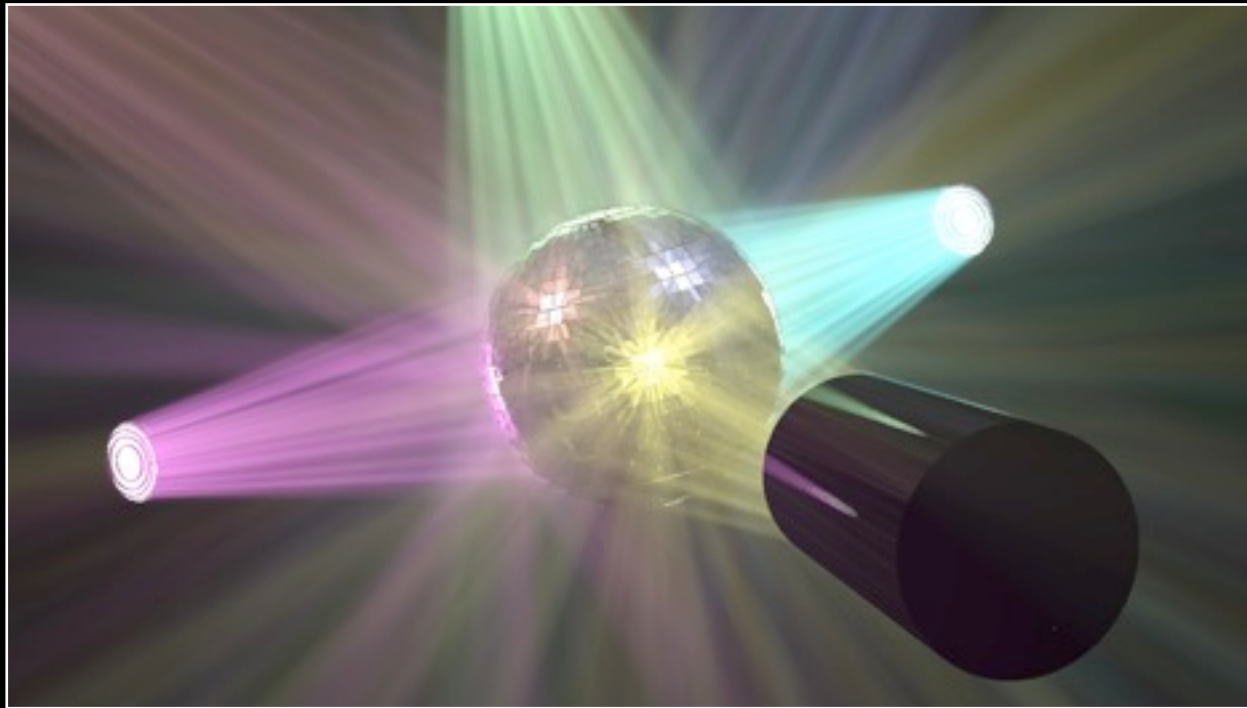


# DISCO

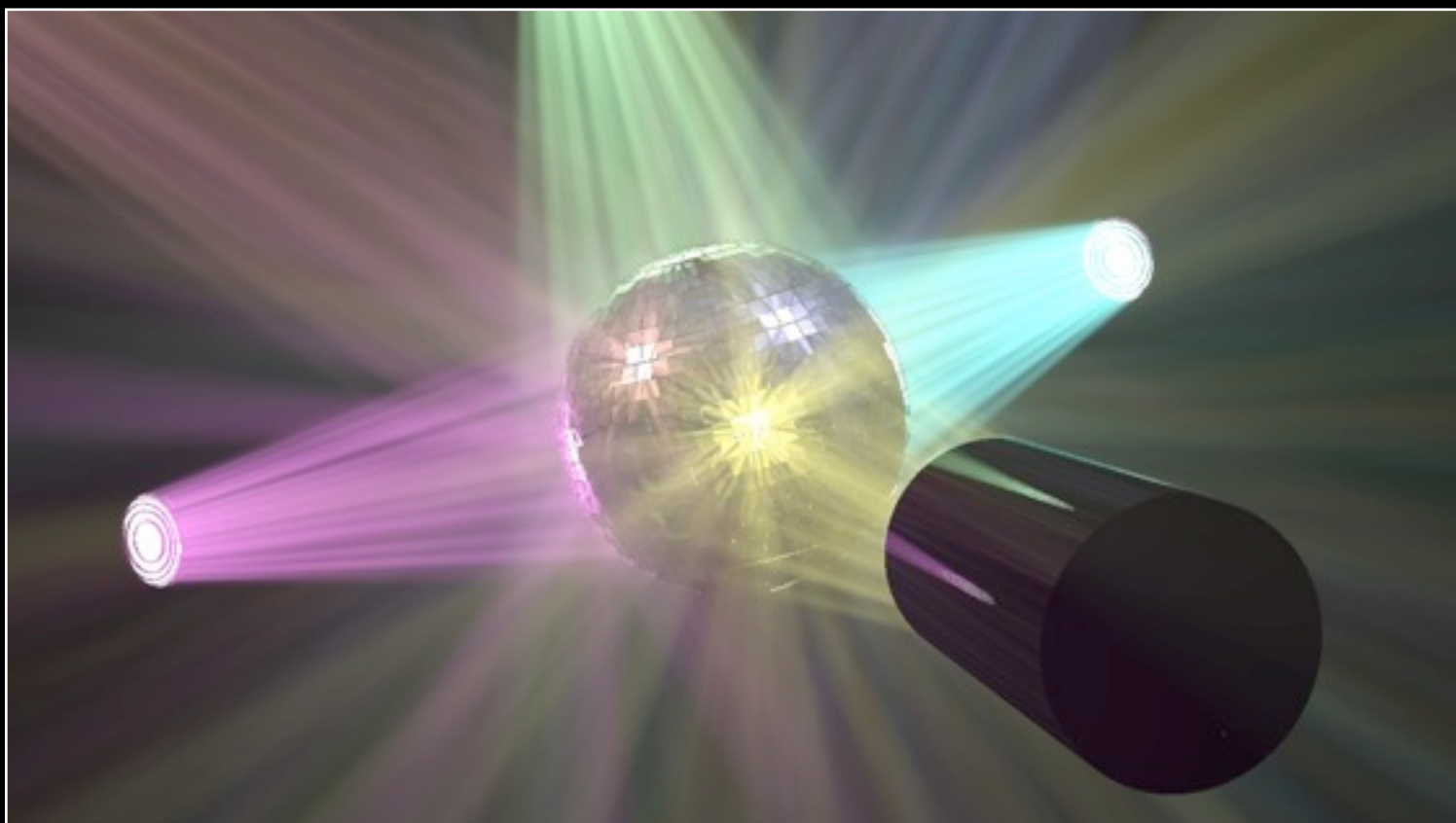
1280x720, Depth-of-Field

Pass 1

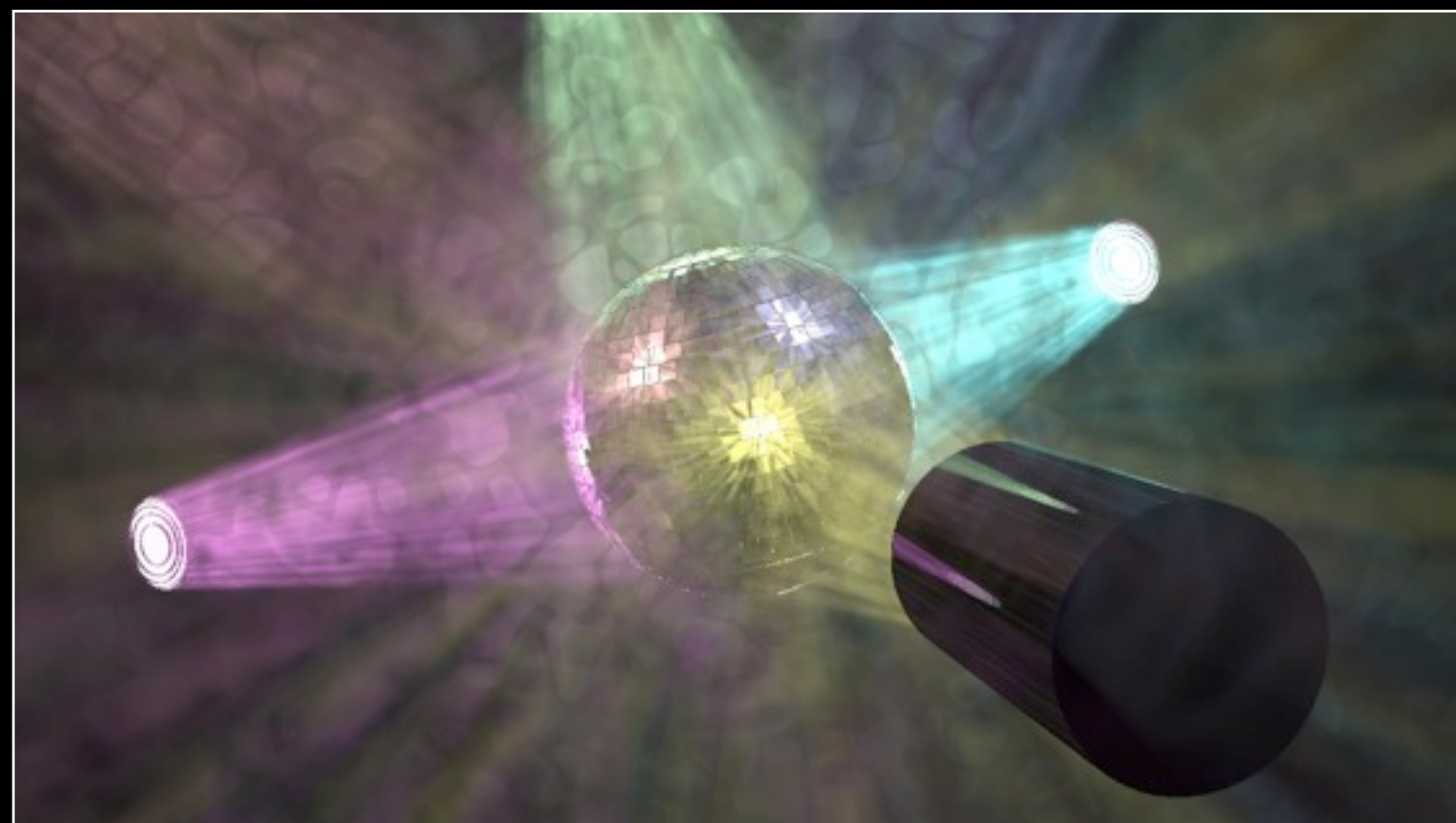
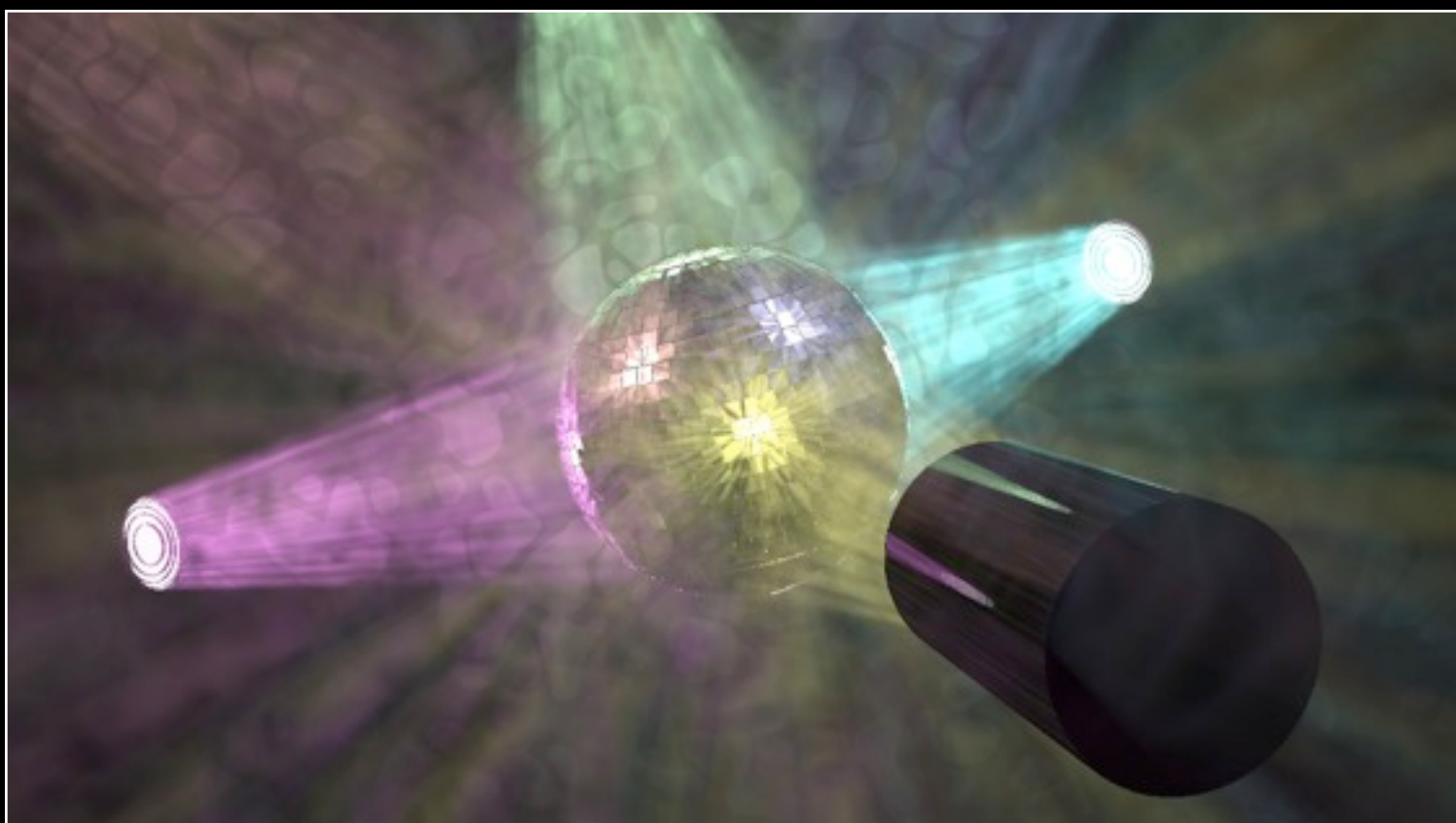
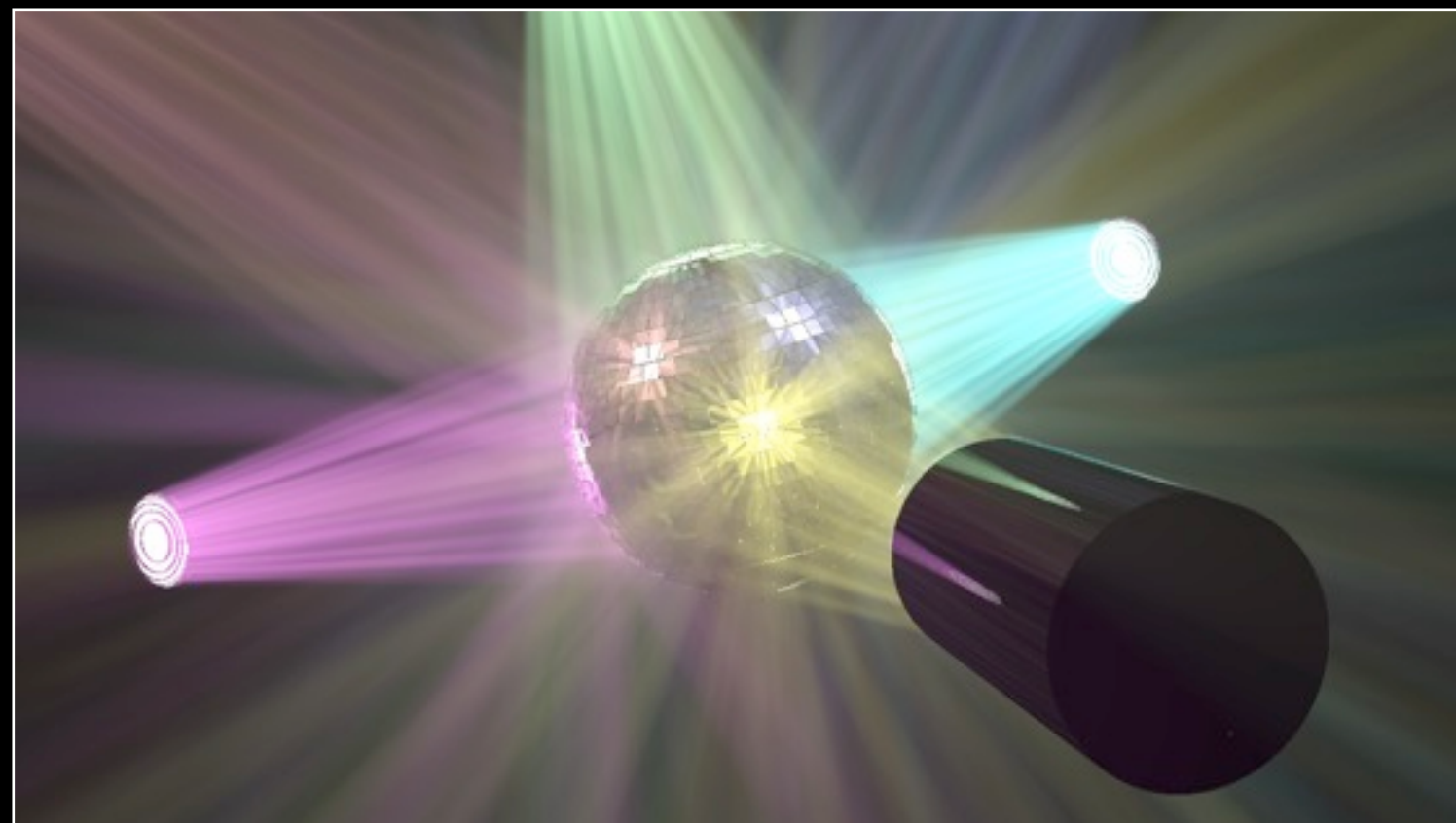
Average of Passes 1..1



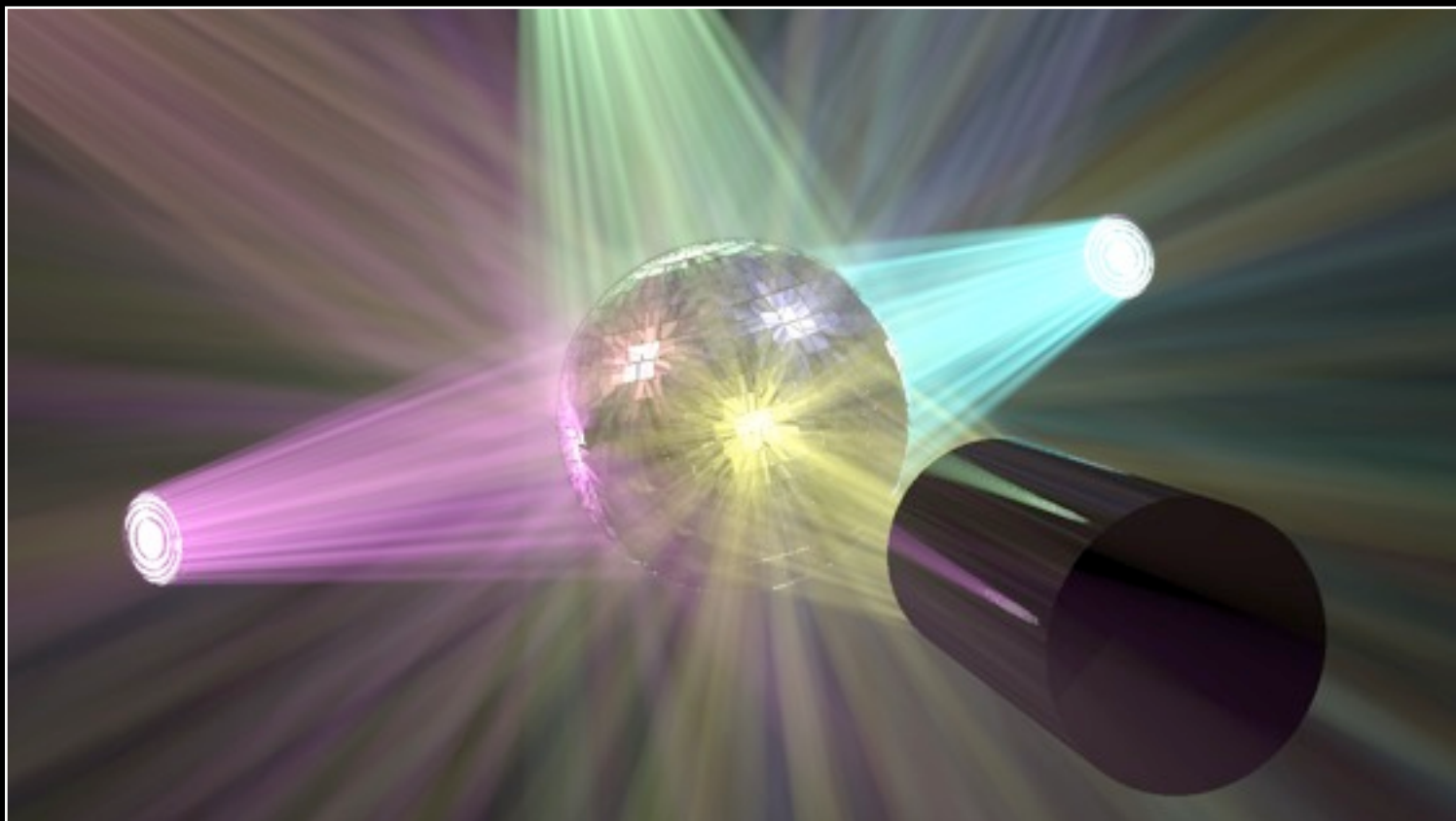
Pass 1



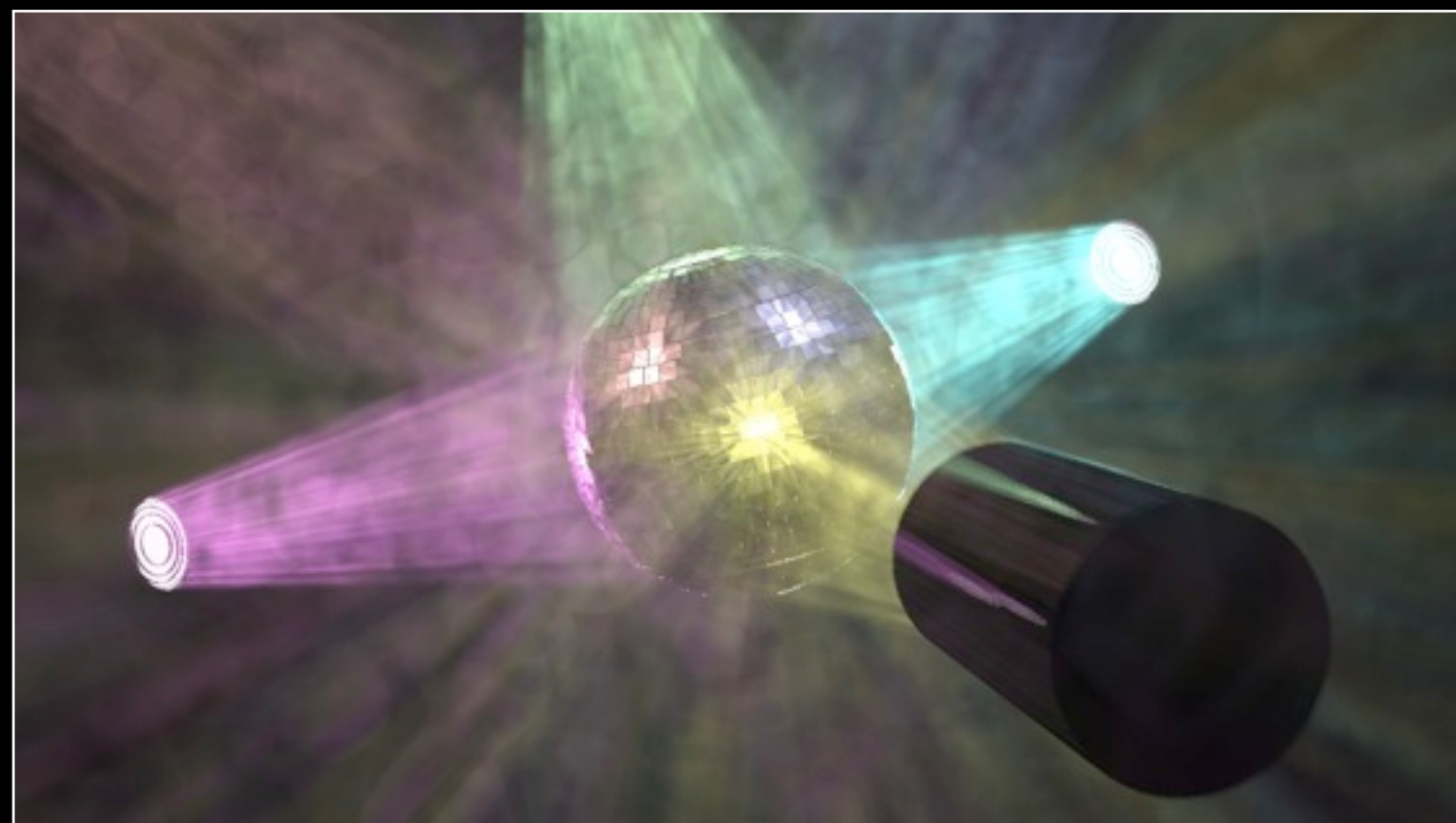
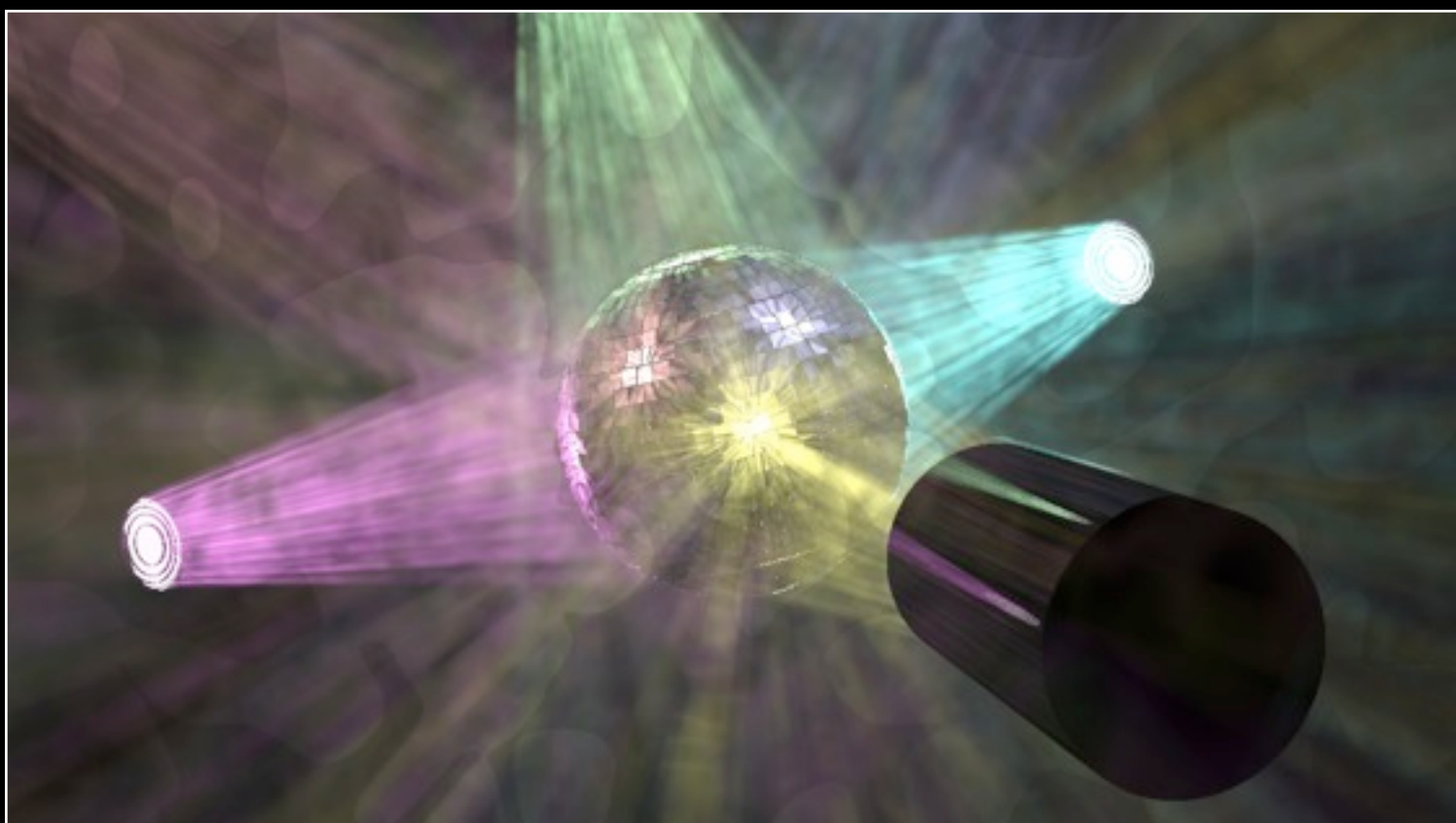
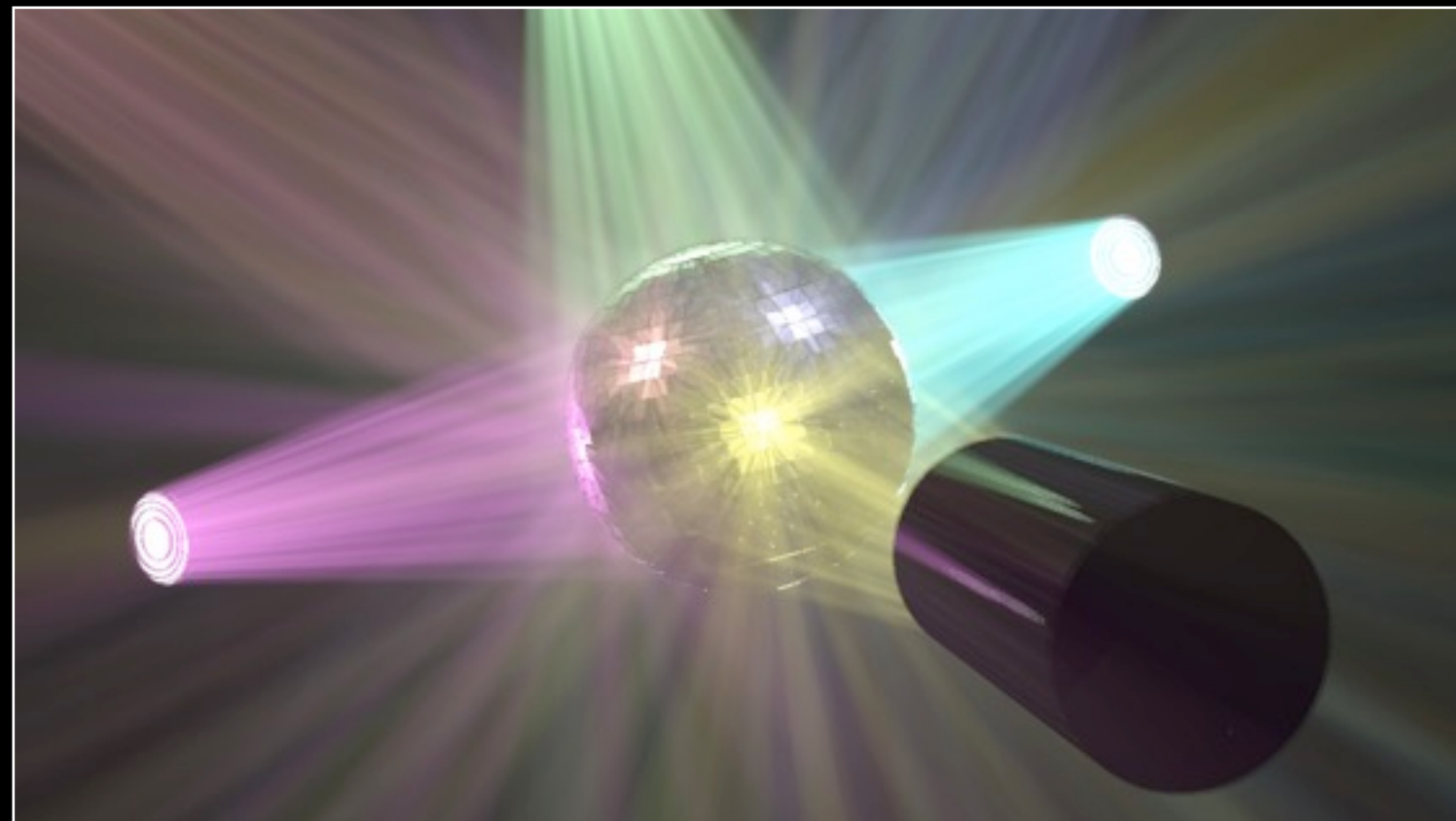
Average of Passes 1..1



Pass 2

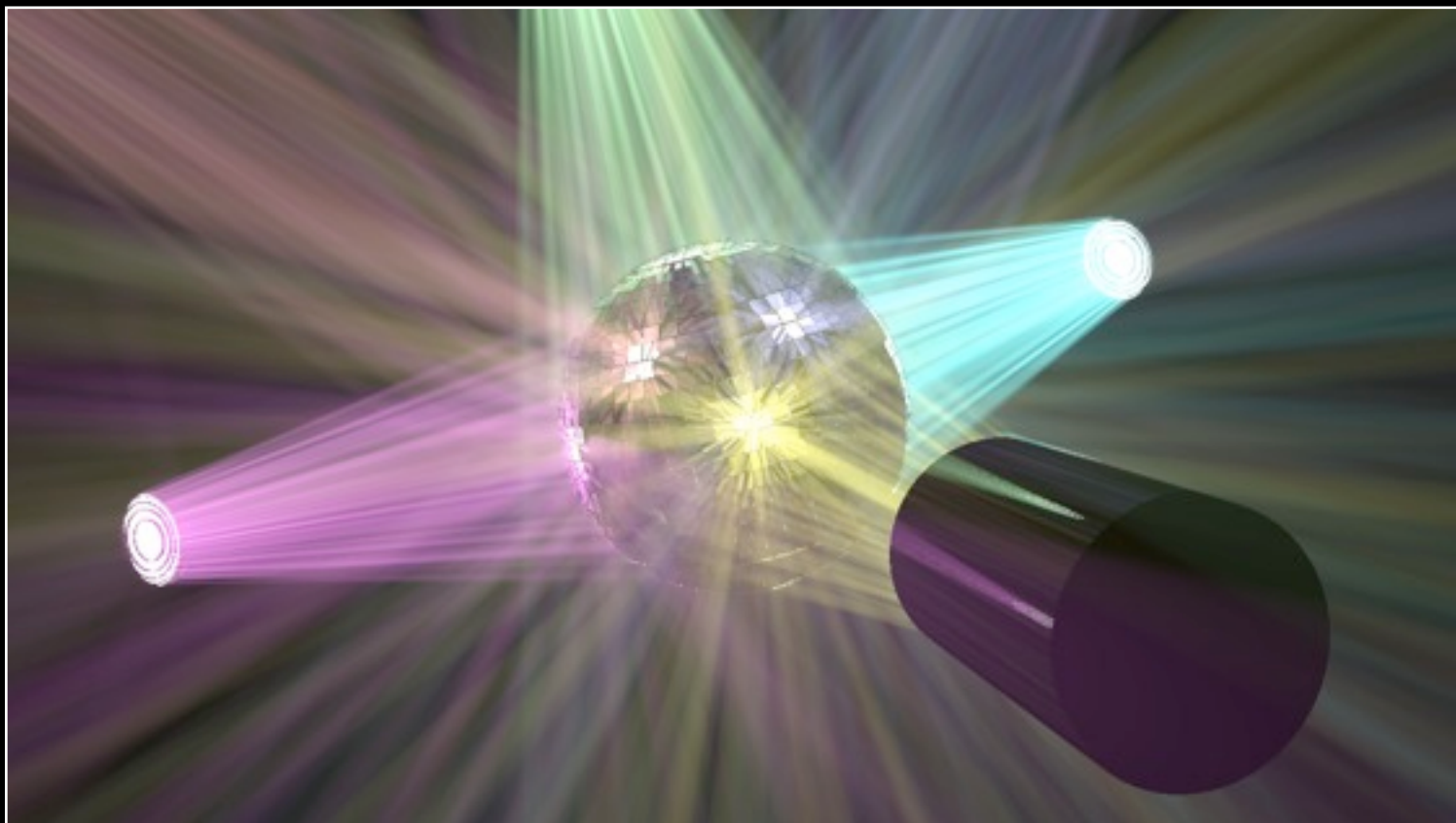


Average of Passes 1..2

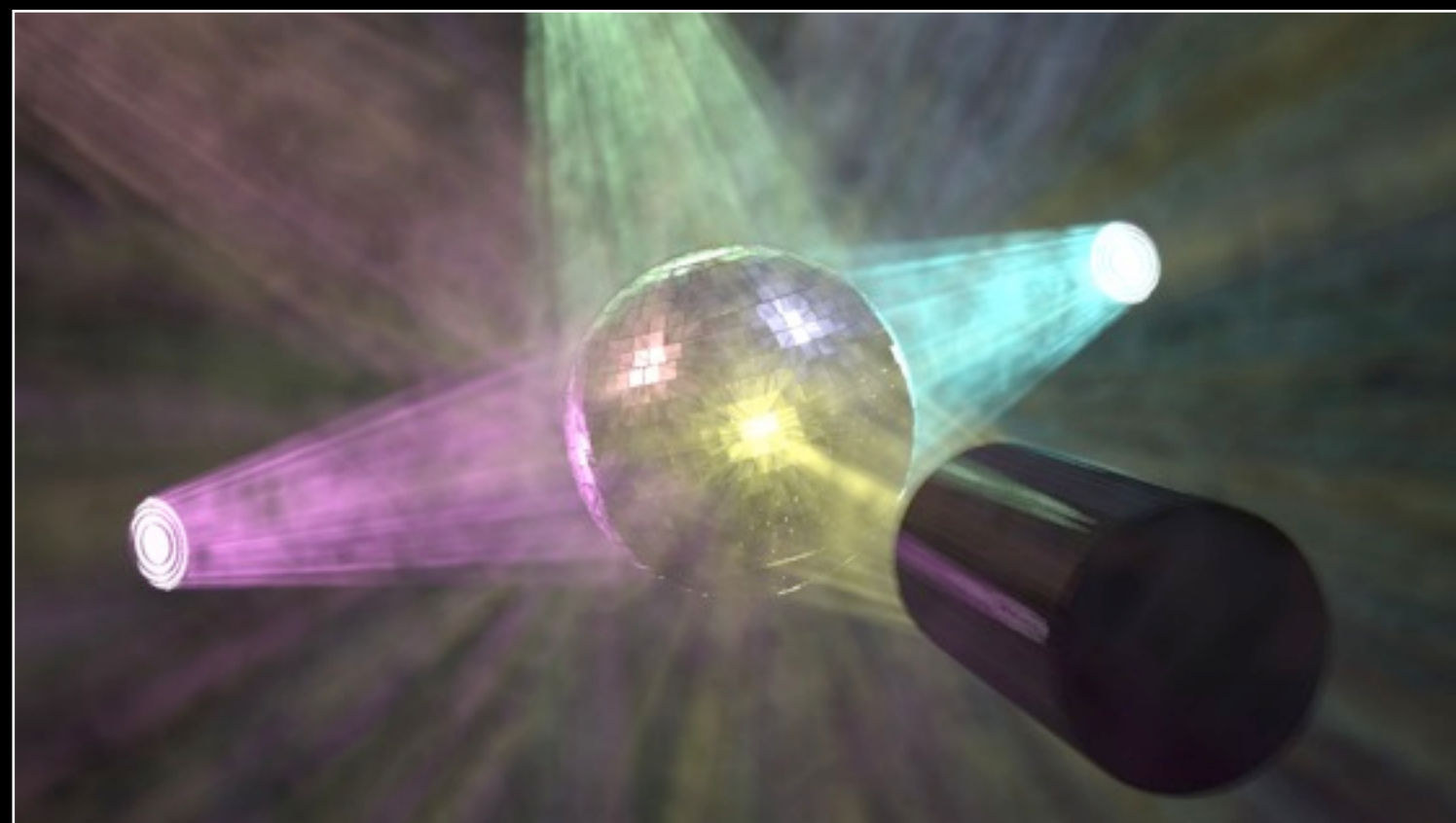
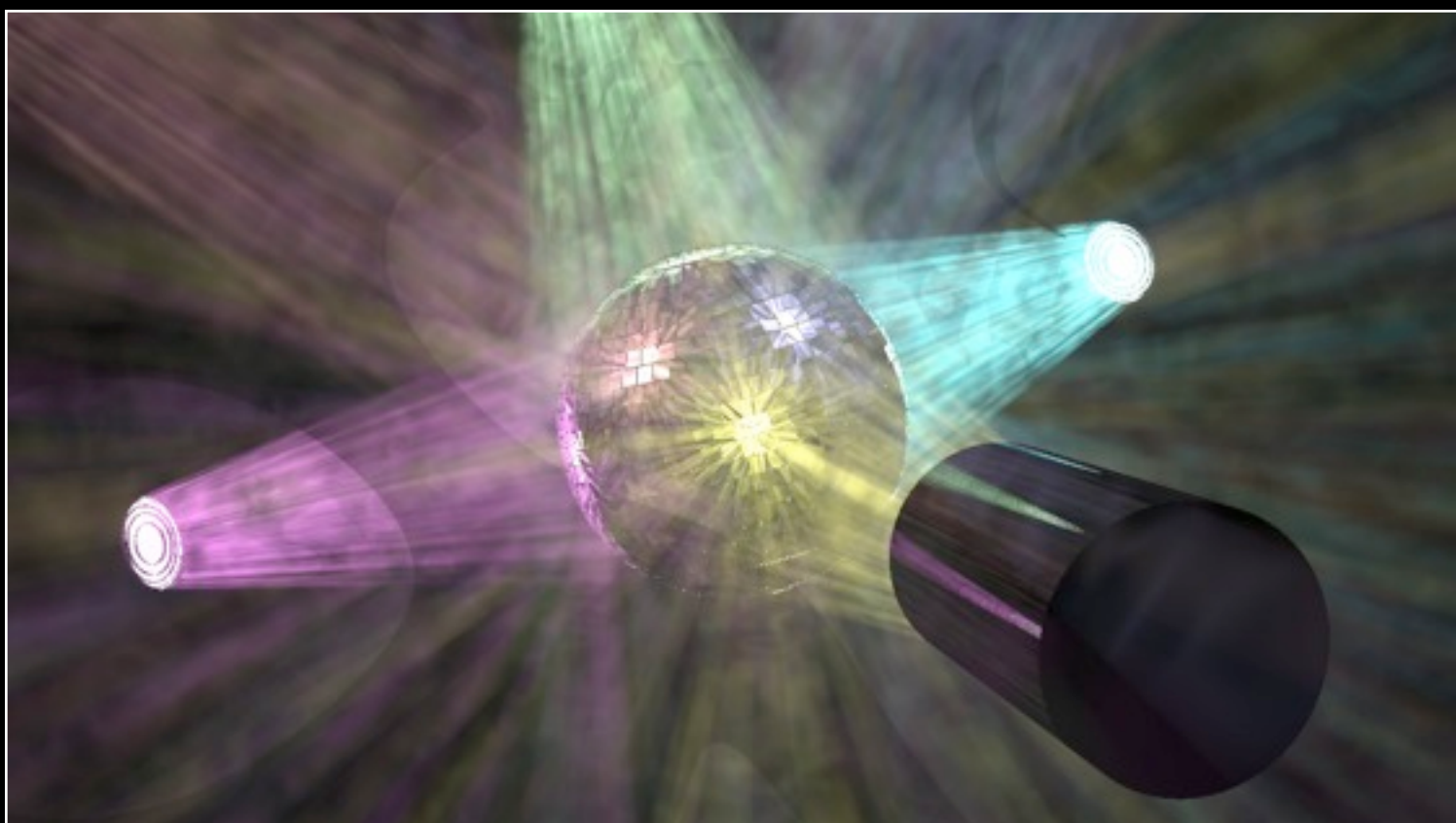
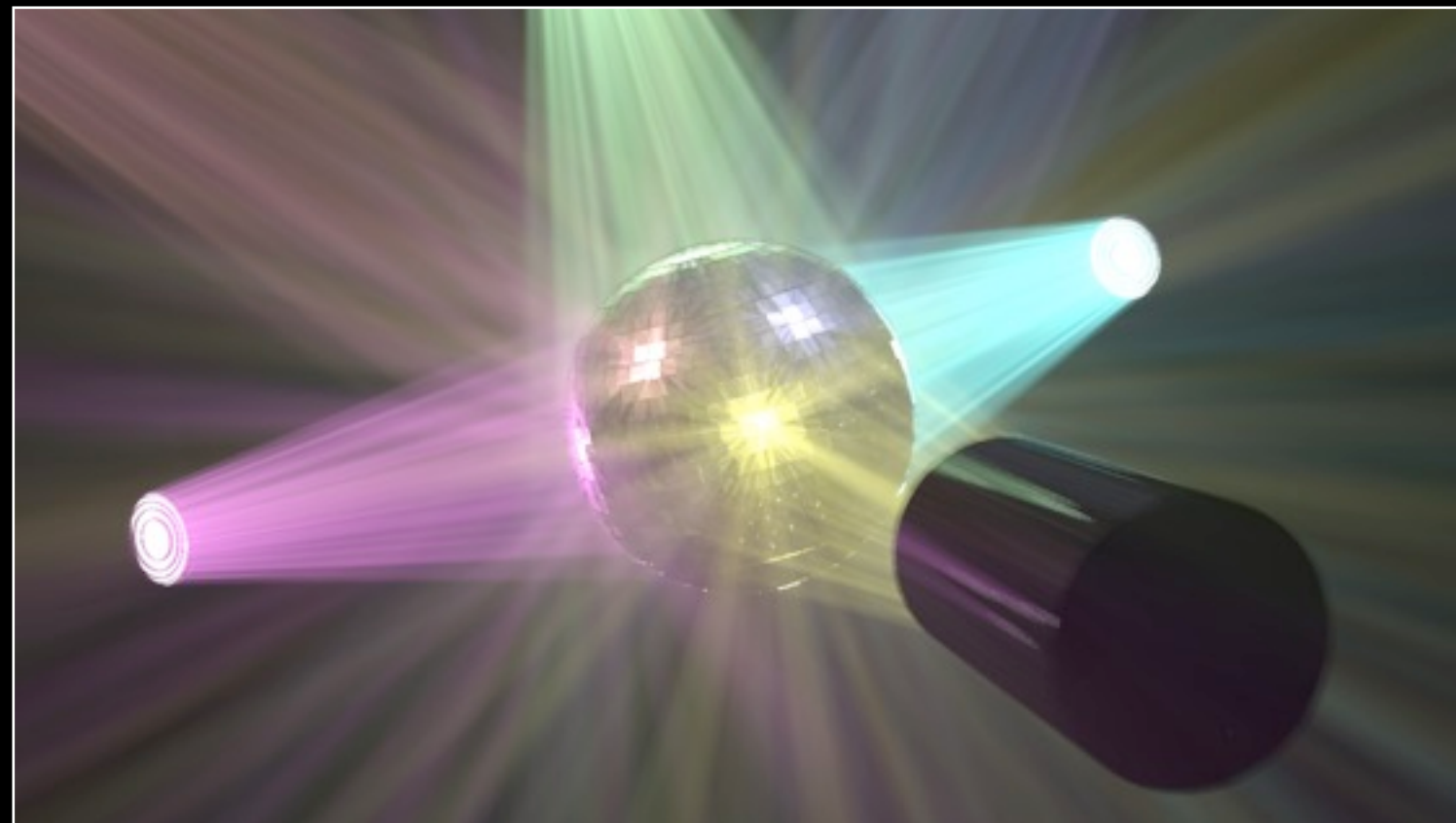




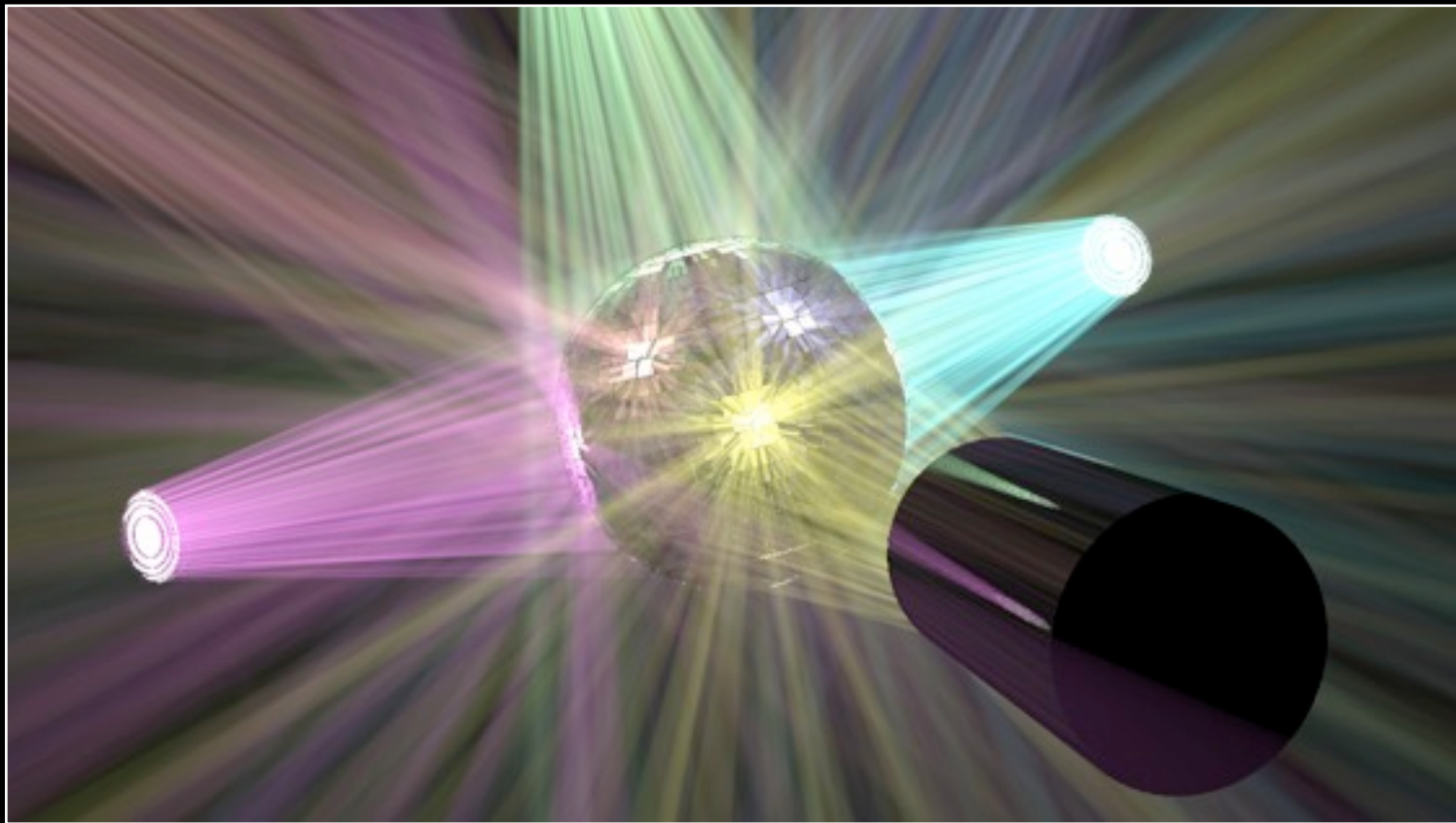
Pass 4



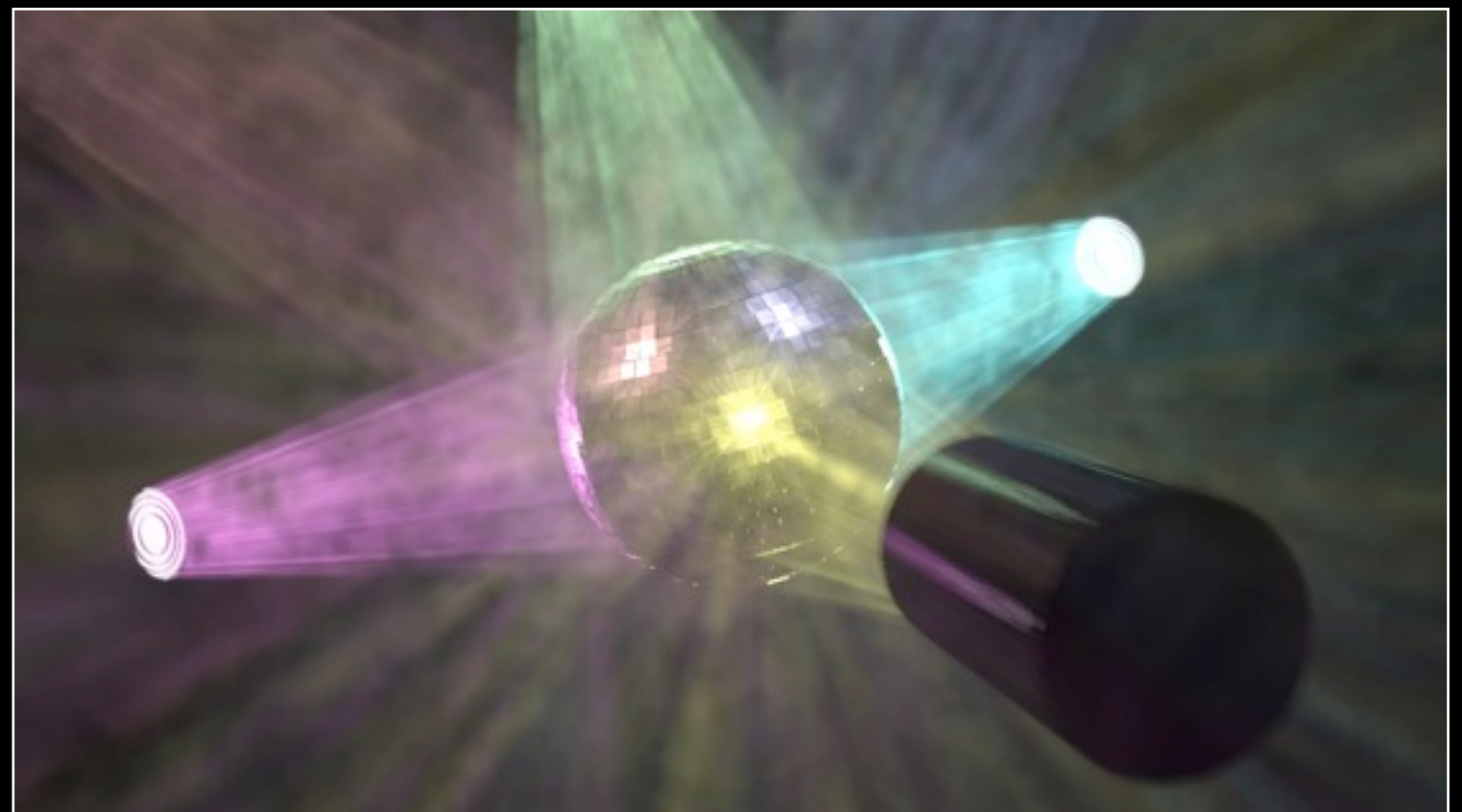
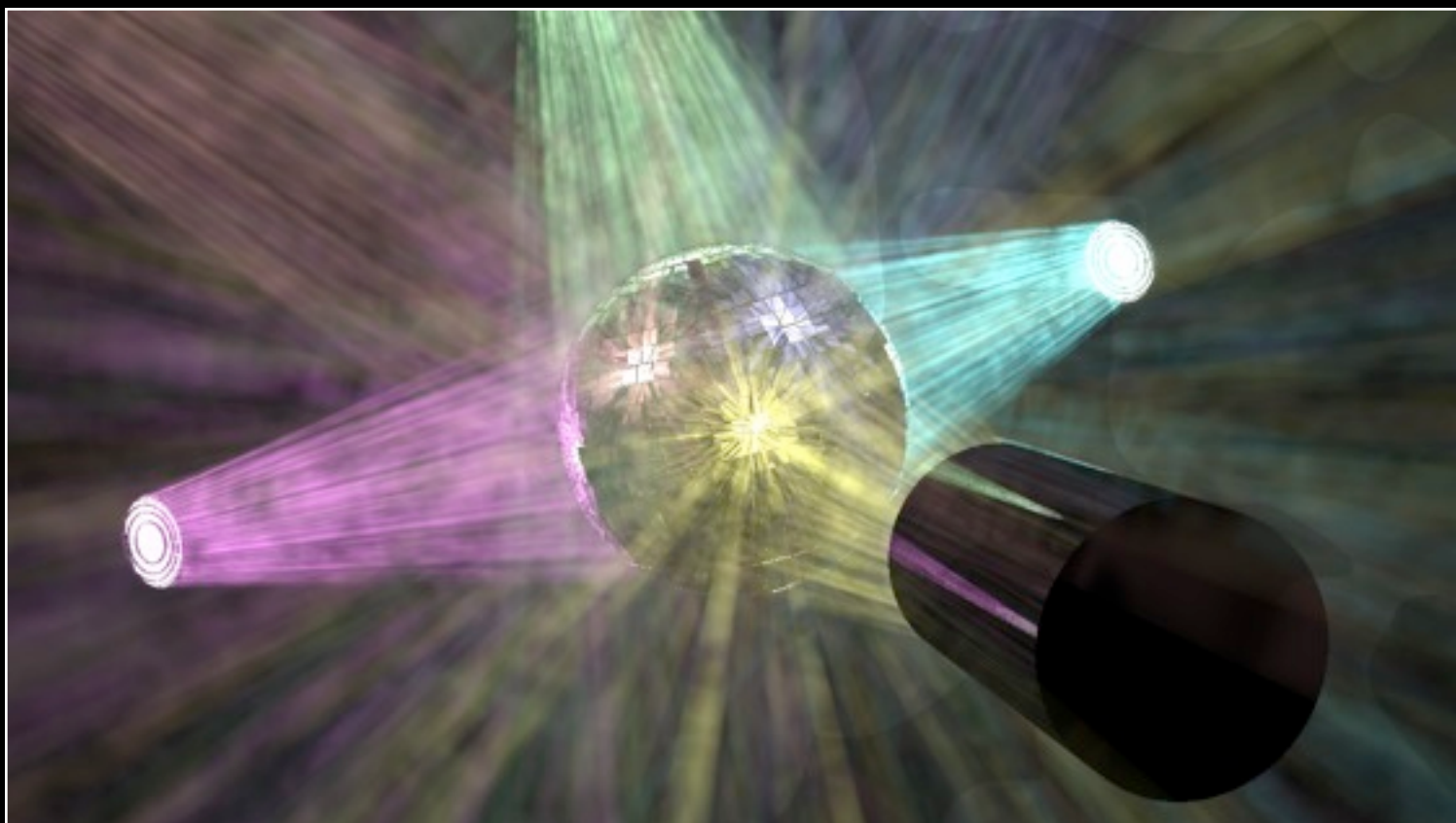
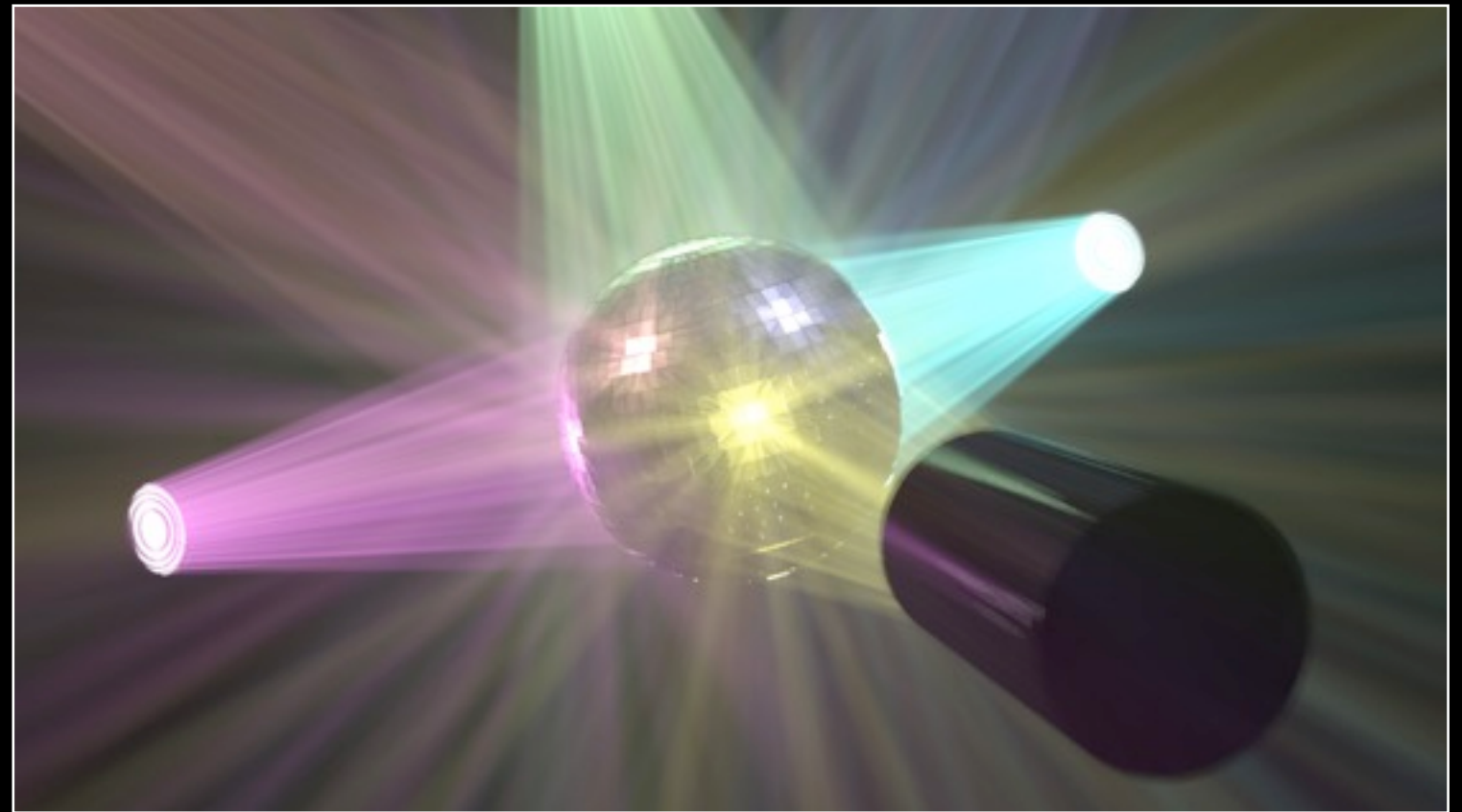
Average of Passes 1..4



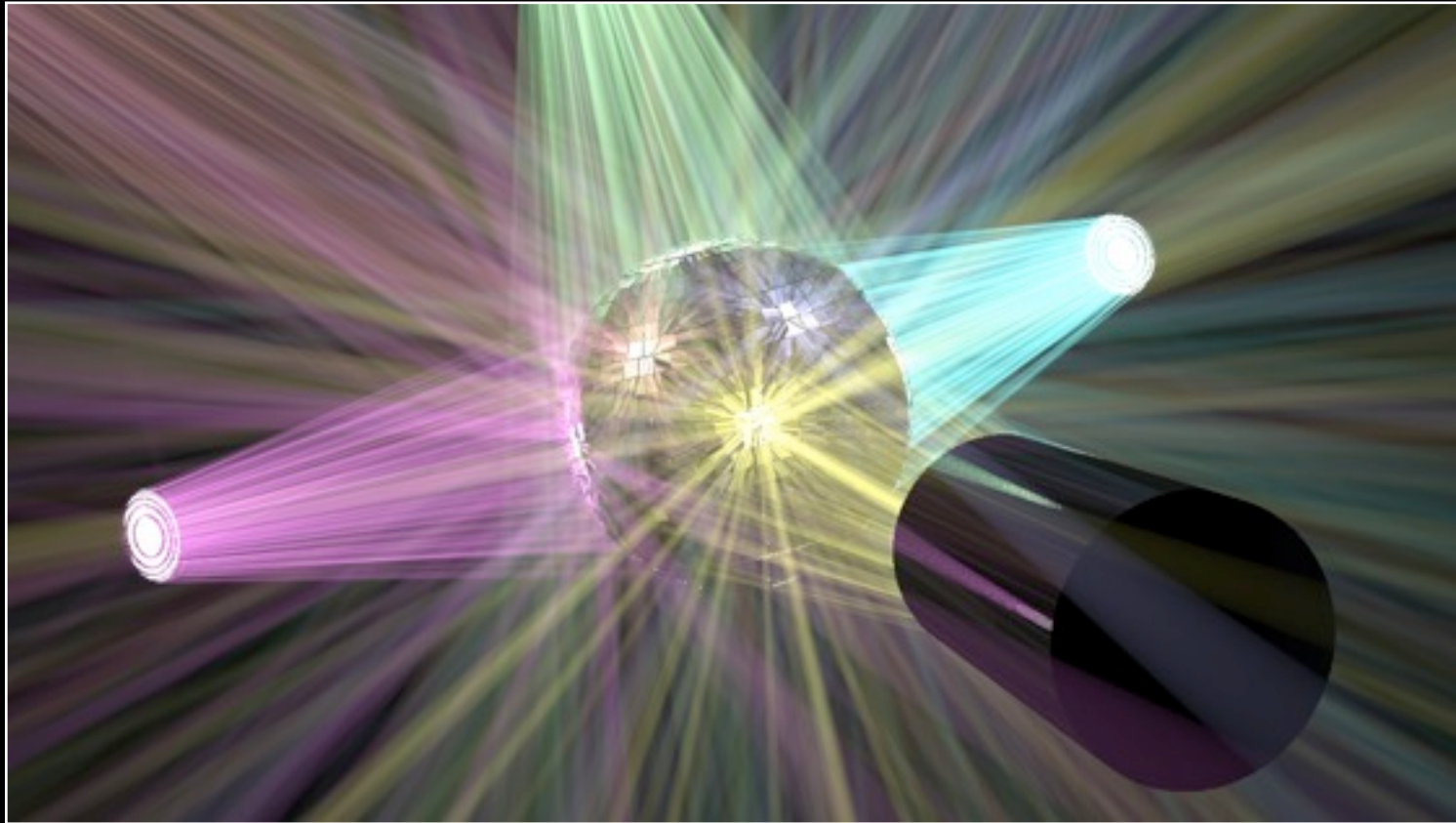
Pass 8



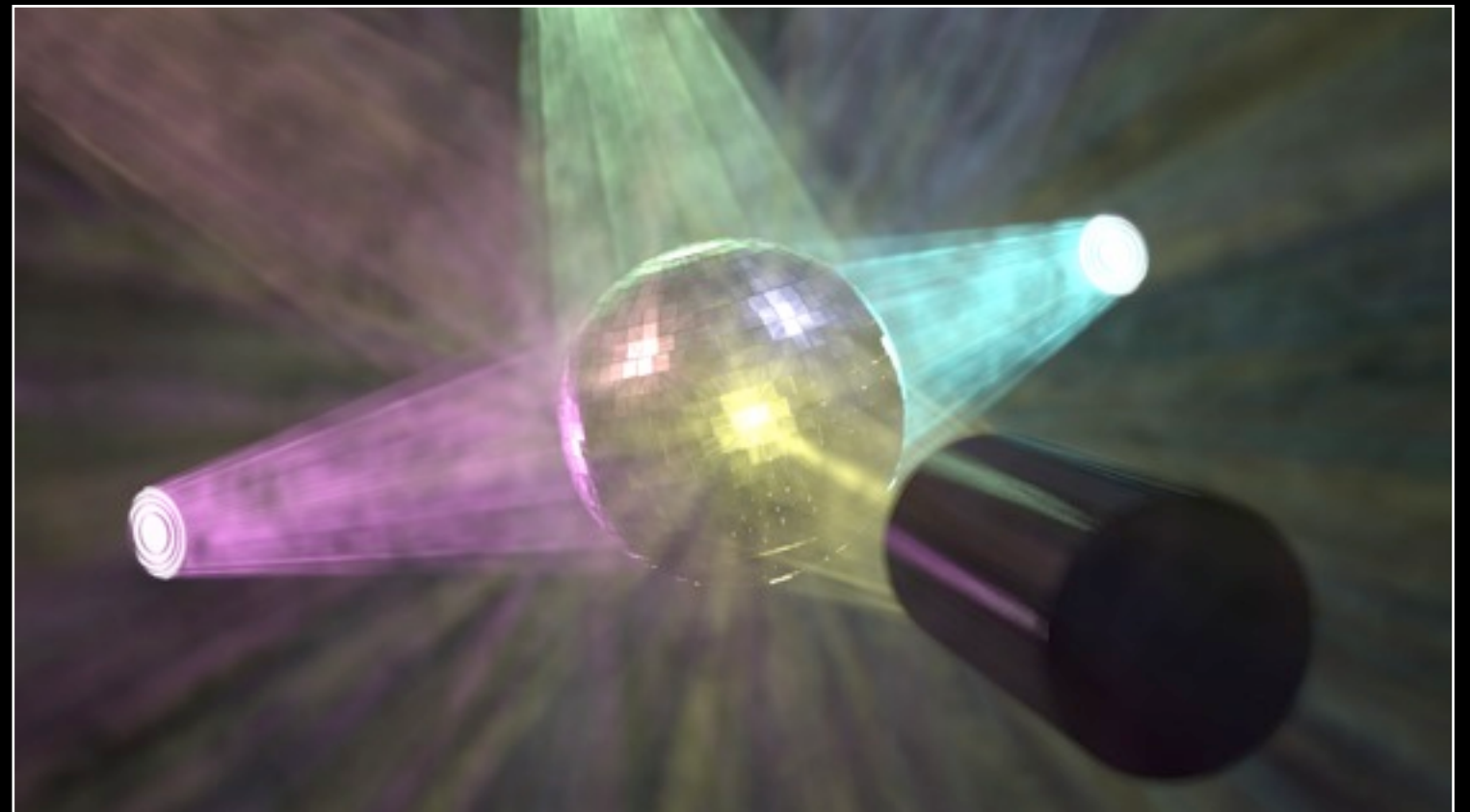
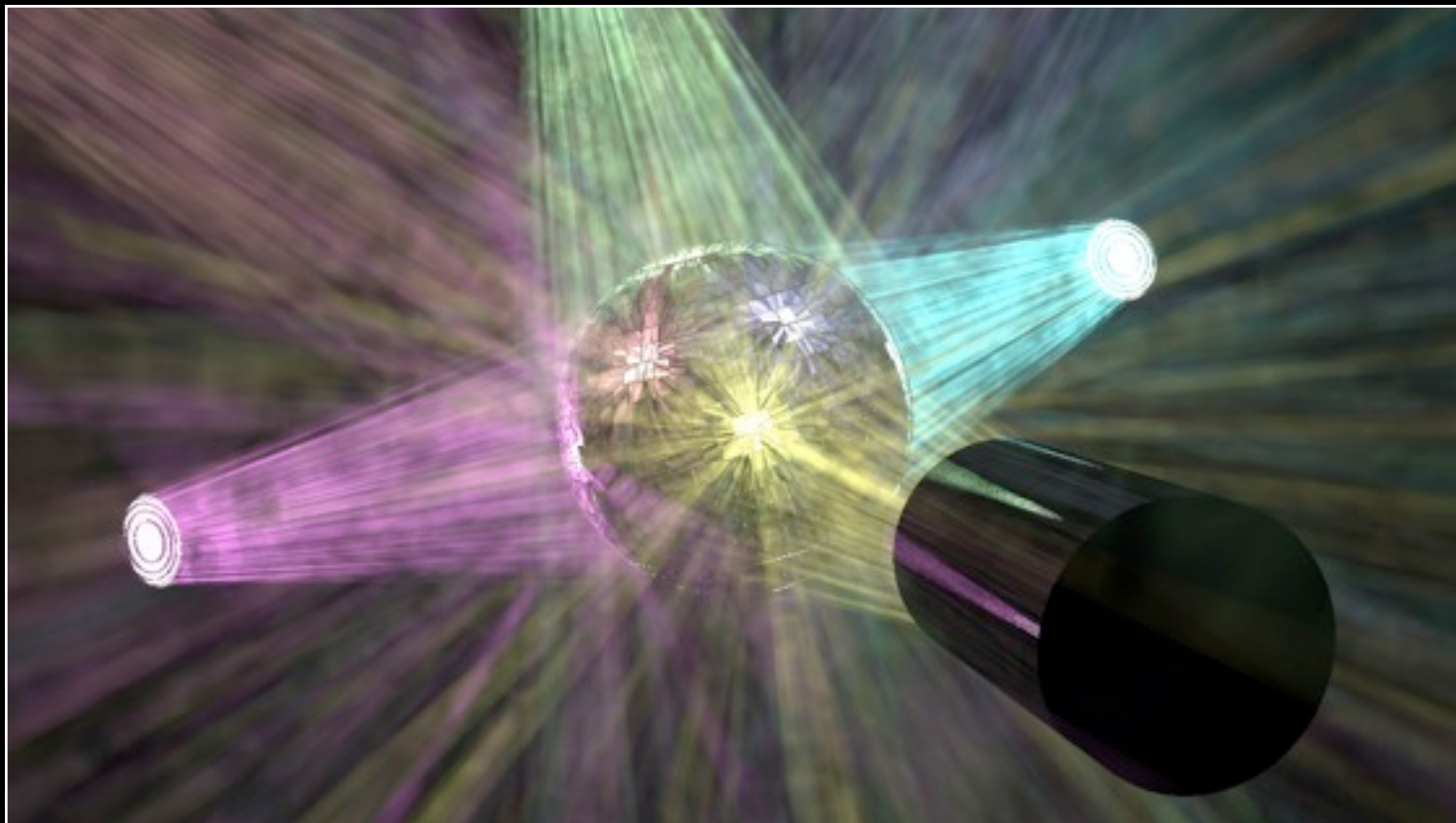
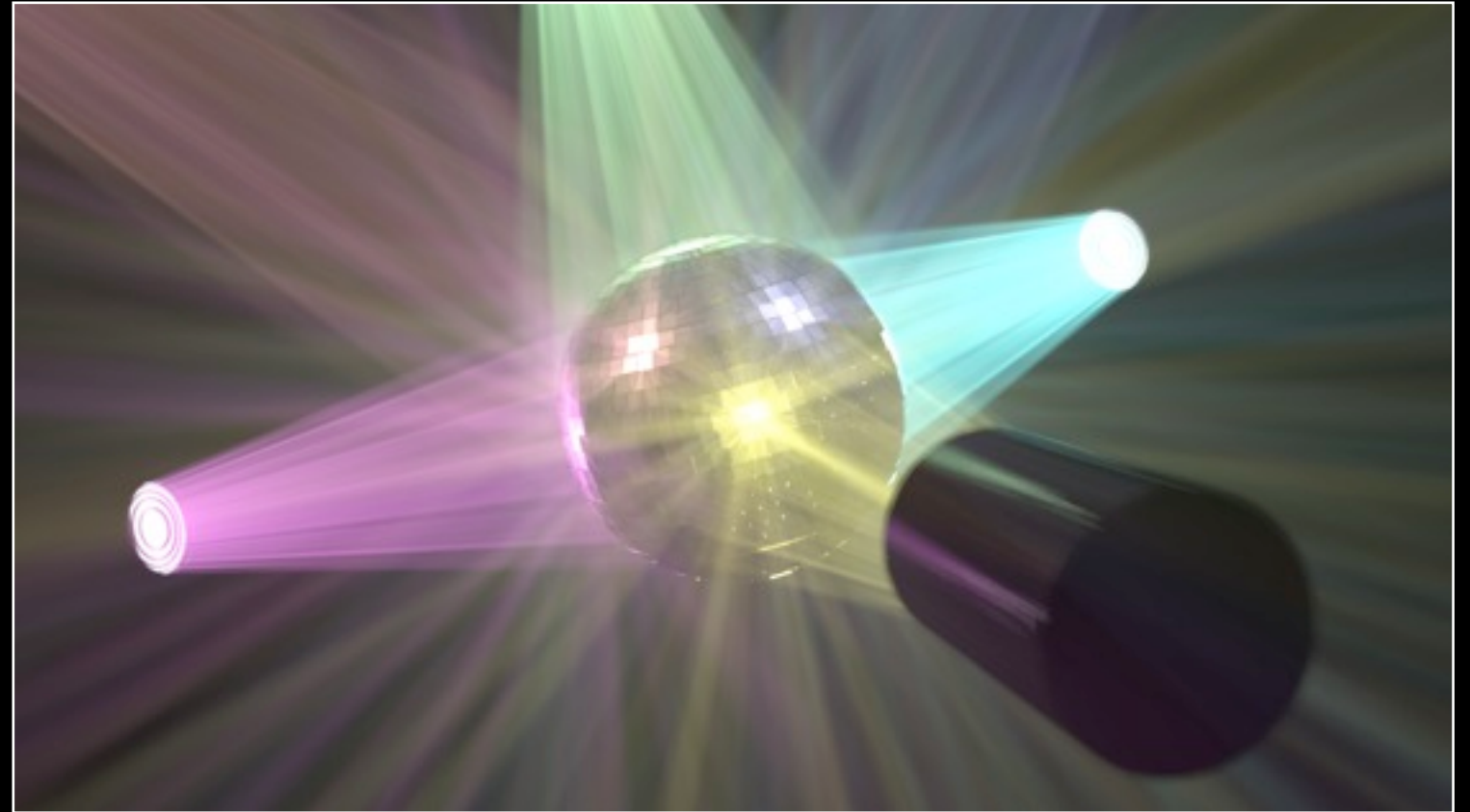
Average of Passes 1..8



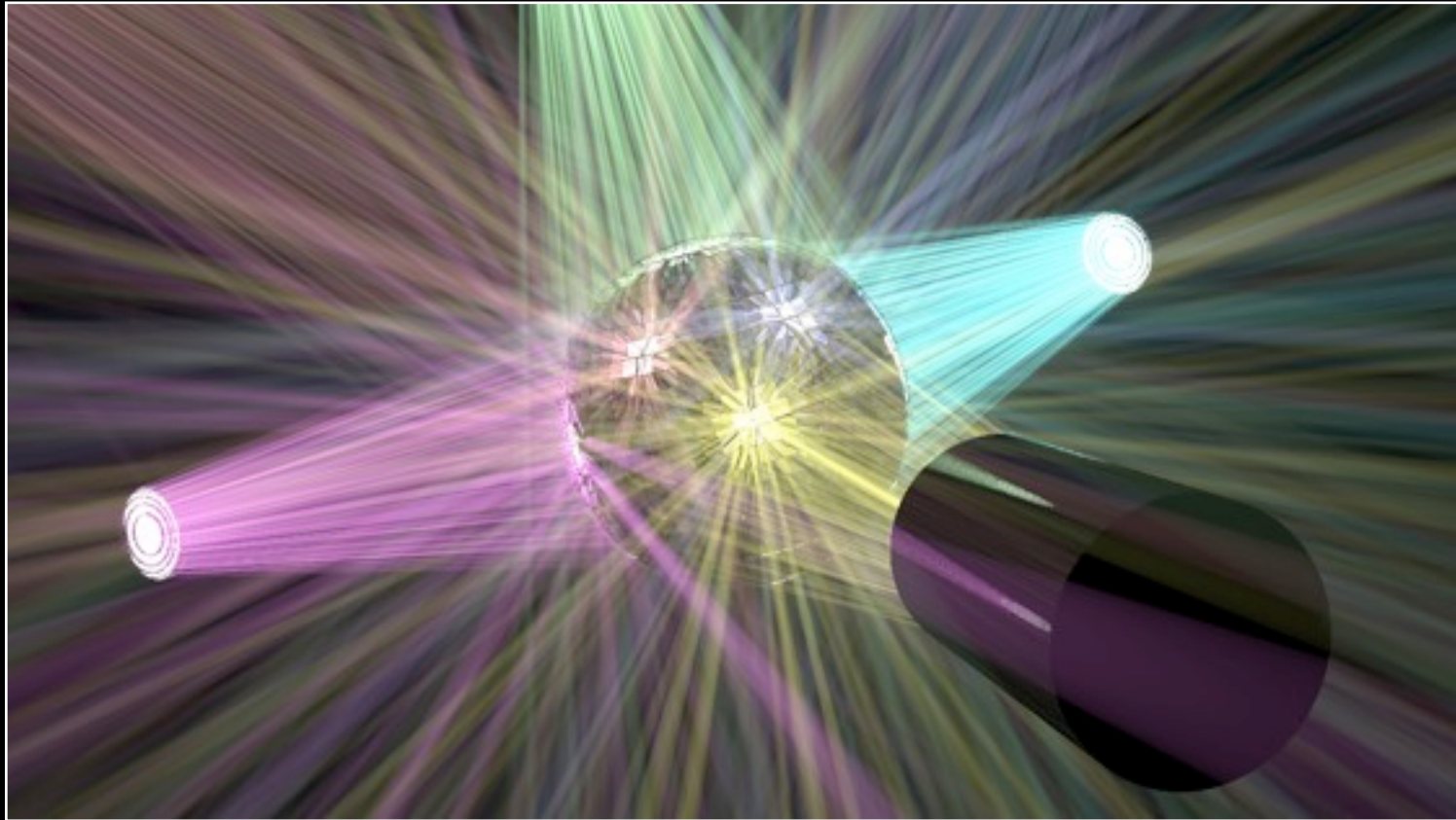
Pass 16



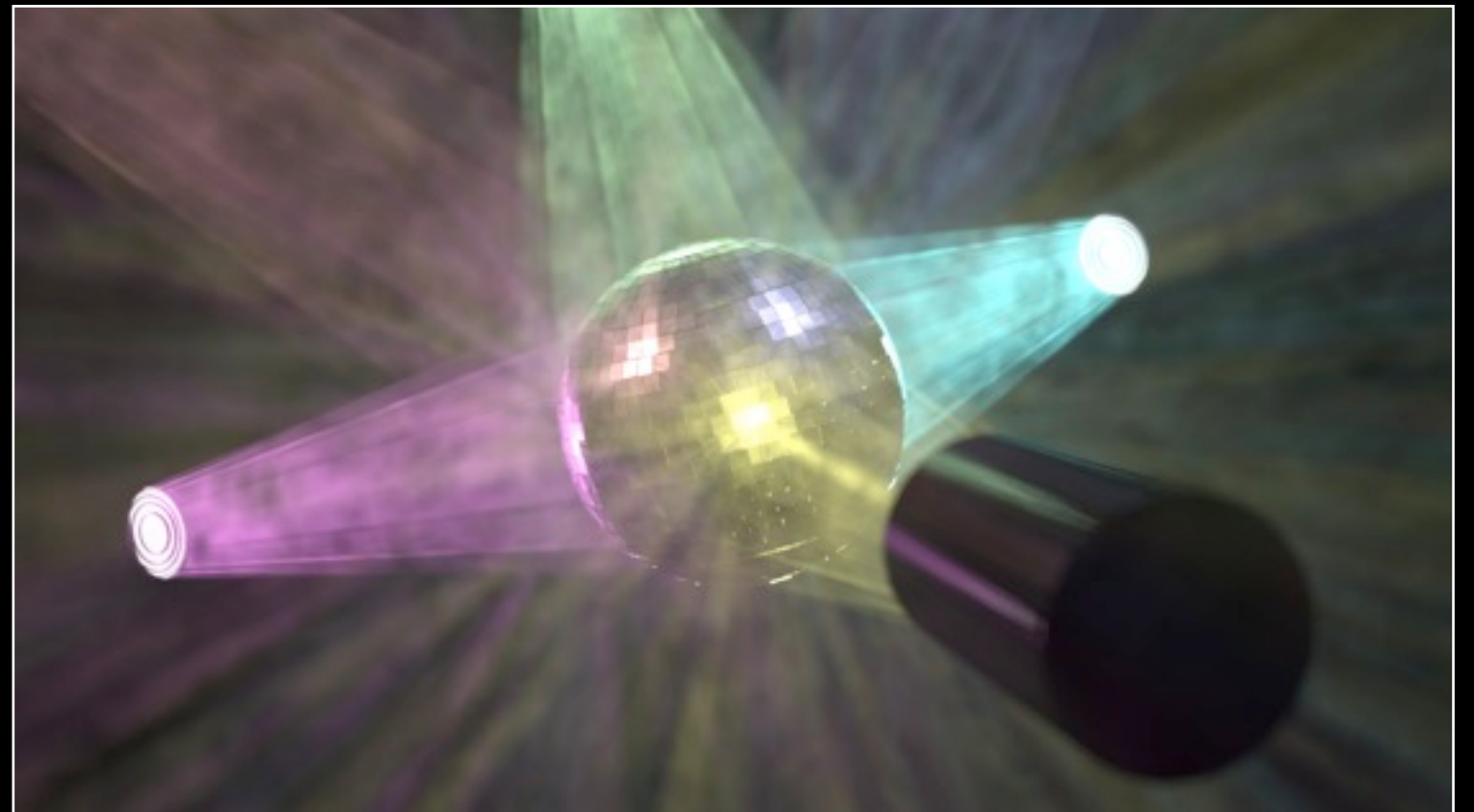
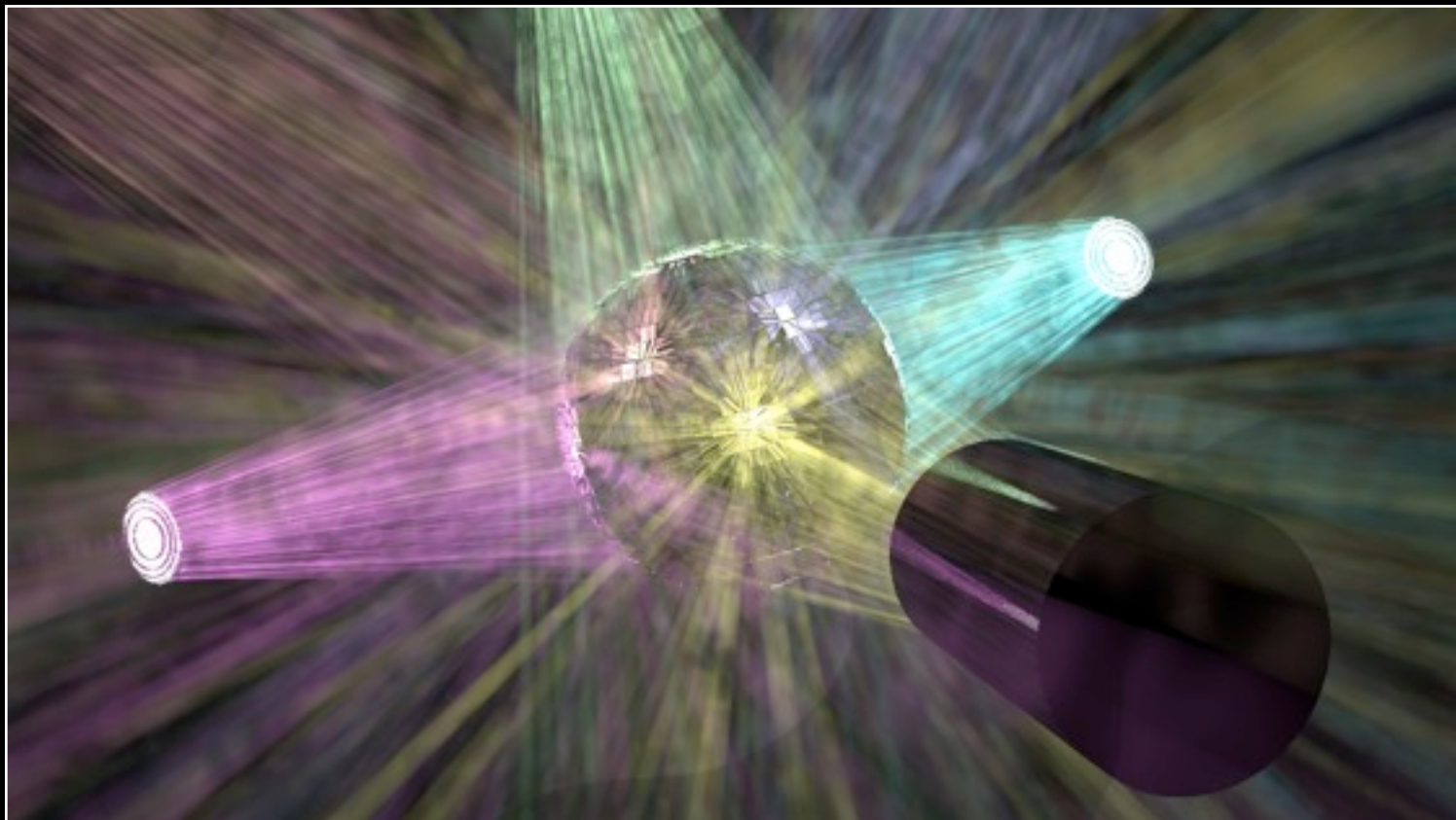
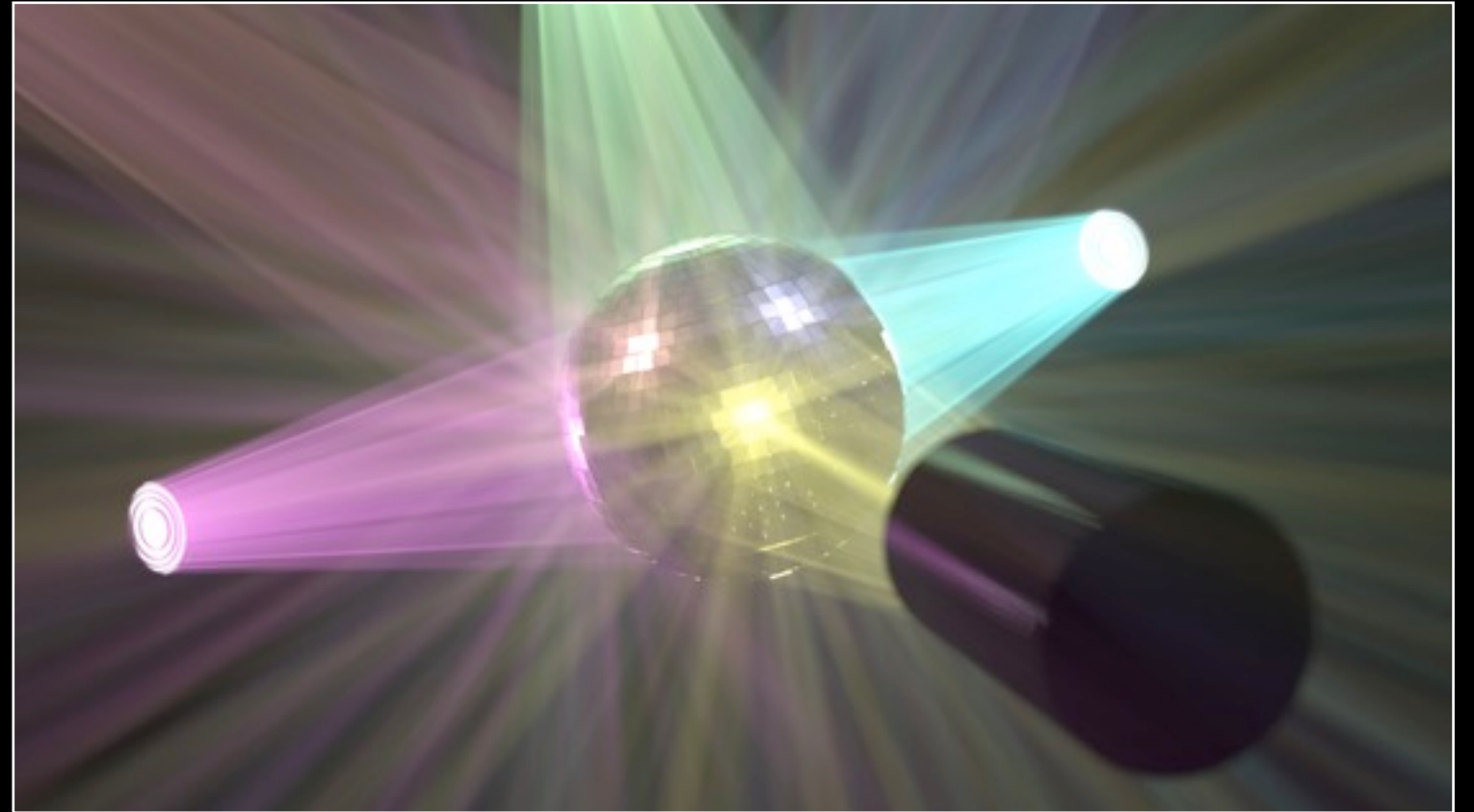
Average of Passes 1..16



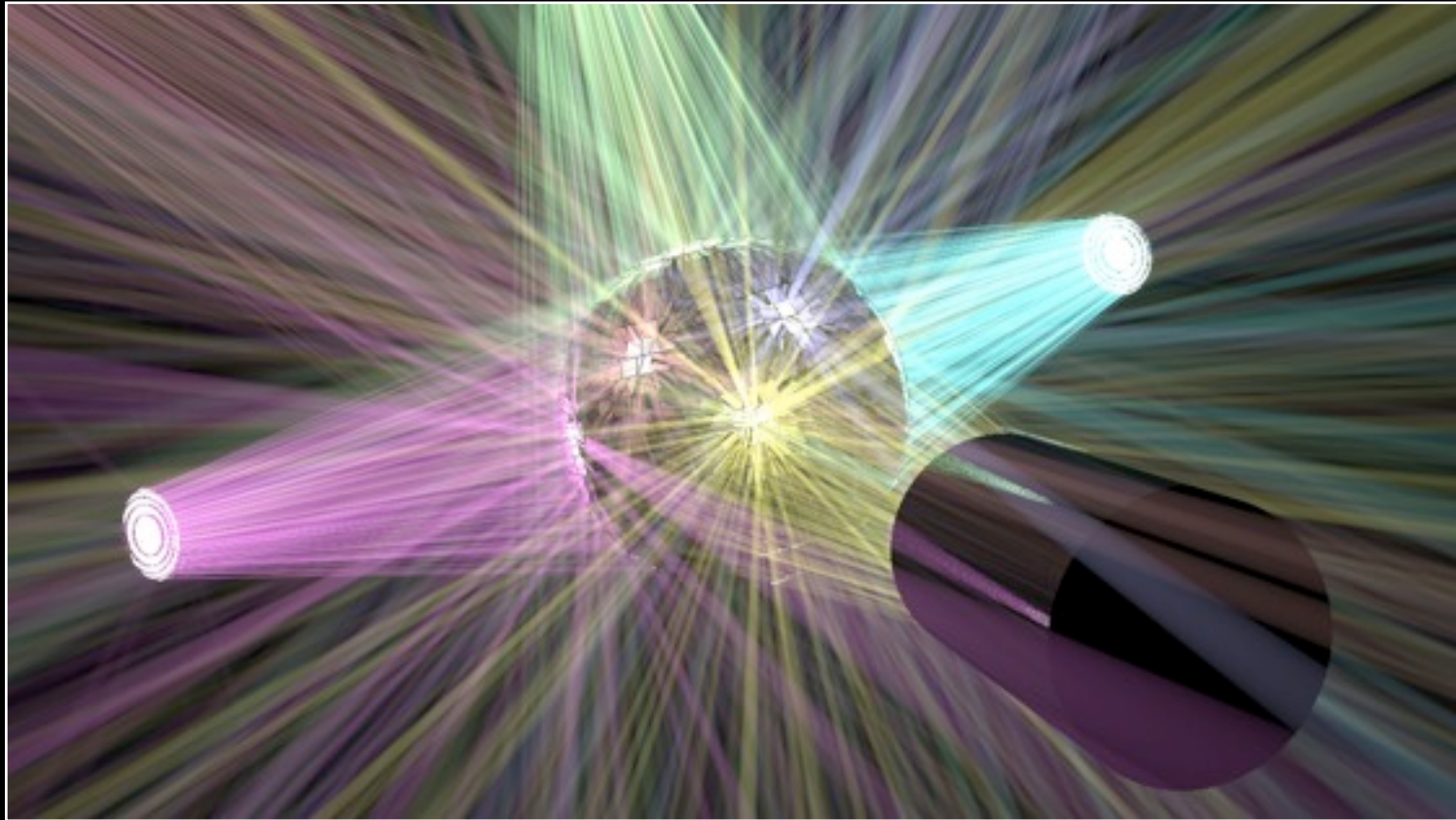
Pass 32



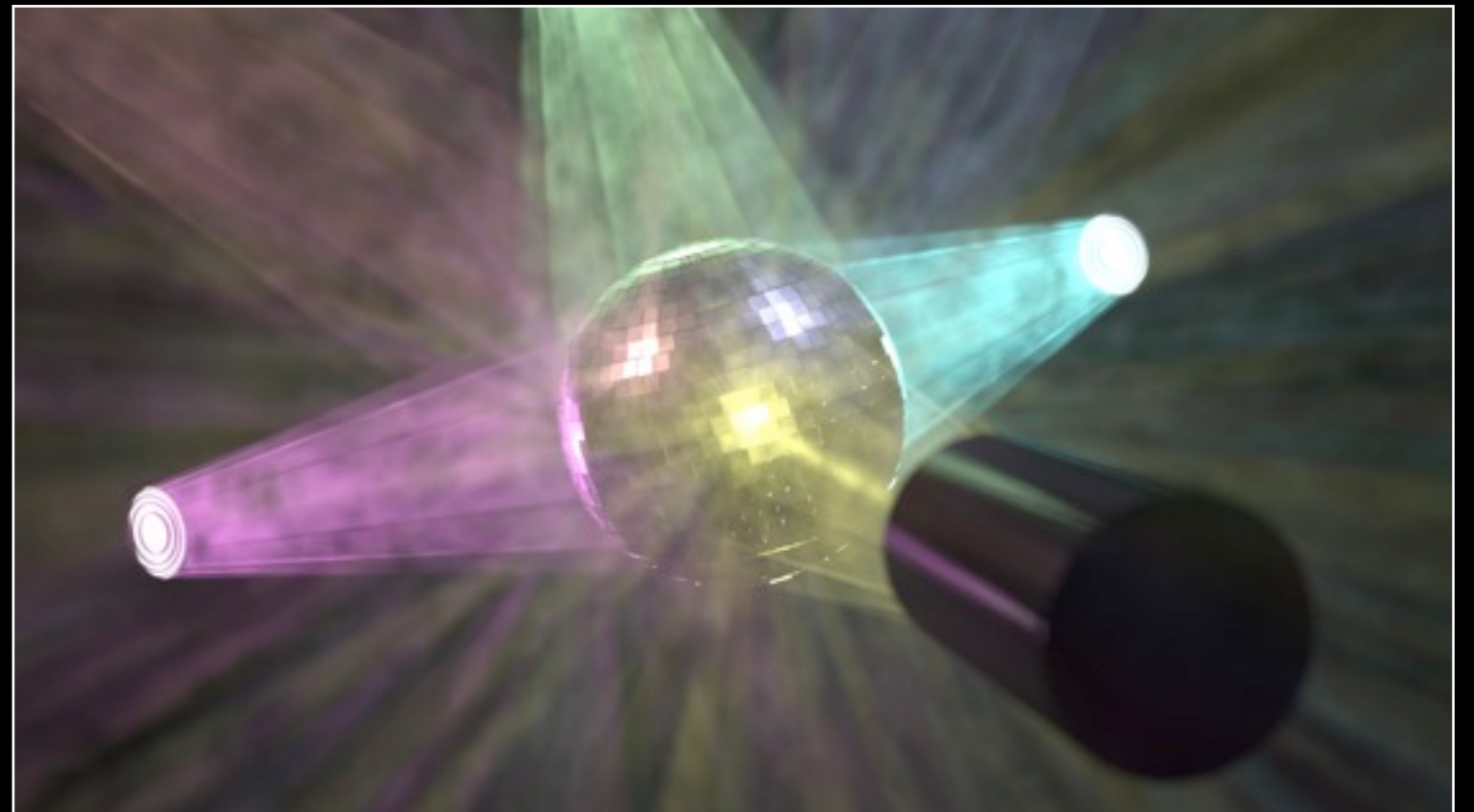
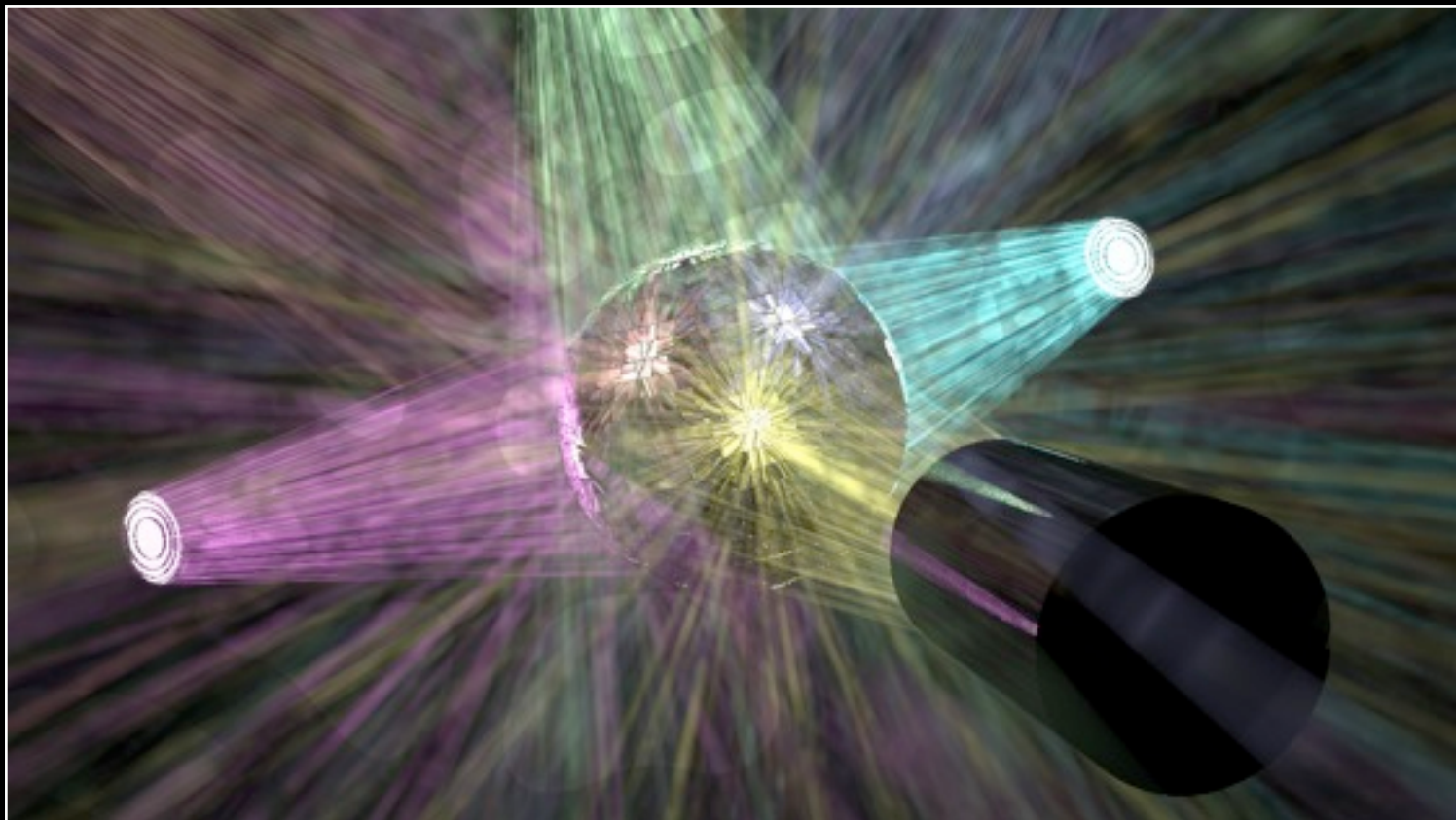
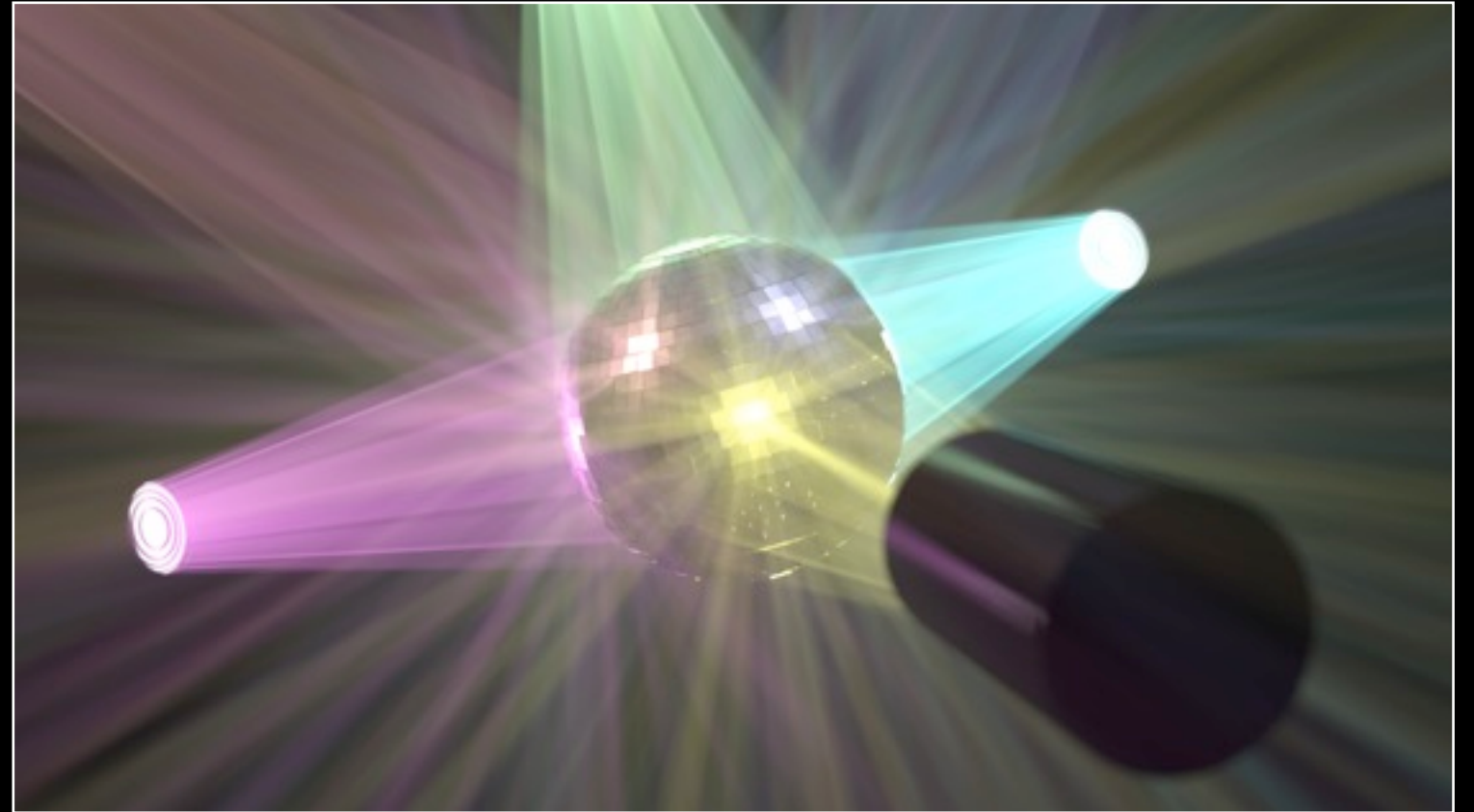
Average of Passes 1..32



Pass 64

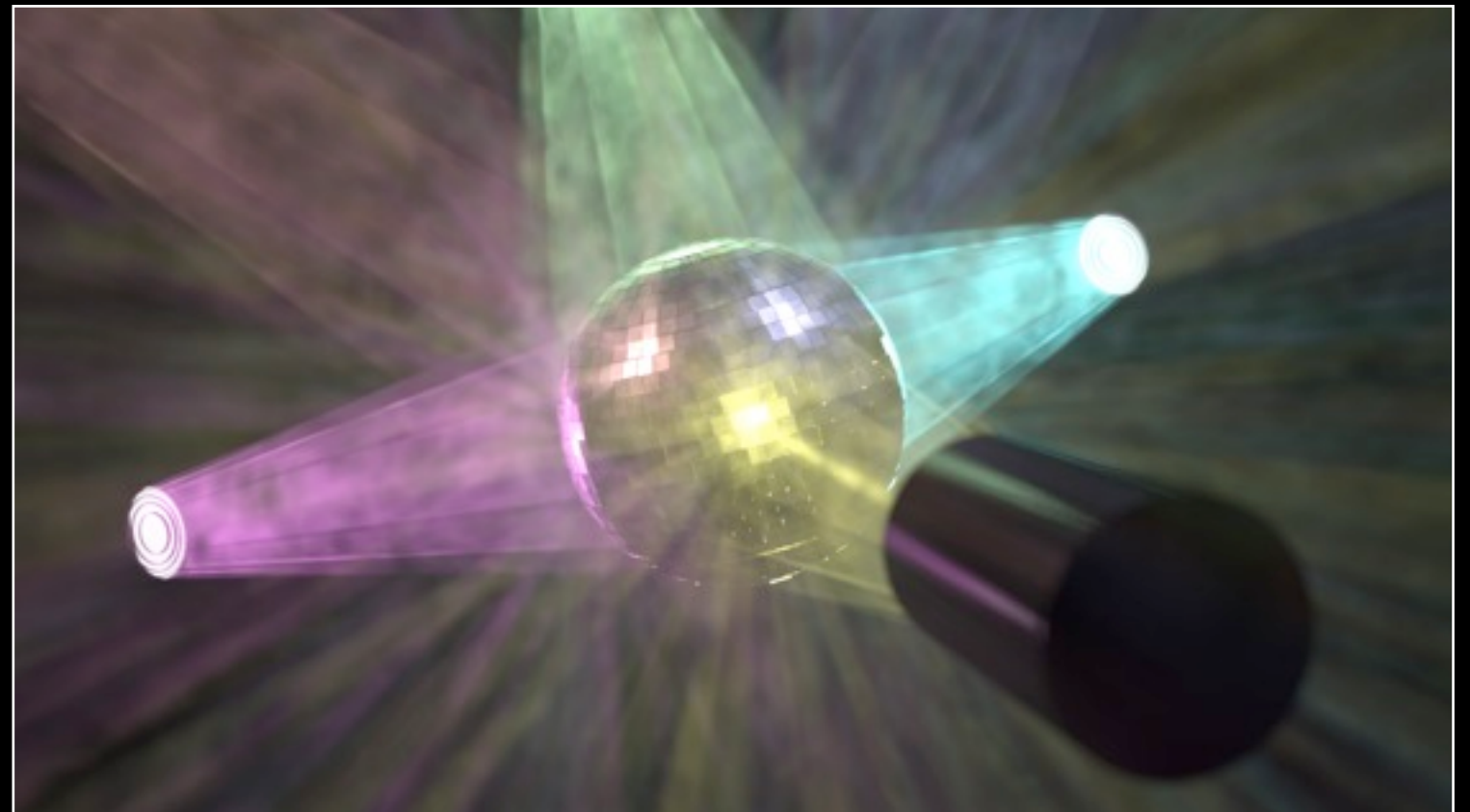
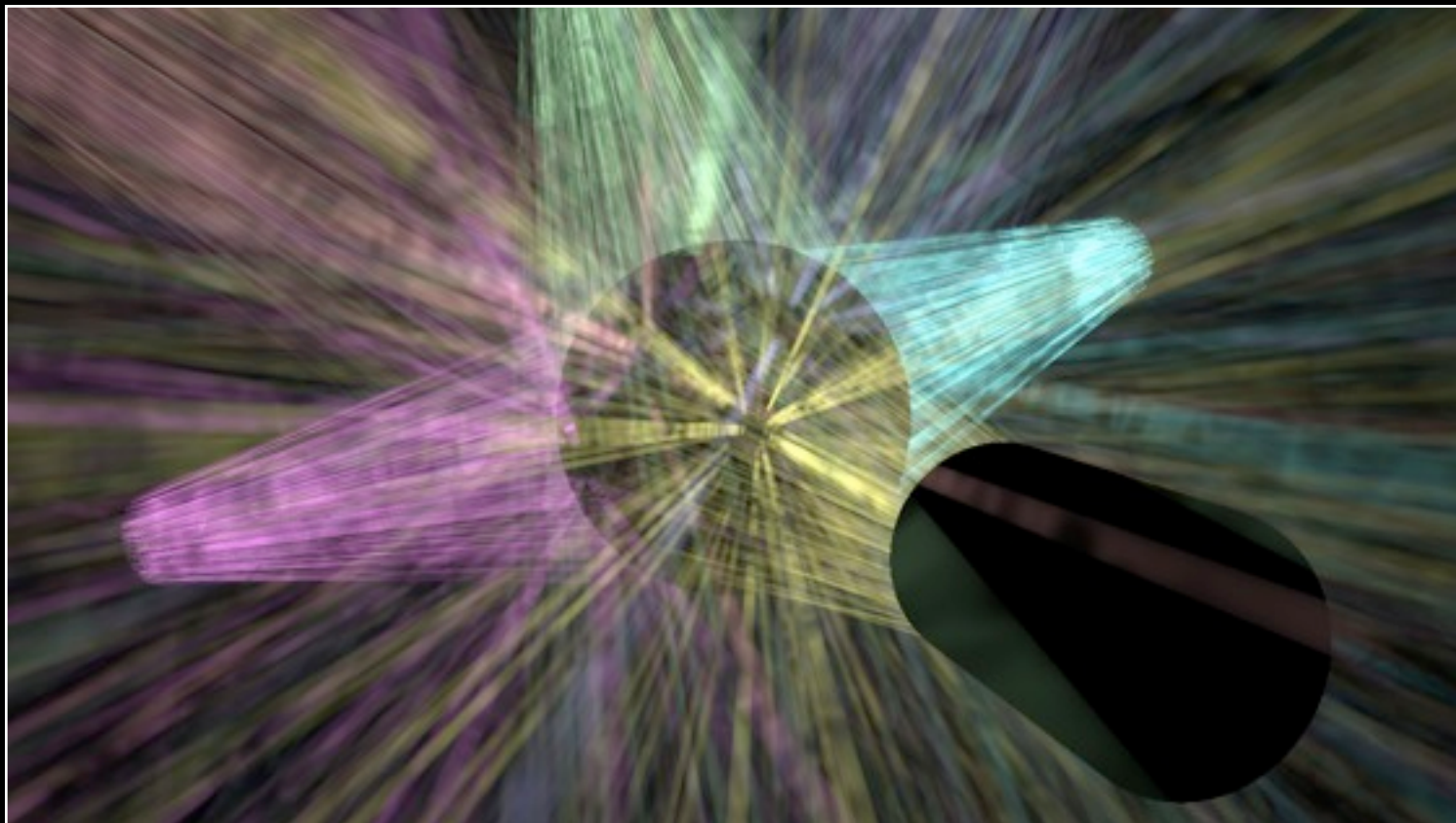
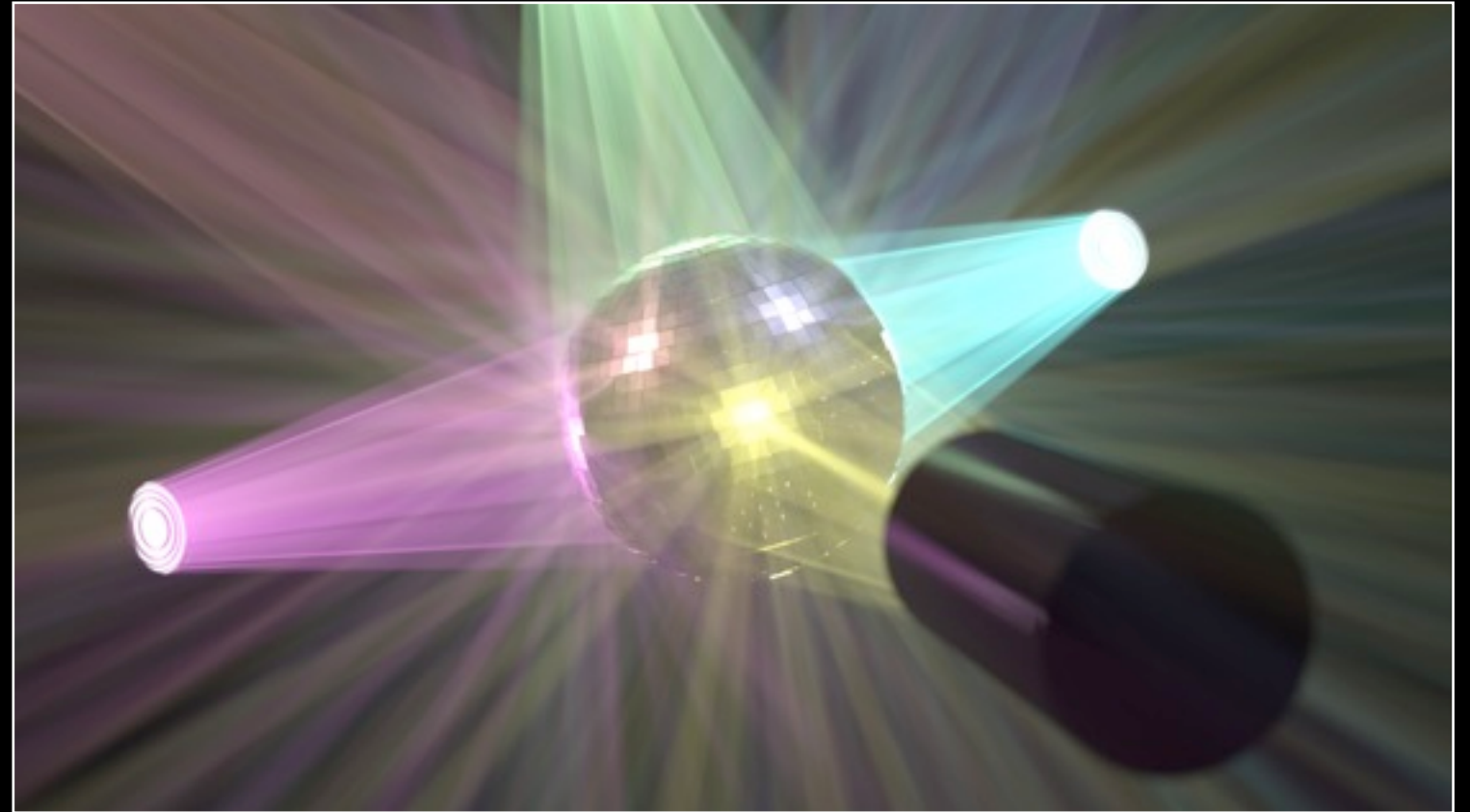
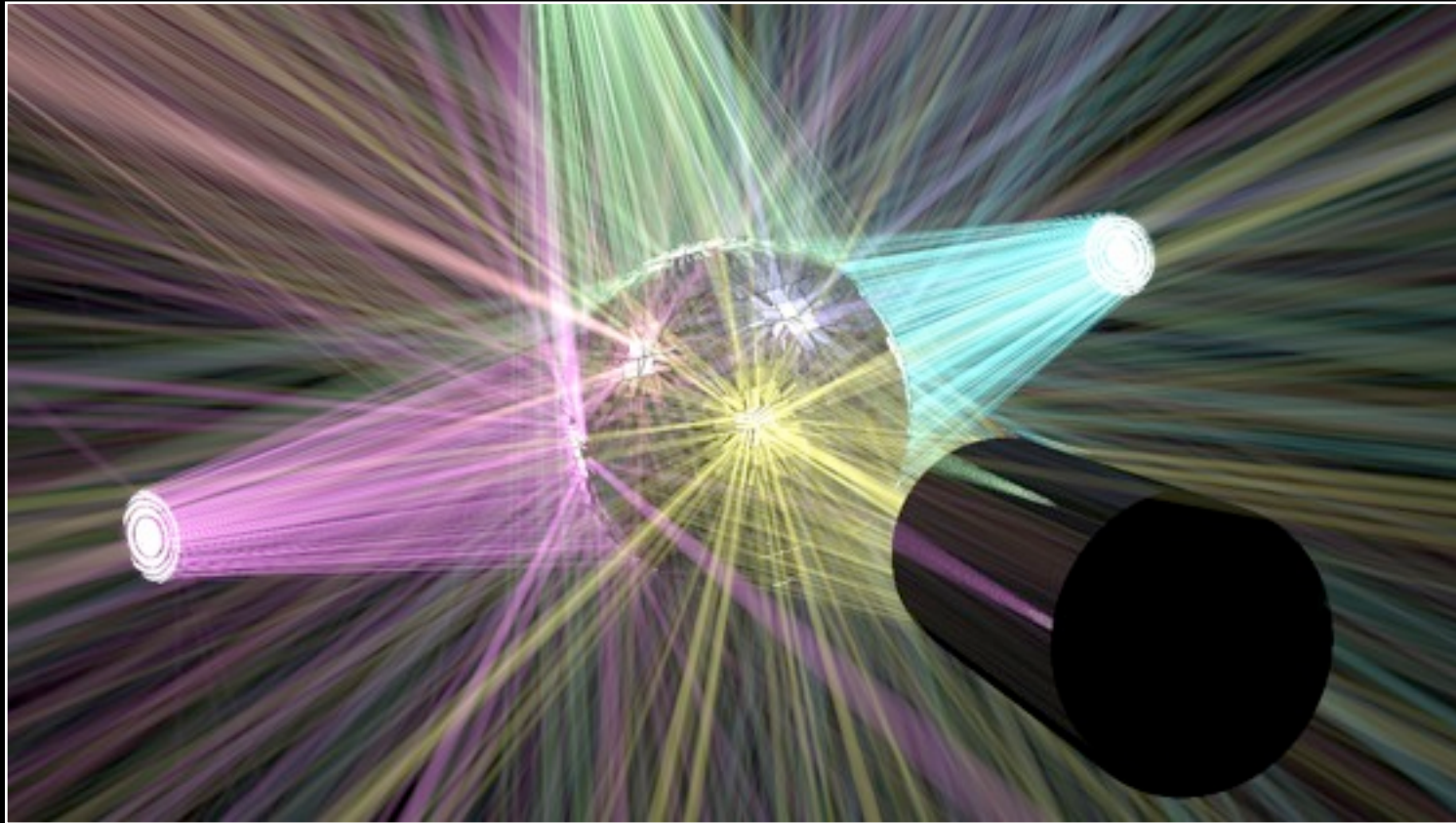


Average of Passes 1..64

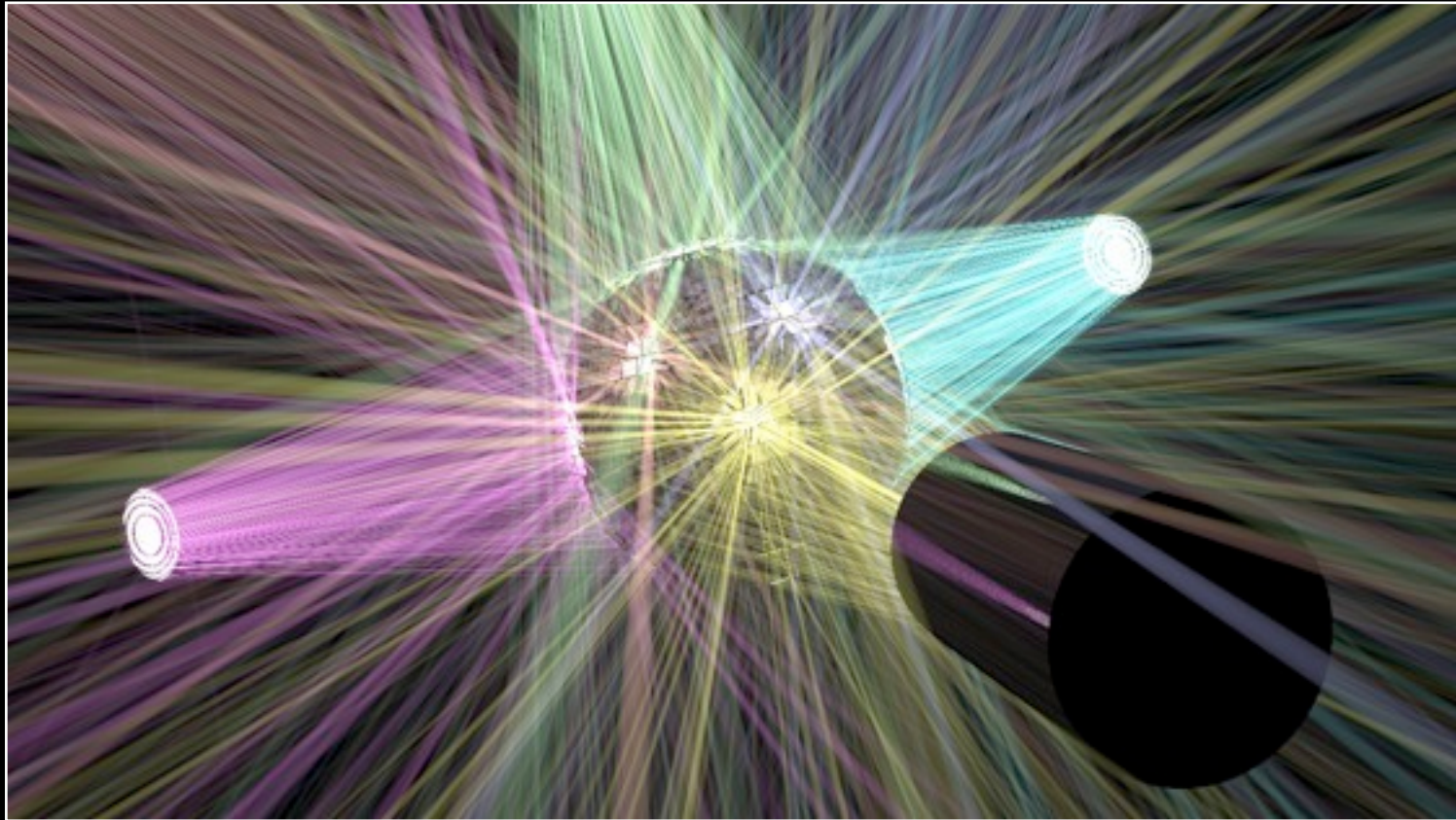


Pass 128

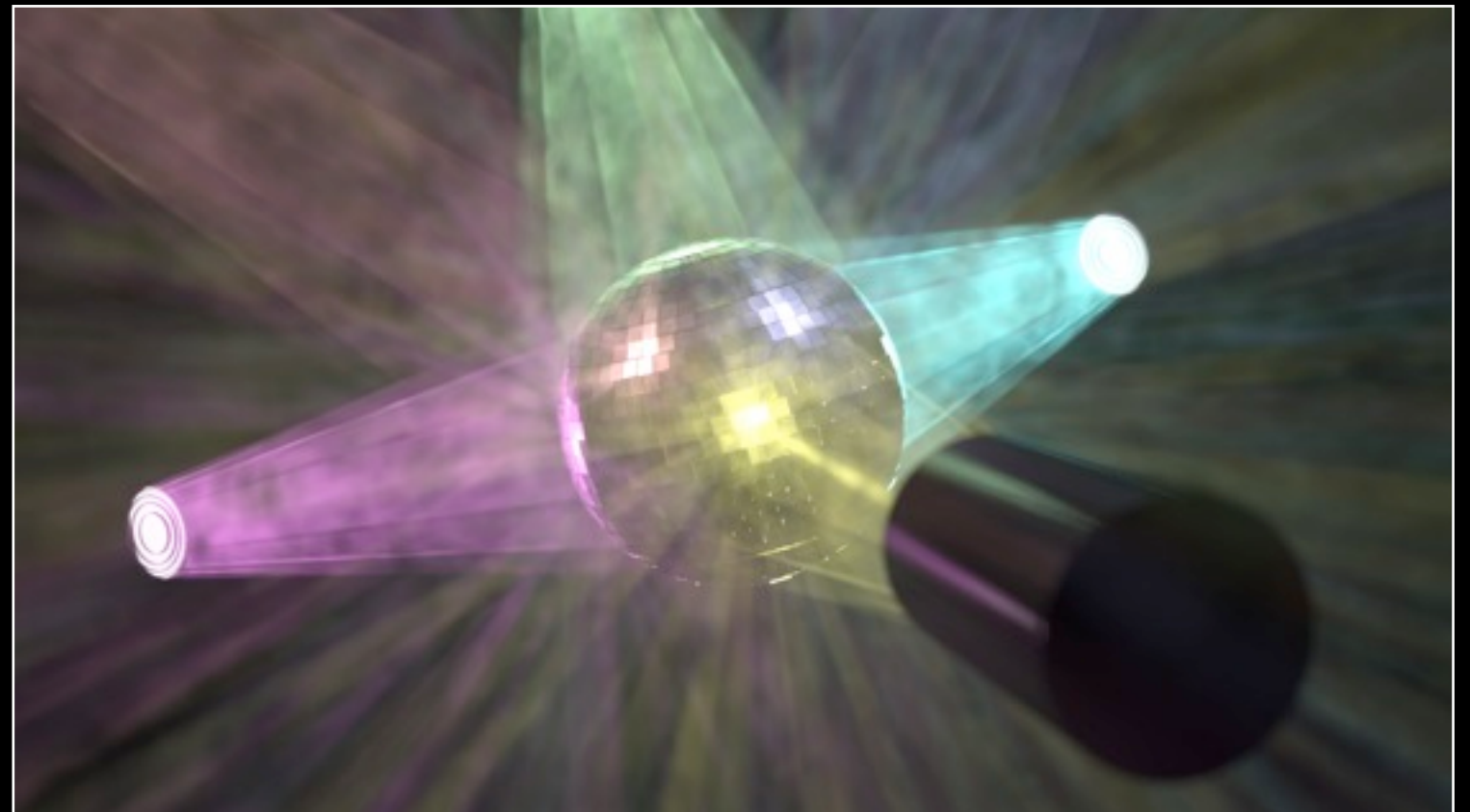
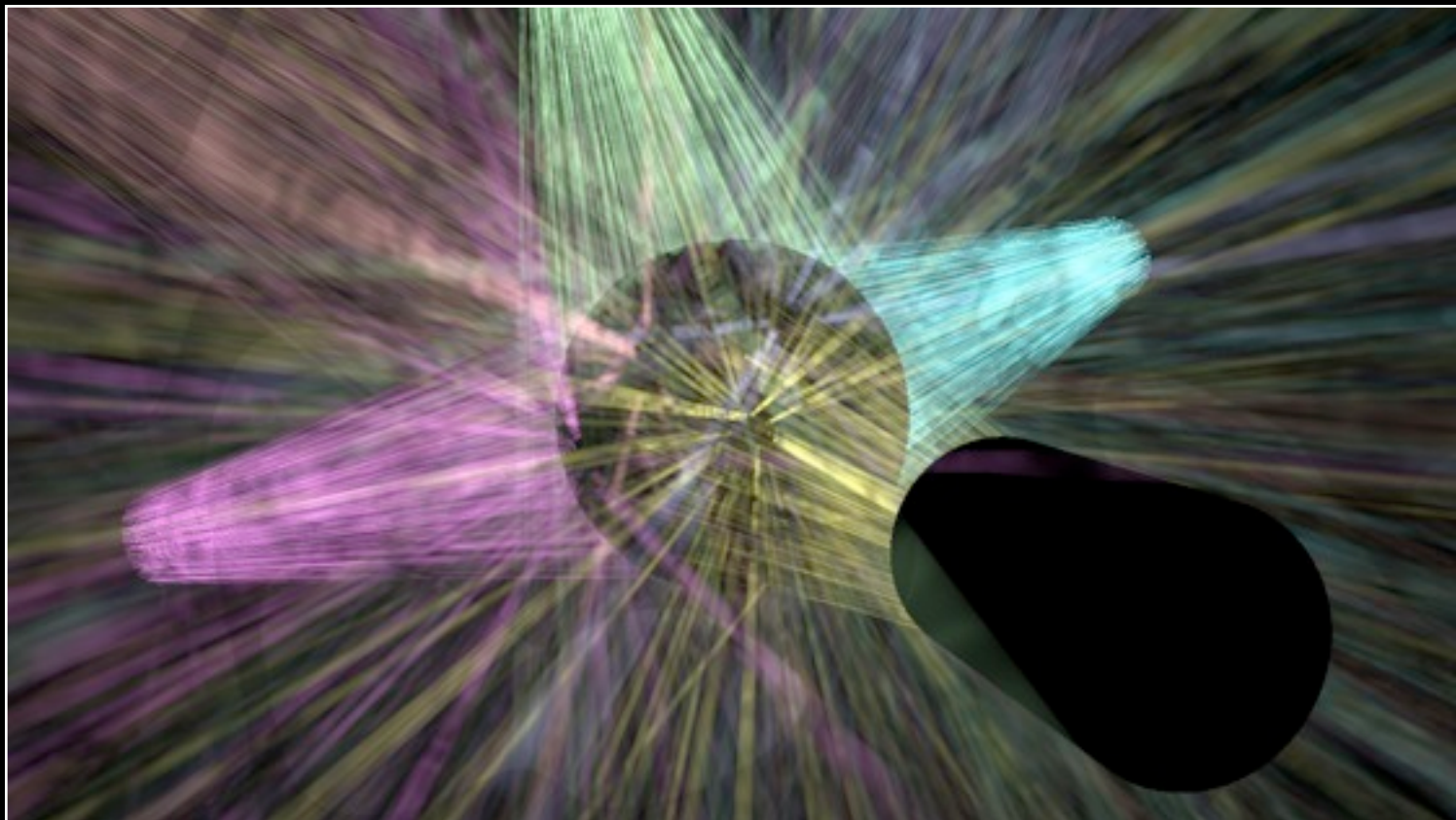
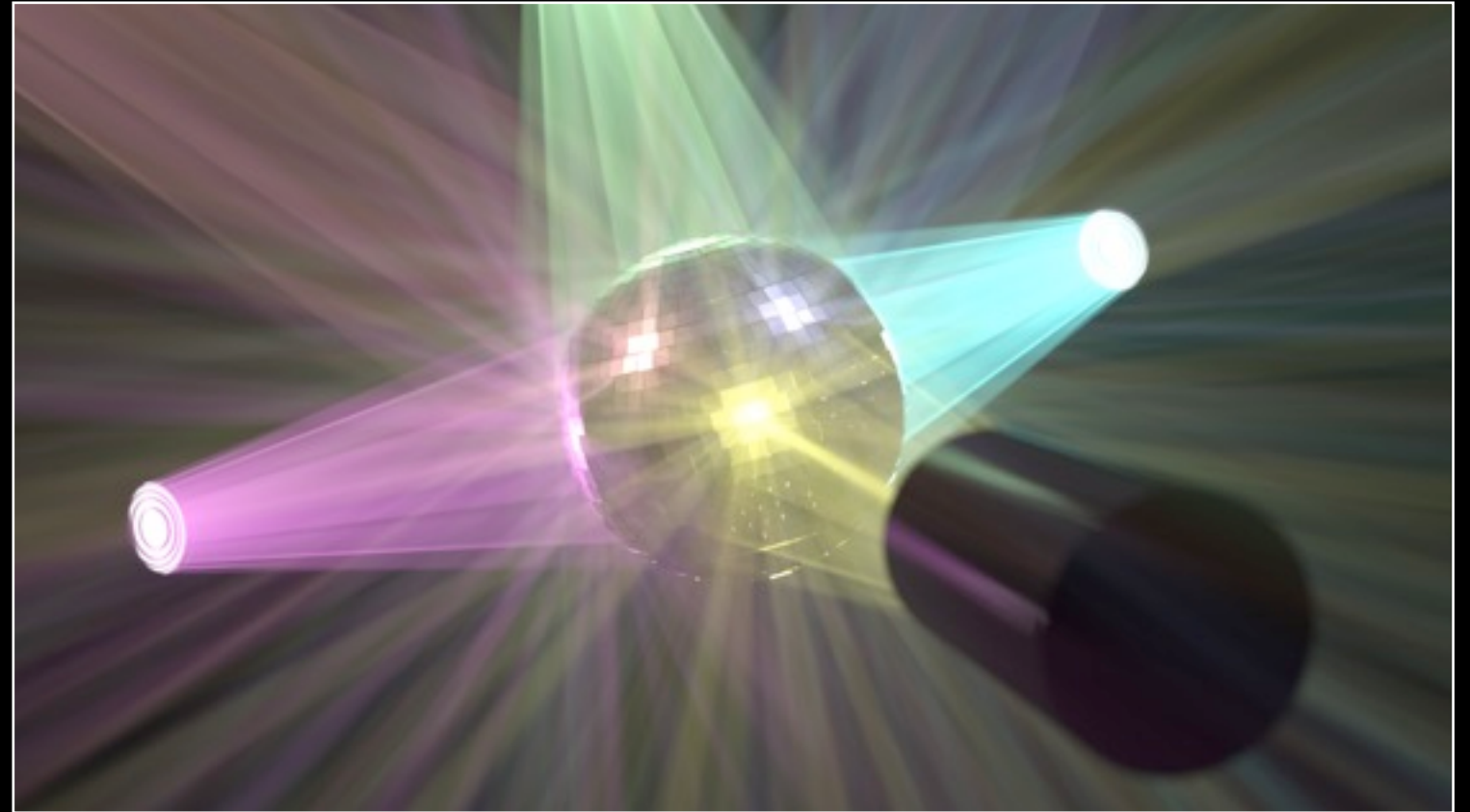
Average of Passes 1..128



Pass 256

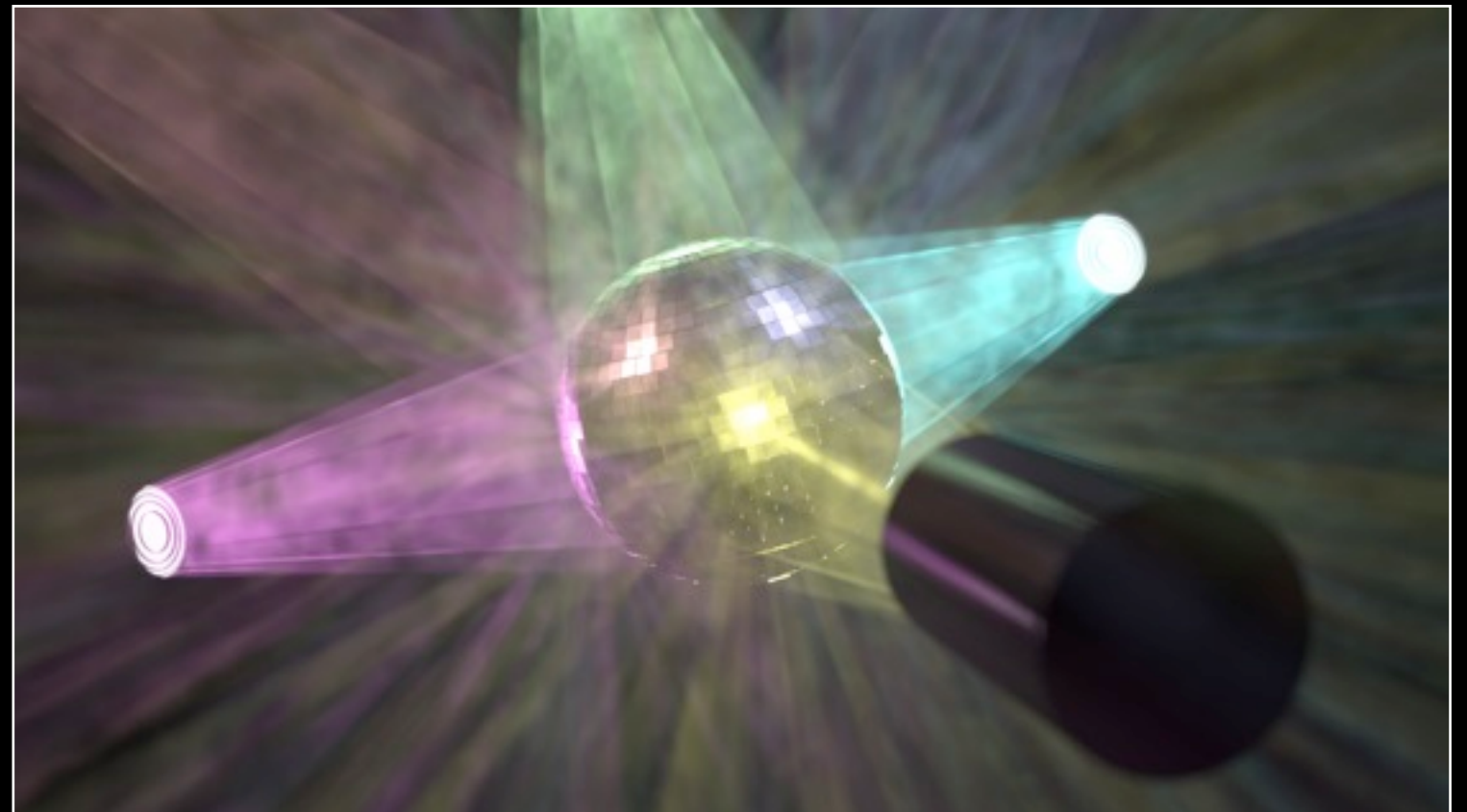
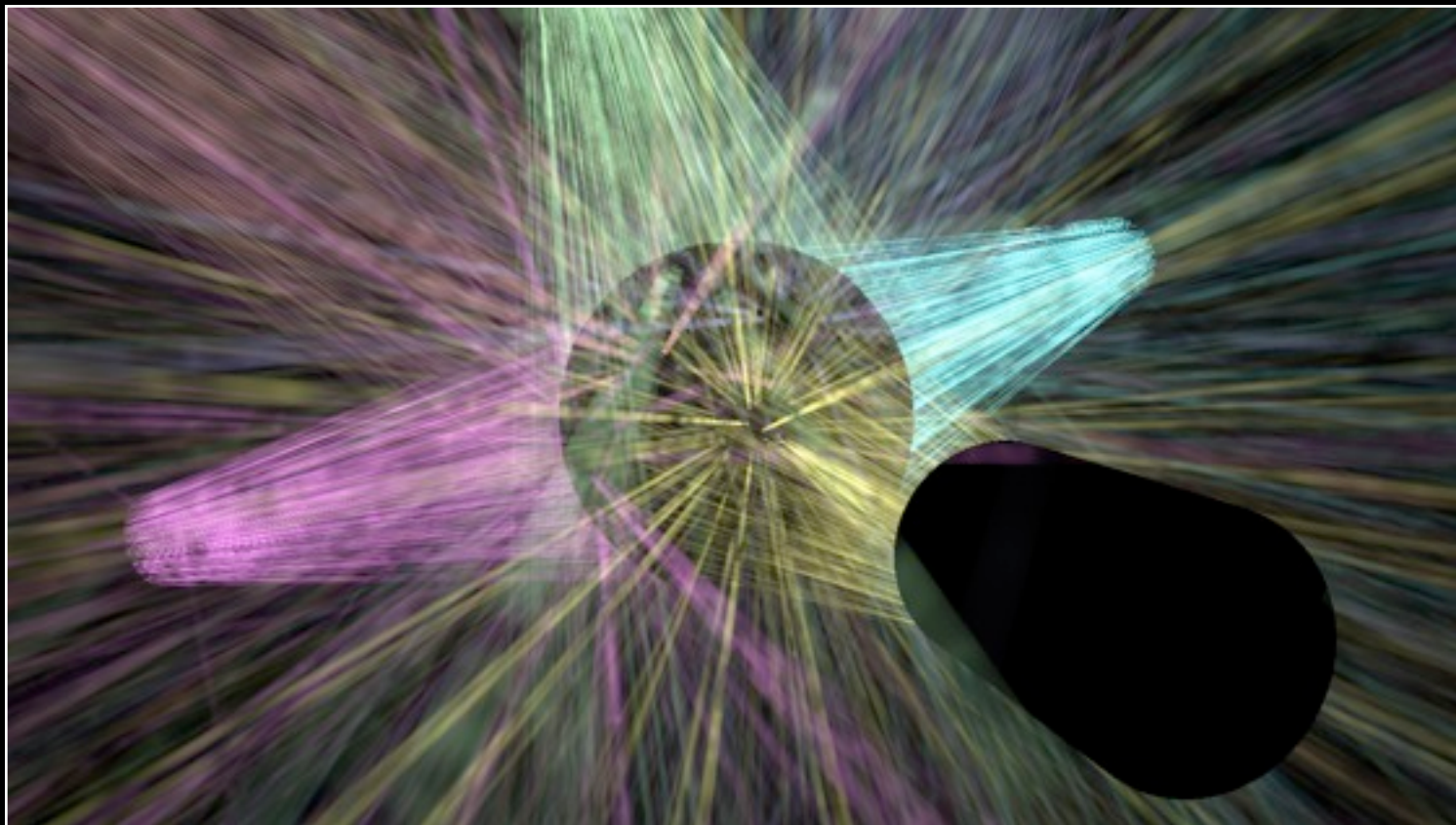
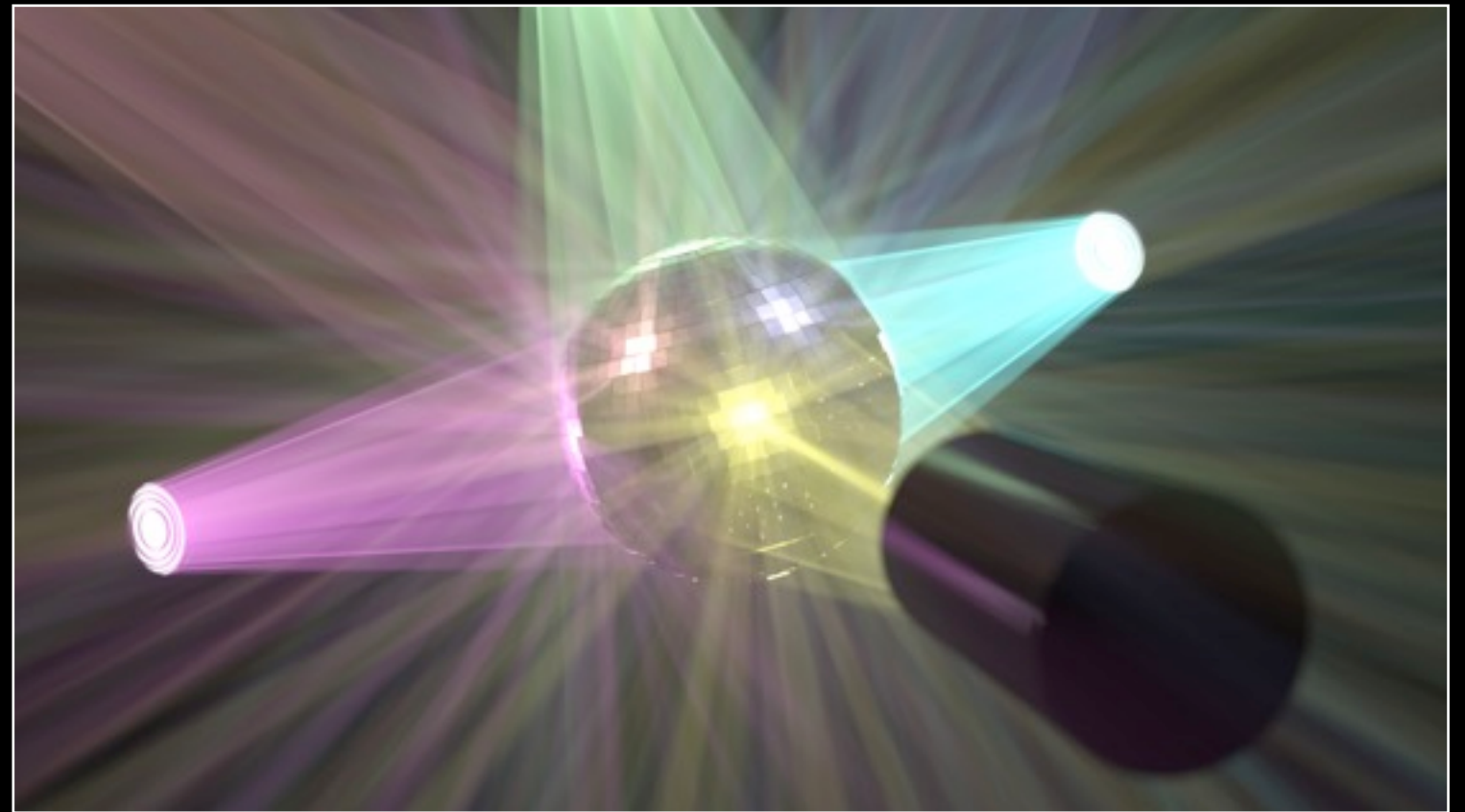
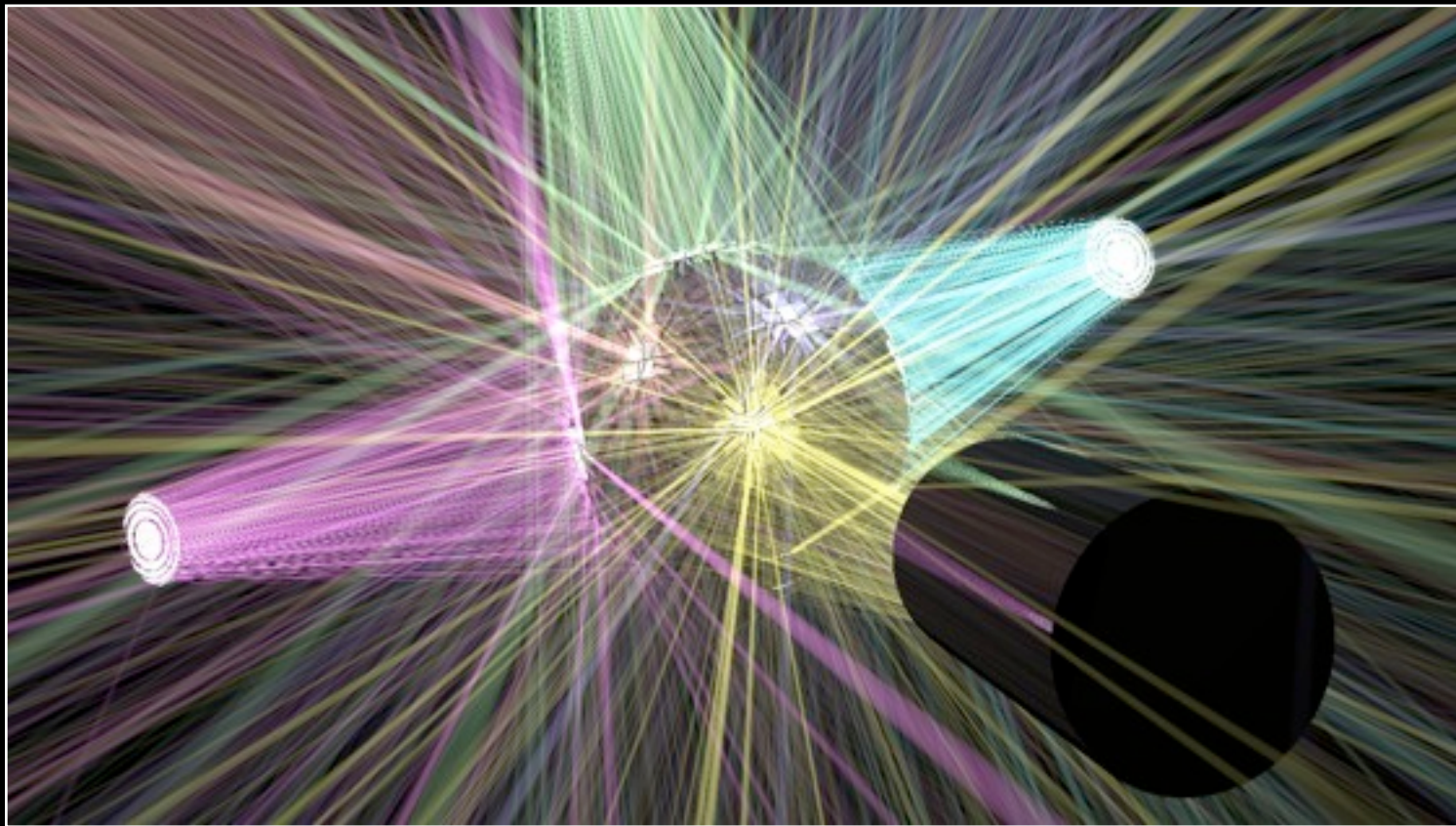


Average of Passes 1..256



Pass 512

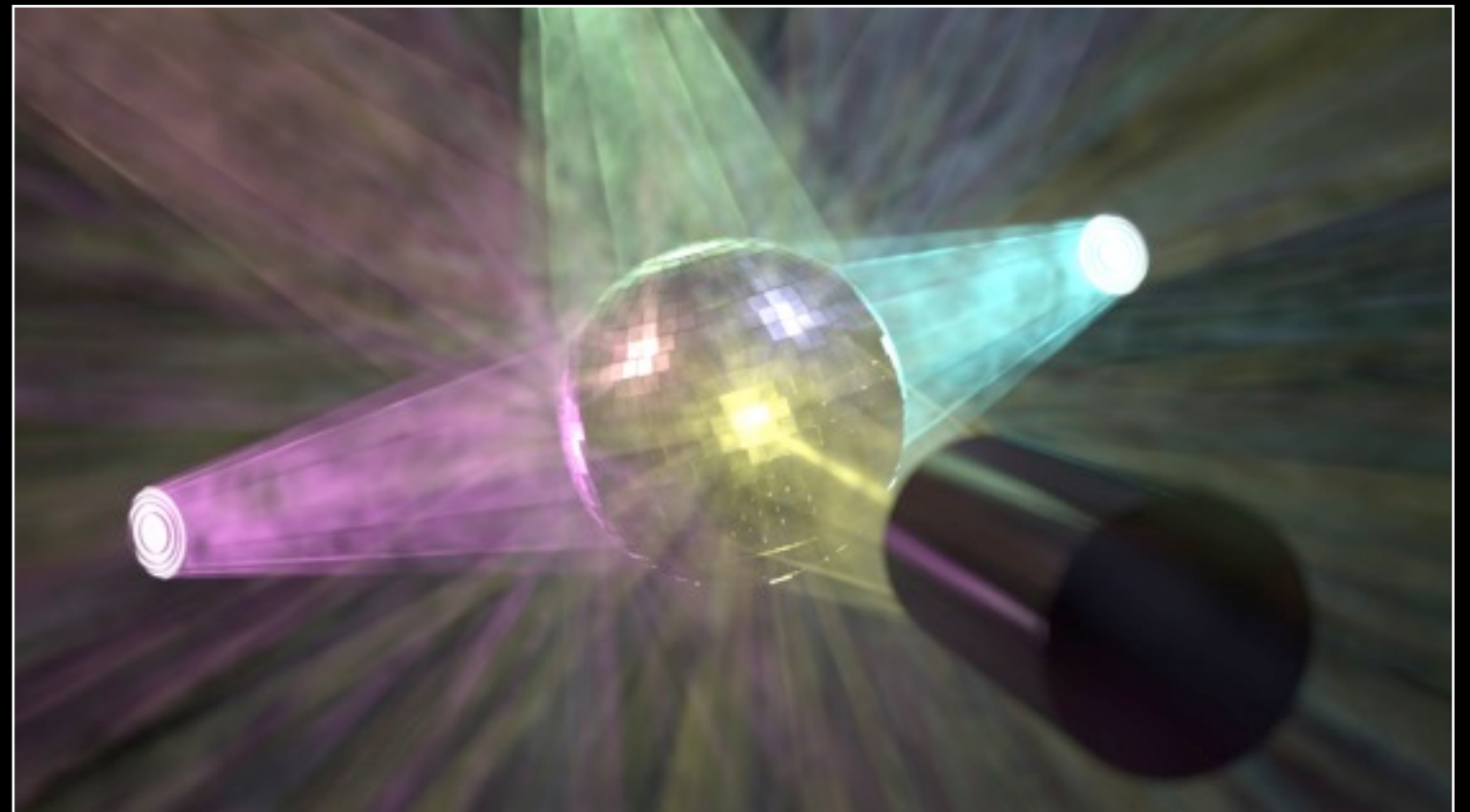
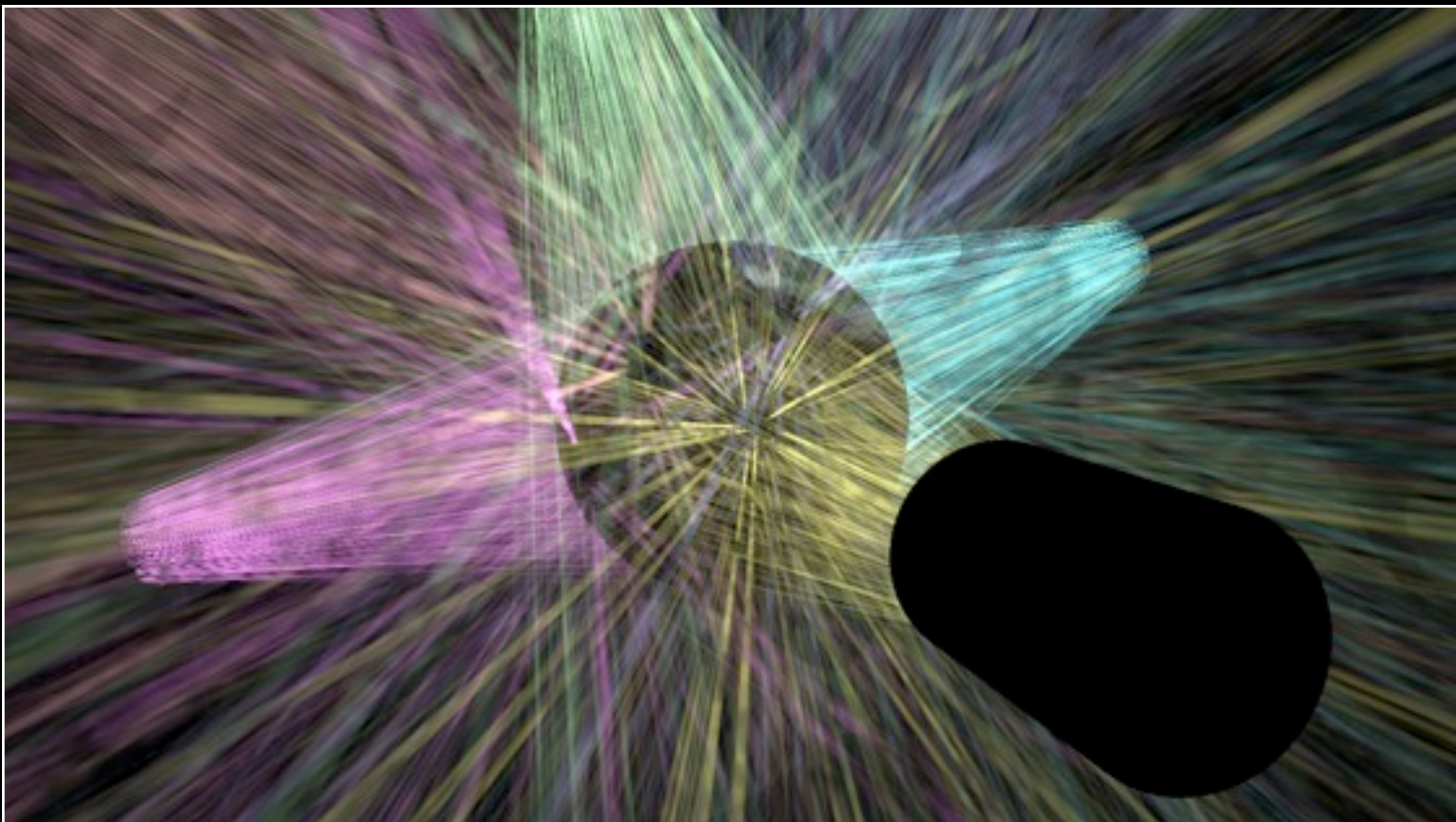
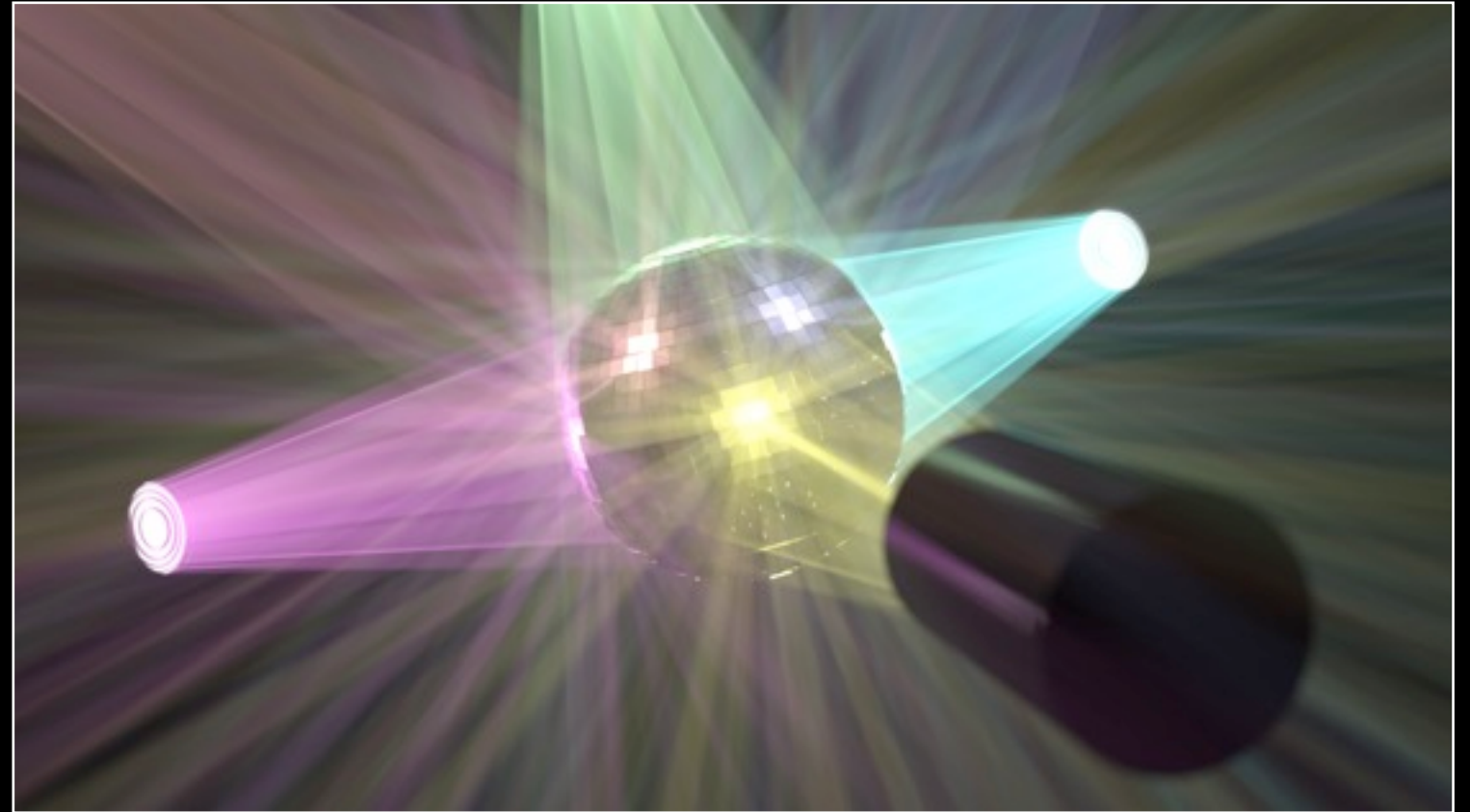
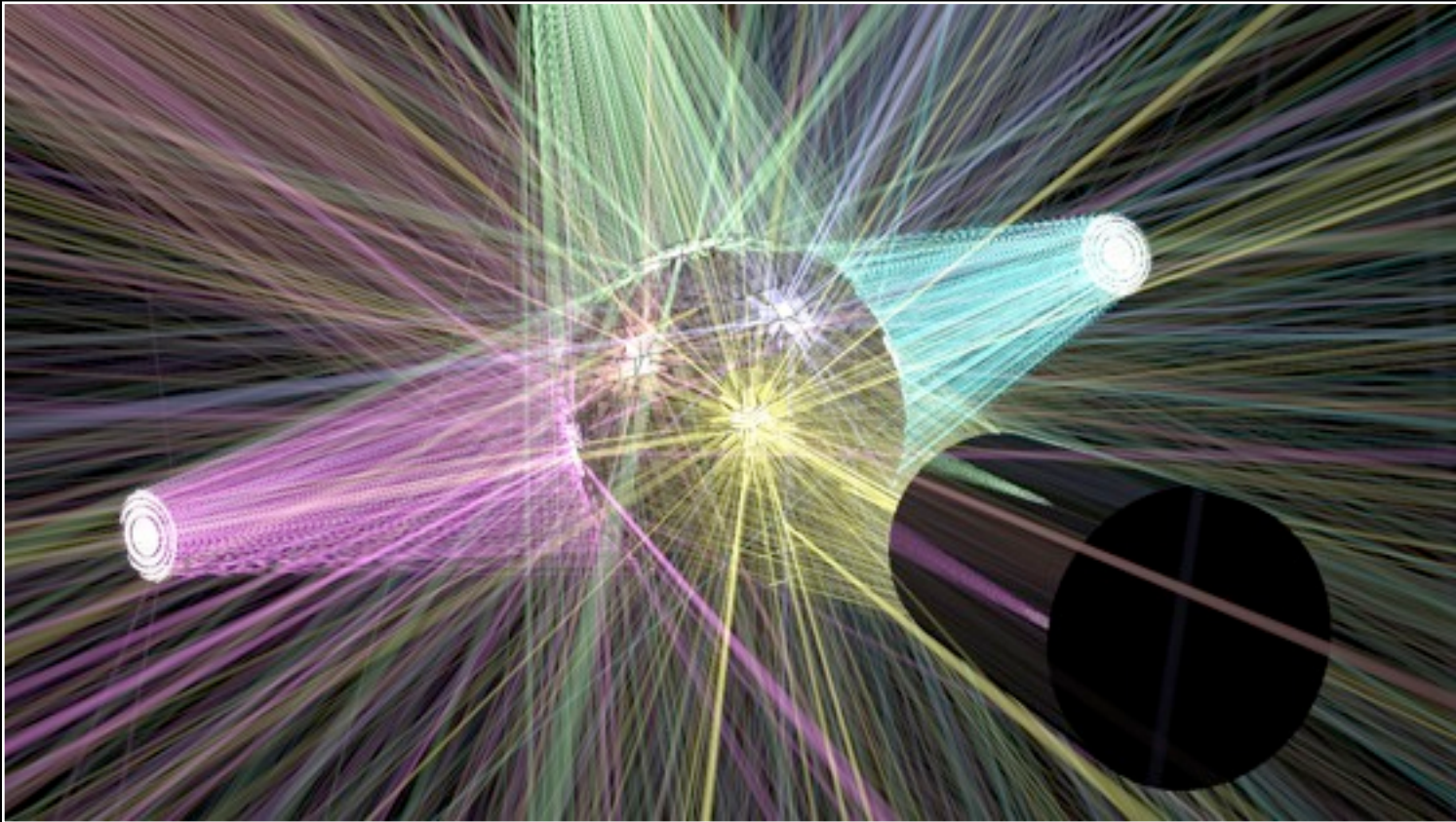
Average of Passes 1..512





Pass 1024

Average of Passes 1..1024



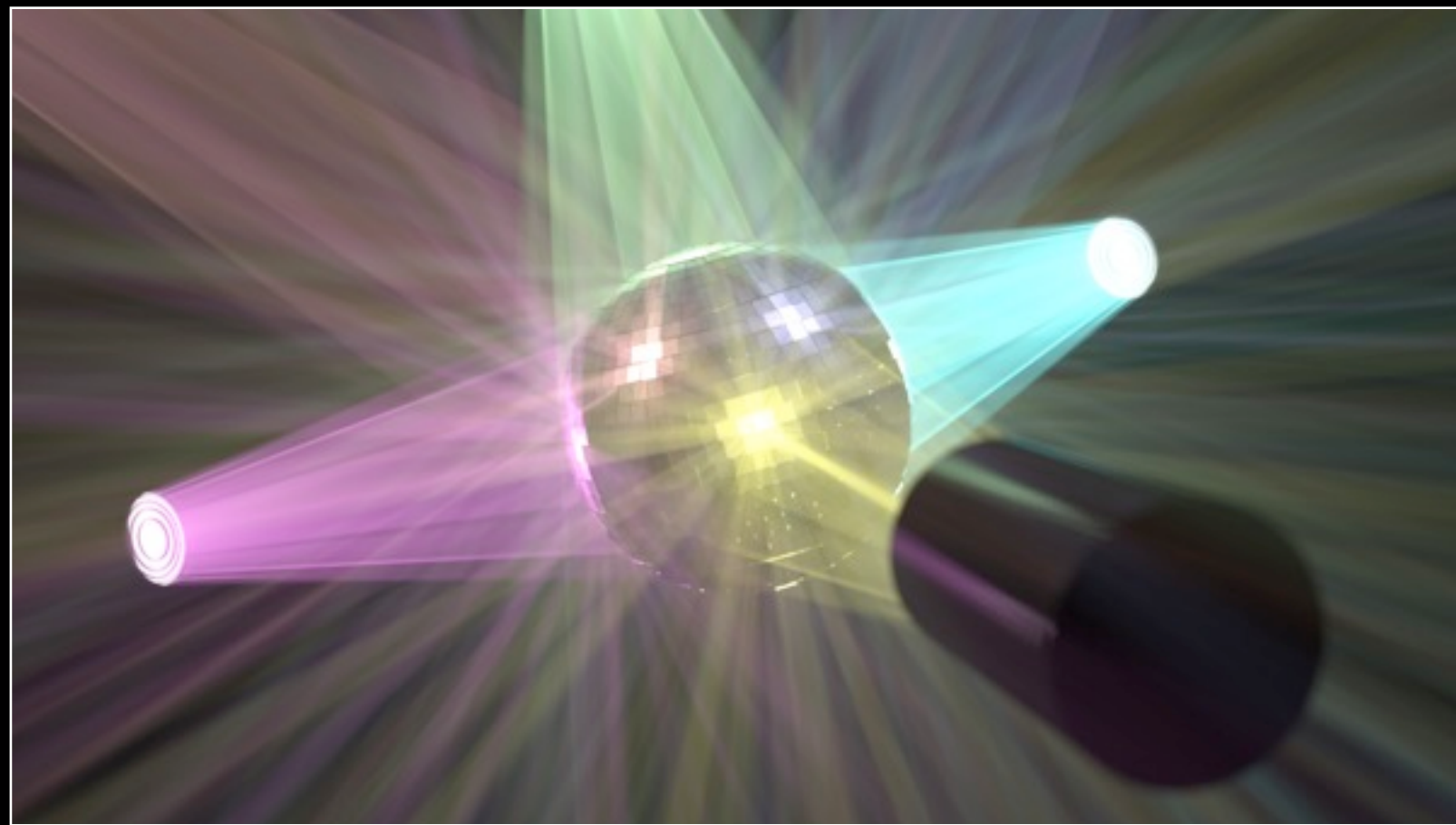
# DISCO

1280x720, Depth-of-Field

**Homogeneous**

19.67M Photon Beams

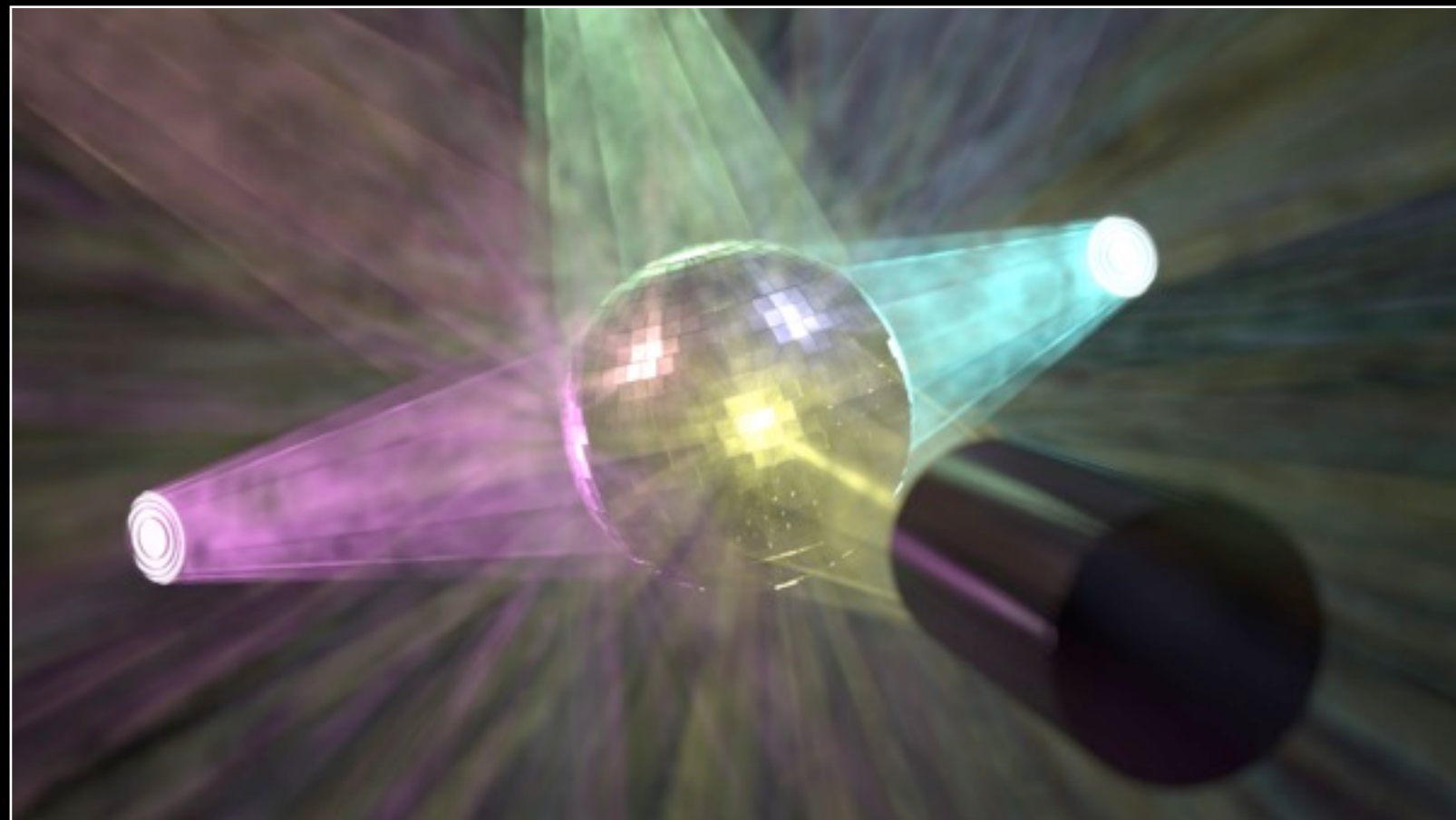
3 minutes



**Heterogeneous**

16.19M Photon Beams

5.7 minutes



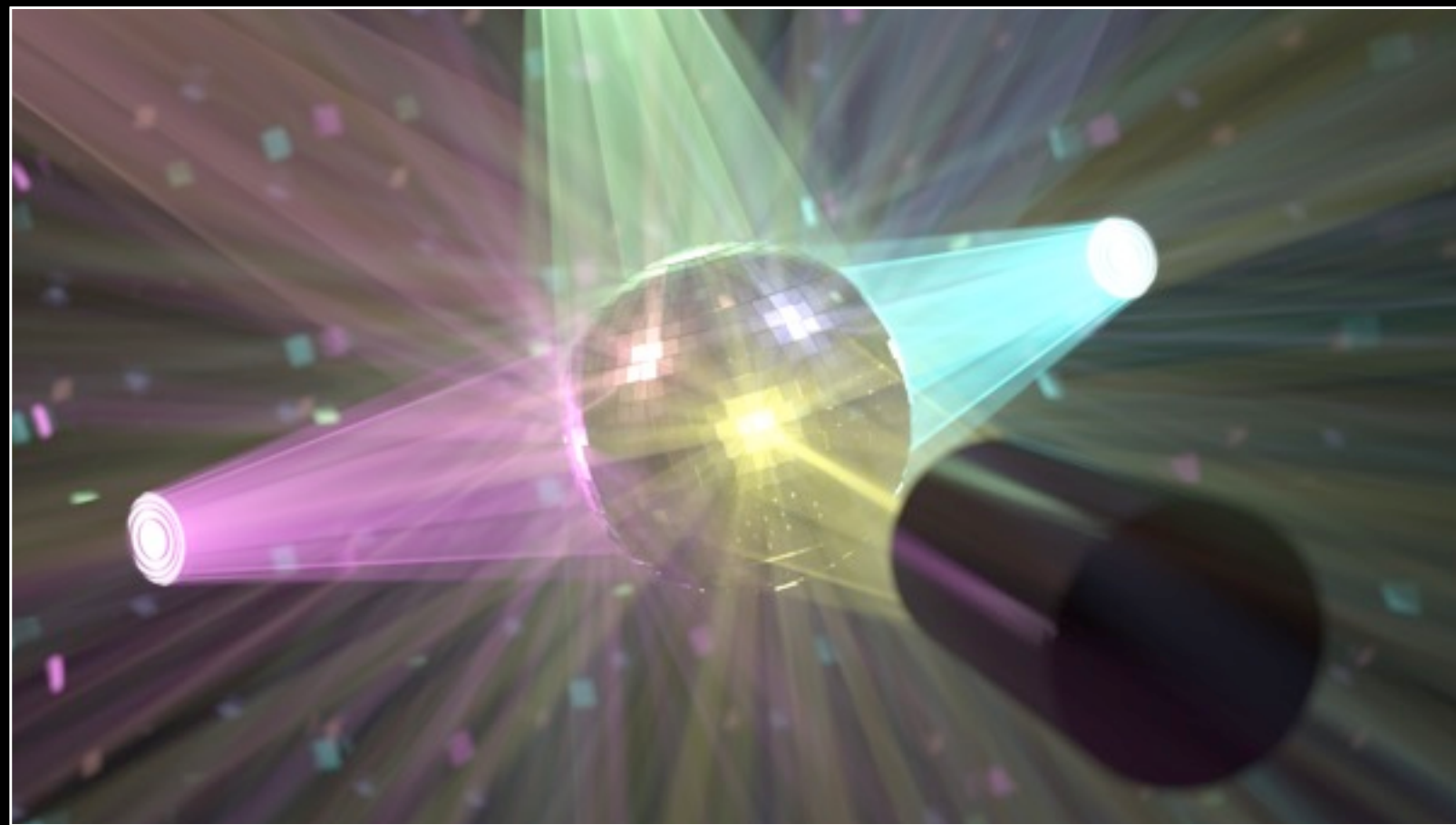
# DISCO

1280x720, Depth-of-Field

**Homogeneous**

19.67M Photon Beams

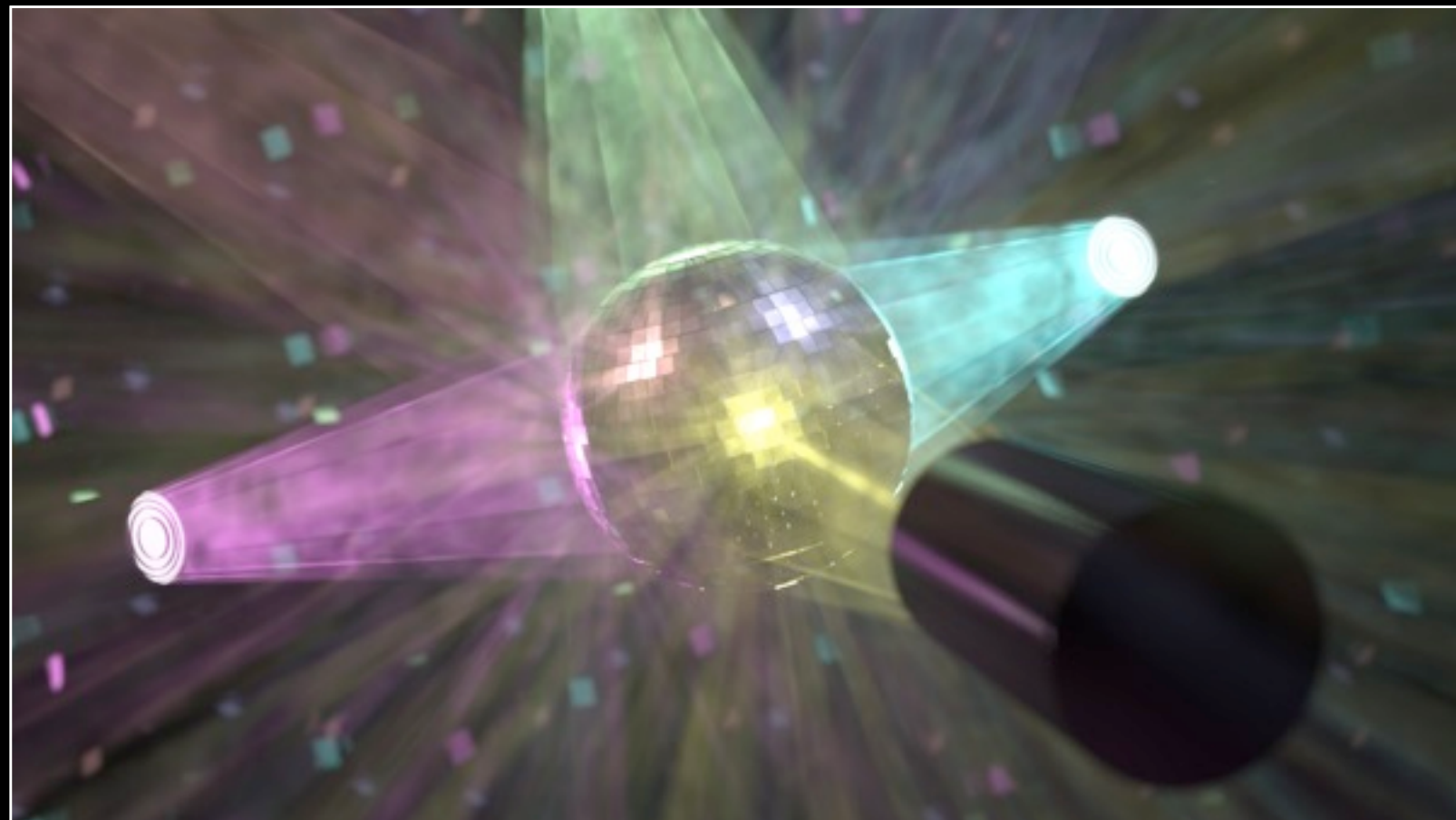
3 minutes



**Heterogeneous**

16.19M Photon Beams

5.7 minutes



# USER INTERACTION

## Hybrid CPU/GPU Implementation

```
Pass number (GPU): 5  
Pass number (CPU): 0  
Photons per pass: 10000  
Total render time: 0.36 s  
12 fps : 82 ms (Total time between redraws)  
17 fps : 60 ms (OpenGL rendering)  
53 fps : 19 ms (CPU beam shooting)  
876 fps : 1 ms (CPU camera tracing)
```



Homogeneous

```
Exposure: -0.250  
Gamma: 1.414  
Pass number (GPU): 22  
Pass number (CPU): 22  
Total render time: 5.27 s  
Photons per pass: 1000  
4 fps : 250 ms (Total time between redraws)  
23 fps : 43 ms (OpenGL rendering)  
176 fps : 6 ms (CPU beam shooting)  
6 fps : 180 ms (CPU camera tracing)
```



Heterogeneous

Real-time capture

# Questions?

